Dota 2: what should I pick?

Data Mining
Clustering and Association Analysis
732A61

Rasmus Holm

Abstract

The emergence of esports in the recent years have made it an ideal target for the data mining community. All the gameplay data and information surrounding it are stored on servers begging to be explored for knowledge. In this report the target is to analyze team compositions in the video game DOTA 2.

I show that it is possible to use association and cluster analysis to find interesting hero combinations in professional matches.

Introduction

Electronics sports, hereafter will be referred to as esports, are a form of competition using electronic systems, in particular video games, controlled by human players. In recent years, the revenue and audience have seen a rapid growth with an estimation of over 300 million viewers in 2016 and over \$450 million in global revenue, and it is expected to see a formidable growth in the near future.¹

The esports industry utilizes many different platforms such as personal computers (PCs), X-Box, Playstation, and since everything is electronic we could potentially utilize all that data that is being generated for various kinds of analyses. That could help organizations/teams find better strategies, improve the viewer experience, and help newcomers getting accustomed to the different games in a short time span, thus further increase the growth.

DOTA 2

Defense of the Ancients (DOTA 2) is a so called multiplayer online battle arena (MOBA) video game developed by Valve Corporation made first available in 2011. The game plays out as two teams of 5 players battle against each other where each player controls a hero, a character with unique abilities. The aim is to destroy the opponents ancient and thus win the game. How that is achieved varies from game to game, from fast paced game that are under 20 minutes to long drawn out game lasting over 60 minutes.

Draft Phase

The draft phase is the time the two teams pick their heroes that will be played during the gameplay phase. As of June 15, 2017, there are 113 unique heroes to select from. Each team has to pick 5 heroes, ban 5 heroes, and banned heroes are unavailable for either team to pick. The actual order is shown in figure 1.

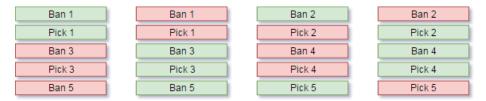


Figure 1: The pick and ban order read from left to right, top to bottom. The colors represent the two teams.

This phase is very tactical and determines a lot how the gameplay will pan out. The reason for that is that heroes have their strengths and weaknesses. The heroes of a team composition fulfill different purposes, very broadly speaking at what time periods they are weak or powerful. A useful term is the *metagame* that is globally influential on what heroes are being picked. It describes what strategies, heroes, and ideas about the game is currently popular and is heavily influenced by the developers' changes to the game, but also as the professional community figures out what works well.

¹https://newzoo.com/insights/articles/esports-revenues-will-reach-696-million-in-2017/

Questions

In this report I am going to use cluster and association analysis in order to figure out if it is possible to find relevant patterns that could help newcomers watch professional DOTA 2. The questions I have set to explore are mainly based the relationships between heroes. The relationship is either *synergistic*, e.g., hero X works well with hero Y, or *counteractive*, e.g., hero X is strong against hero Y.

- When should I pick hero X?
- Which heroes should I pick along with hero X?
- What are common team compositions overall?
- Do team compositions change between tournaments?

Theory

In this section I present the theory that is required to understand this report.

k-modes

k-means is one of the oldest and most well known clustering algorithms today. However, it is not well suited for categorical variables that is being used in this report, but k-modes by Zhexue Huang [6] is an extension to k-means for just that purpose.

The k-modes algorithm uses the simple matching dissimilarity measure for categorical objects and is formally

$$d_1(x_i, x_j) = \sum_{k=1}^m \mathbb{1}\{x_{i,k} \neq x_{j,k}\},\$$

where $\mathbb{1}\{\cdot\}$ is the indicator function and x_i , x_j are vectors of m categorical values.

