

Bayesian Learning

Lab 3

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Question 1

```
rainfall <- read.table("../data/rainfall.dat", header=F)
```

Prior

$$\begin{aligned}\mu &\sim N(\mu_0, \tau_0^2) \\ \sigma^2 &\sim \text{Inv-}\chi^2(\nu_0, \sigma_0^2)\end{aligned}$$

Likelihood

$$\mathbf{y}|\mu, \sigma^2 \sim N(\mu, \sigma^2)$$

Posterior

$$\begin{aligned}\mu|\sigma^2, \mathbf{x} &\sim N(\mu_n, \tau_n^2) \\ \sigma^2|\mu, \mathbf{x} &\sim \text{Inv-}\chi^2\left(\nu_n, \frac{\nu_0\sigma_0^2 + \sum_{i=1}^n (x_i - \mu)^2}{n + \nu_0}\right)\end{aligned}$$

where (?)

$$\begin{aligned}\mu_n &= \frac{\frac{1}{\tau_0^2}}{\frac{1}{\tau_0^2} + n} \mu_0 + \frac{n}{\frac{1}{\tau_0^2} + n} \bar{y} \\ \frac{1}{\tau_n^2} &= \frac{1}{\tau_0^2} + n \\ \nu_n &= \nu_0 + n\end{aligned}$$

a)

b)

c)

Question 2

a)

b)

c)