Let $X = [x_1, x_2, ..., x_n]$ be a set of categorical objects describe by categorical attributes $A_1, A_2, ..., A_m$. A mode of dataset X is a vector $q = [q_1, q_2, ..., q_m]$ that minimizes

$$d(X,q) = \sum_{i=1}^{n} d_1(x_i, q).$$

Let $n_{c_{k,j}}$ be the number of objects having the kth category $c_{k,j}$ in attribute A_j and $f_r(A_j = c_k, j|X) = \frac{n_{c_{k,j}}}{n}$ is the relative frequency of category $c_{k,j}$ in X. The function d(X,q) is minimized by selecting the mode according to $f_r(A_j = q_j|X) >= f_r(A_j = c_{k,j}|X)$ for $q_j \neq c_{k,j}$ for all $j = 1, \ldots, m$.

The cost function becomes

$$P(W,Q) = \sum_{l=1}^{k} \sum_{i=1}^{n} \sum_{j=1}^{m} w_{l,i} \mathbb{1}\{x_{i,j} \neq q_{l,j}\},\$$

where $q_l = [q_{l,1}, q_{l,2}, \ldots, q_{l,m}]$ and $w_{l,i} \in \{0,1\}$, $\sum_{l=1}^k w_{l,i} = 1$, and $0 < \sum_{i=1}^n w_{l,i} < n$. This can be minimized iteratively similar to how k-means does it, but instead using the simple matching dissimilarity measure, working with cluster modes, and updating those modes according to the above criteria. Since this algorithm converges to a local optima the initial set of modes are important, therefore I decided to use the initialization method by Cao et al. [1] based on density to do that automatically.

The ordering of the categorical attributes in the dissimilarity measure above matters because it do not make any assumptions about their domains. In the analyses done in this report the domain is the same for all variables so the ordering should not matter in this particular case. So I will also use an alternative dissimilarity measurement defined below.

Let x_i and x_j be two vectors of length m, then the dissimilarity measure is defined as

$$d_2(x_i, x_j) = n - \sum_{k=1}^m \sum_{l=1}^m \mathbb{1}\{x_{i,k} == x_{j,l}\}.$$

Method

As esports is a rather new phenomenon, there have not been much analyses around it in the literature. However, some research have been made in DOTA 2 such as a recommendation engine for picks based on machine learning by Conley and Perry [2]. Summerville et al. [3] have used supervised learning to predict picks in the draft phase. In this report, it is more of interest to explore patterns in the draft using data mining rather than machine learning which is lacking in the literature. The techniques applied are of unsupervised nature; meaning there are no defined "right" answers.

Dataset

DOTABUFF² is a website that contains detailed information and statistics about both competitive and casual matches. The dataset used in this article consists of all the matches from all the Valve major championships³ until June 15, 2017, and all the Internationals from 2012 stored by DOTABUFF. That covers 3028 matches in total. The reasoning behind the choice of events is that those events are the most prestigious and have the highest prize pools; teams are therefore unlikely to hold back on any secret strategies.

Experimentation

In order to investigate the questions given in the introduction, I conducted four experiments using association and cluster analysis. I used the ROCK [4] and k-modes clustering algorithms for finding clusters and FP-Growth algorithm [5] for finding association rules.

Association Analysis

When should I pick hero X?: To keep a realistic scope I chose two particular heroes in mind, Anti-Mage and Clinkz, to analyze when they should be picked according to patterns in professional matches from Valve events. The reasons for those are that they are niche picks that have very specific strengths and weaknesses. Anti-Mage, as his name suggests, is a mobile hero that is extra strong against magical damage heroes. Clinkz, on the other hand, is very mobile due to his ability of becoming invisible and can deal huge amount of physical damage to a single target.

What they have in common during the drafting phase is that they are usually picked as 4th or 5th pick, indicating that they are counter picks to the opposing teams heroes. In Valve events, Anti-Mage was picked 4th or 5th in 153 out of 180 matches and, Clinkz, 93 out of 102 matches. The analysis will thus look at combinations of heroes in the team compositions against 4th or 5th pick Anti-Mage or Clinkz.

What hero(es) should I pick along X?: For similar reasons above, I decided to choose two heroes, Io the Wisp and Magnus. Io is very good at adding mobility and durability to heroes, and is most commonly picked early in the draft since it can be combined with many heroes depending on the opponent's picks.

²https://www.dotabuff.com/

³http://wiki.teamliquid.net/dota2/Dota Major Championships

Magnus is good at buffing melee heroes and initiate engagements, thus being flexible enough to be picked in all stages of the draft.

The complete dataset of 3028 matches, 6056 team compositions, is used in order to find answers to this question.

Cluster Analysis

Hero Combinations: An important part of understanding DOTA 2 is to understand the heroes and how they might synergize. The first step in doing so is to find common hero combinations which is the purpose of this analysis. Due to performance issues with ROCK on larger datasets it had to be excluded from the analysis.

Evolution of the Metagame: The metagame shapes how the game is being played and is important for games in esports. To investigate whether it is possible to detect differences between events in DOTA 2, I chose the Shanghai and Manila Majors that were played in 2016, approximately 3 months apart. The number of observations are 598 and 642 respectively.

Evaluation

To evaluate the results from the analyses they have to be analyzed by either players, analysts, or enthusiasts that have a fairly good understanding of the game and the heroes in particular. I decided upon using qualitative analysis based on my own knowledge gained from watching a lot of professional games over the years and therefore heard professional game analysts' opinions about the game.

Result

In this section I will present the analyses that were done. I will start of presenting the association analysis followed by the cluster analysis.

Association Analysis

In the introduction I asked two questions about hero picks, when to pick certain heroes and with what other heroes, and to investigate those questions I decided upon using association analysis with the FP-Growth algorithm. The analyses are presented below.

When should I pick hero X?

As mentioned in the method, the focus was on Anti-Mage and Clinkz and tables 1 and 2 show the respective rules that were found.

| Antecedent | Consequent |
|--------------|------------|
| Razor | Rubick |
| Ember Spirit | Dark Seer |
| Sand King | Rubick |
| Naga Siren | Dark Seer |

Table 1: Association rules by FP-Growth algorithm of 153 team compositions against 4th or 5th pick Anti-Mage. The parameters were set to minimum support of 5 and minimum confidence of 0.4.

| Antecedent | Consequent |
|------------|-------------|
| Dark Seer | Juggernaut |
| Gyrocopter | Earthshaker |
| Tiny | Io |

Table 2: Association rules by FP-Growth algorithm of 180 team compositions against 4th or 5th pick Clinkz. The parameters were set to minimum support of 5 and minimum confidence of 0.5.

Which hero(es) should I pick along X?

The rules selected contained either Io or Magnus in either the antecedent or consequent. Table 3 shows the rules found for Io by FP-Growth

| Antecedent | Consequent |
|---------------------|------------|
| Earthshaker, Tiny | Io |
| Tiny, Beastmaster | Io |
| Tiny, Rubick | Io |
| Earthshaker, Io | Tiny |
| Tiny, Queen of Pain | Io |
| Tiny, Batrider | Io |

Table 3: Association rules containing Io by FP-Growth algorithm of 6028 team compositions. The parameters were set to minimum support of 10 and minimum confidence of 0.5.

and table 4 contains the rules that include Magnus.

| Antecedent | Consequent |
|--------------------------|------------|
| Vengeful Spirit, Magnus | Juggernaut |
| Templar Assassin, Magnus | Juggernaut |
| Silencer, Magnus | Juggernaut |
| Witch Doctor, Magnus | Juggernaut |

Table 4: Association rules containing Magnus by FP-Growth algorithm of 6028 team compositions. The parameters were set to minimum support of 5 and minimum confidence of 0.5.

Cluster Analysis

In this section I will present the two different cluster analyses that have been conducted. The presented results are manually selected and only partial. The complete set of clusters can be found in the appendix at the end of the report. The analyses have utilized k-modes and ROCK algorithms and follow the questions in the introduction, What are common team compositions overall? and Do team compositions change between tournaments?, and they are described below.

Note that the tables contain numbers beside the hero names and those correspond to the frequency of the particular hero in the cluster.

Hero Combinations

Some of the hero combinations found by k-modes are found in tables 5 and 6

| | Clusters | |
|------|--|--|
| Size | Samples | |
| 614 | Queen of Pain: 195, Disruptor: 193, Dark Seer: 191, Lifestealer: 93, Rubick: 122 | |
| 014 | Earthshaker: 43, Queen of Pain: 195, Gyrocopter: 61, Disruptor: 193, Dark Seer: | |
| | 191 | |
| 486 | Io: 203, Earthshaker: 82, Templar Assassin: 97, Witch Doctor: 176, Tiny: 80 | |
| | Io: 203, Bristleback: 23, Batrider: 48, Tiny: 80, Witch Doctor: 176 | |
| 91 | Tinker: 14, Disruptor: 39, Lifestealer: 33, Slardar: 44, Clockwerk: 37 | |
| | Templar Assassin: 6, Disruptor: 39, Ogre Magi: 6, Lifestealer: 33, Slardar: 44 | |

Table 5: 3 manually picked clusters out of 15 found by k-modes on all obervations from Valve events.

| | Clusters | |
|------|---|--|
| Size | Samples | |
| 691 | Disruptor: 229, Dark Seer: 211, Lifestealer: 107, Queen of Pain: 219, Rubick: 126 | |
| 091 | Disruptor: 229, Dark Seer: 211, Gyrocopter: 64, Queen of Pain: 219, Earthshaker: | |
| | 66 | |
| 197 | Sand King: 36, Razor: 27, Shadow Demon: 73, Mirana: 69, Juggernaut: 65 | |
| | Ogre Magi: 27, Shadow Demon: 73, Sand King: 36, Mirana: 69, Luna: 29 | |
| 119 | Slark: 26, Invoker: 43, Beastmaster: 40, Rubick: 19, Winter Wyvern: 19 | |
| | Invoker: 43, Clinkz: 4, Earth Spirit: 6, Beastmaster: 40, Oracle: 15 | |

Table 6: 3 manually picked clusters out of 15 found by k-modes on all obervations from Valve events using modified dissimilarity measure.

Evolution of the Metagame

Parts of the result can be seen in tables 7 and 8. The clusters were found by ROCK from the Shanghai and Manila Majors respectively.

| Clusters | |
|----------|--|
| Size | Samples |
| 29 | Io: 21, Beastmaster: 13, Tiny: 17, Witch Doctor: 9, Queen of Pain: 3 |
| 29 | Io: 21, Dark Seer: 9, Sven: 7, Tiny: 17, Witch Doctor: 9 |
| 27 | Invoker: 6, Gyrocopter: 23, Oracle: 4, Dark Seer: 16, Rubick: 9 |
| | Invoker: 6, Gyrocopter: 23, Oracle: 4, Dark Seer: 16, Bane: 8 |
| 23 | Invoker: 14, Faceless Void: 13, Enchantress: 8, Witch Doctor: 11, Spectre: 4 |
| 23 | Earth Spirit: 5, Faceless Void: 13, Invoker: 14, Witch Doctor: 11, Ember Spirit: |
| | |

Table 7: 3 manually picked clusters out of 150 found by ROCK with a threshold of 0.6 for cluster merging on observations from the Shanghai Major.

| | Clusters | |
|------|--|--|
| Size | Samples | |
| 21 | Queen of Pain: 11, Dark Seer: 12, Lifestealer: 9, Doom: 10, Lion: 9 | |
| 21 | Earth Spirit: 6, Dark Seer: 12, Queen of Pain: 11, Lifestealer: 9, Lion: 9 | |
| 13 | Dark Seer: 5, Gyrocopter: 3, Vengeful Spirit: 13, Doom: 11, Queen of Pain: 2 | |
| | Vengeful Spirit: 13, Dark Seer: 5, Puck: 4, Doom: 11, Lifestealer: 1 | |
| 34 | Puck: 10, Juggernaut: 19, Faceless Void: 12, Enchantress: 19, Lion: 20 | |
| | Slardar: 5, Invoker: 8, Juggernaut: 19, Enchantress: 19, Lion: 20 | |

Table 8: 3 manually picked clusters out of 150 found by ROCK with a threshold of 0.6 for cluster merging on observations from the Manila Major.

Discussion

In this section I will discuss the results that were presented previously. Starting off with the association analysis followed by cluster analysis.

Association Analysis

When should I pick hero X?

As mentioned before, Anti-Mage is a mobile hero that is durable against magic damage, and examining the rules found by FP-Growth in table 1 all the heroes are either heavy magic damage dealers or excel at split pushing, i.e., be all over the map. That suggests that the rules are actually useful in finding combinations of heroes that a player should pick Anti-Mage against.

And for Clinkz, the results also make sense (table 2), since he is a physical dealer he works well against the likes of Juggernaut that is more suited against magic damage dealers. He also has the surprise factor with invisibility to easily kill vulnerable heroes such as Io.

Which hero(es) should I pick along X?

Io is a hero that have many pairings that are commonly seen in games where Io is picked. In table 3 we can see certain combinations that are common and it is clear that Tiny is one of those—it is a well known pairing in the DOTA community. We can see that it is combined with initiators such as Earthshaker, Beastmaster, and Batrider that enhances the team with what Io is lacking.

Cluster Analysis

Hero Combinations

There are certain hero combinations that standout among those that have been played in Valve events such as { Queen of Pain, Disruptor, Dark Seer } and { Io, Tiny, Witch Doctor }. Given knowledge of these heroes, it is clear that these combinations of heroes synergize well together, in particular { Io, Tiny } is a well known pairing. We also see some less common pairings such as { Invoker, Beastmaster } and { Lifestealer, Slardar } that synergize very well together.

Evolution of the Metagame

From the selected clusters it is obvious that different heroes were prioritized between the two events, check the appendix for more results. We can see that $\{$ Io, Tiny $\}$, $\{$ Gyrocopter, Dark Seer $\}$, and $\{$ Invoker, Faceless Void, Witch Doctor $\}$ were fairly common combinations of heroes at the Shanghai major while at Manila others were popular such as $\{$ Queen of Pain, Dark Seer, Lifestealer, Lion $\}$, $\{$ Doom, Vengeful Spirit $\}$, and $\{$ Lion, Juggernaut, Enchantress $\}$. From these results alone I can only speculate what that actually means in terms of gameplay, but since the events did occur fairly up close to each other I would perhaps be naive to assume a complete shift in the metagame.

Summary

Overall, it seems that association rules can find combinations of heroes that are either good together or that specific heroes are good against. The parameters can of course be tweaked further for generating even more rules that may have been missed but are useful.

Clustering do seem to find useful hero combinations and can detect differences, but it does not tell the whole story alone because DOTA 2 is more than just hero picks. The same can be said above the association rules. The choice of number of clusters was arbitrarily set based on experimenting with different values and something that is important to consider for future studies.

Conclusion

In this paper I have used data mining techniques to find patterns in the drafting phase of DOTA 2 in professional matches by looking at the team compositions. Association and cluster analysis was both used to answer different questions.

Association rules gave us some ideas as to what to pick against certain combinations of heroes and also what combinations are common with specific heroes.

To find broader patterns in the team compositions, specifically the metagame, I used cluster analysis that found common combinations of heroes and what heroes are contested in professional games at different events.

These results do however not answer the reasons behind the choices that are being made by professionals and are therefore not by themselves fully complete, but rather a step in a series of analyses.

Future Work

The full analyses may consist of searching for interesting hero combinations (similar to this paper) and then use those results to further analyze the whys in the gameplay itself to gain insight in the synergistic and counteractive nature between heroes.

To further improve the evaluation of the techniques used in the analyses is to make it possible for the community to rate it by an online interface. That way it would be possible to gain feedback from people with various degree of knowledge about the game to determine if the results are useful to the targeted demographic.

References

- [1] Fuyuan Cao, Jiye Liang, and Liang Bai. A new initialization method for categorical data clustering. *Expert Systems with Applications*, 36(7):10223–10228, 2009.
- [2] Kevin Conley and Daniel Perry. How does he saw me? a recommendation engine for picking heroes in dota 2. Np, nd Web, 7, 2013.
- [3] Michael Cook. Draft-analysis of the ancients: Predicting draft picks in dota 2 using machine learning. 2016.
- [4] Sudipto Guha, Rajeev Rastogi, and Kyuseok Shim. Rock: A robust clustering algorithm for categorical attributes. *Information systems*, 25(5):345–366, 2000.
- [5] Jiawei Han, Jian Pei, and Yiwen Yin. Mining frequent patterns without candidate generation. In *ACM Sigmod Record*, volume 29, pages 1–12. ACM, 2000.
- [6] Zhexue Huang. Extensions to the k-means algorithm for clustering large data sets with categorical values. Data mining and knowledge discovery, 2(3):283-304, 1998.

Clustering Results

In all of the tables there will be numbers becide each hero name and those correspond to the frequency of the particluar hero in the cluster.

Clustering of All Valve Events Since 2012

k-modes

| | Clusters |
|------|---|
| Size | Samples |
| 2326 | Juggernaut: 268, Timbersaw: 225, Slardar: 300, Rubick: 315, Dazzle: 296 |
| 2020 | Faceless Void: 179, Invoker: 281, Dazzle: 296, Rubick: 315, Timbersaw: 225 |
| 614 | Queen of Pain: 195, Disruptor: 193, Dark Seer: 191, Lifestealer: 93, Rubick: 122 Earthshaker: 43, Queen of Pain: 195, Gyrocopter: 61, Disruptor: 193, Dark Seer: 191 |
| 486 | Io: 203, Earthshaker: 82, Templar Assassin: 97, Witch Doctor: 176, Tiny: 80 Io: 203, Bristleback: 23, Batrider: 48, Tiny: 80, Witch Doctor: 176 |
| 462 | Slark: 102, Vengeful Spirit: 169, Earth Spirit: 128, Batrider: 131, Dragon Knight: 102 |
| | Slark: 102, Vengeful Spirit: 169, Dark Seer: 38, Earth Spirit: 128, Dragon Knight: 102 |
| 306 | Disruptor: 98, Gyrocopter: 99, Dark Seer: 169, Templar Assassin: 29, Rubick: 33 Disruptor: 98, Night Stalker: 30, Gyrocopter: 99, Dark Seer: 169, Viper: 13 |
| 398 | Juggernaut: 119, Disruptor: 103, Invoker: 84, Batrider: 140, Enchantress: 53 Juggernaut: 119, Disruptor: 103, Enchantress: 53, Batrider: 140, Beastmaster: 33 |
| 372 | Tusk: 124, Ember Spirit: 80, Lina: 82, Rubick: 110, Dragon Knight: 78 Queen of Pain: 20, Tusk: 124, Winter Wyvern: 22, Rubick: 110, Dragon Knight: 78 |
| 160 | Io: 21, Tinker: 58, Sven: 57, Rubick: 35, Clockwerk: 49 Tinker: 58, Sven: 57, Dark Seer: 12, Shadow Shaman: 6, Beastmaster: 16 |
| 172 | Templar Assassin: 47, Storm Spirit: 67, Lifestealer: 59, Batrider: 31, Rubick: 31 Lifestealer: 59, Elder Titan: 6, Batrider: 31, Rubick: 31, Templar Assassin: 47 |
| 109 | Io: 31, Juggernaut: 16, Disruptor: 22, Ember Spirit: 76, Bristleback: 21 Io: 31, Juggernaut: 16, Ember Spirit: 76, Bristleback: 21, Lion: 17 |
| 69 | Tinker: 39, Slark: 21, Dark Seer: 19, Slardar: 21, Witch Doctor: 22 Phoenix: 4, Tinker: 39, Faceless Void: 8, Witch Doctor: 22, Slark: 21 |
| 296 | Doom: 108, Queen of Pain: 64, Shadow Demon: 74, Dazzle: 85, Weaver: 49 Doom: 108, Shadow Demon: 74, Storm Spirit: 7, Dazzle: 85, Mirana: 42 |
| 91 | Tinker: 14, Disruptor: 39, Lifestealer: 33, Slardar: 44, Clockwerk: 37 Templar Assassin: 6, Disruptor: 39, Ogre Magi: 6, Lifestealer: 33, Slardar: 44 |
| 84 | Io: 8, Juggernaut: 20, Anti-Mage: 38, Dazzle: 11, Batrider: 40 Anti-Mage: 38, Ogre Magi: 8, Dazzle: 11, Magnus: 6, Batrider: 40 |
| 111 | Queen of Pain: 27, Earthshaker: 73, Luna: 21, Rubick: 18, Shadow Fiend: 48 Tusk: 7, Earthshaker: 73, Luna: 21, Rubick: 18, Shadow Fiend: 48 |

Table 9: All clusters found by k-modes on all obervations from Valve events.

k-modes with modified dissimilarity measure

| | Clusters | |
|------|---|--|
| Size | Samples | |
| 1781 | Dazzle: 282, Slardar: 301, Timbersaw: 184, Juggernaut: 208, Rubick: 376 Dazzle: 282, Templar Assassin: 56, Slardar: 301, Juggernaut: 208, Rubick: 376 | |
| 691 | Disruptor: 229, Dark Seer: 211, Lifestealer: 107, Queen of Pain: 219, Rubick: 126 Disruptor: 229, Dark Seer: 211, Gyrocopter: 64, Queen of Pain: 219, Earthshaker: 66 | |
| 519 | Earthshaker: 83, Tiny: 68, Witch Doctor: 186, Templar Assassin: 108, Io: 213 Witch Doctor: 186, Bristleback: 33, Tiny: 68, Batrider: 53, Io: 213 | |
| 465 | Vengeful Spirit: 167, Slark: 102, Earth Spirit: 121, Dragon Knight: 103, Batrider: 133 | |
| | Dark Seer: 36, Slark: 102, Earth Spirit: 121, Dragon Knight: 103, Vengeful Spirit: 167 | |
| 418 | Disruptor: 114, Enchantress: 53, Invoker: 88, Juggernaut: 123, Batrider: 141 Disruptor: 114, Enchantress: 53, Beastmaster: 34, Juggernaut: 123, Batrider: 141 | |
| 386 | Ember Spirit: 80, Tusk: 126, Lina: 80, Dragon Knight: 83, Rubick: 111 Ember Spirit: 80, Tusk: 126, Ancient Apparition: 31, Spirit Breaker: 24, Dragon Knight: 83 | |
| 283 | Dazzle: 102, Tusk: 59, Ember Spirit: 76, Gyrocopter: 82, Lina: 41 Dazzle: 102, Ember Spirit: 76, Gyrocopter: 82, Slardar: 22, Beastmaster: 25 | |
| 254 | Doom: 95, Lina: 23, Lion: 77, Juggernaut: 59, Clockwerk: 41 Doom: 95, Queen of Pain: 24, Night Stalker: 16, Lion: 77, Juggernaut: 59 | |
| 265 | Disruptor: 59, Vengeful Spirit: 75, Morphling: 47, Invoker: 84, Dark Seer: 64 Morphling: 47, Dark Seer: 64, Invoker: 84, Lion: 9, Bounty Hunter: 19 | |
| 205 | Dark Seer: 93, Templar Assassin: 31, Earthshaker: 49, Spectre: 29, Witch Doctor: 37 | |
| | Gyrocopter: 14, Dark Seer: 93, Templar Assassin: 31, Earthshaker: 49, Ancient Apparition: 7 | |
| 181 | Sven: 34, Storm Spirit: 51, Slardar: 47, Shadow Demon: 53, Bounty Hunter: 28 Storm Spirit: 51, Axe: 14, Shadow Demon: 53, Sand King: 15, Luna: 9 | |
| 197 | Sand King: 36, Razor: 27, Shadow Demon: 73, Mirana: 69, Juggernaut: 65 Ogre Magi: 27, Shadow Demon: 73, Sand King: 36, Mirana: 69, Luna: 29 | |
| 162 | Timbersaw: 33, Shadow Demon: 46, Sand King: 42, Mirana: 73, Shadow Fiend: 26 Naga Siren: 16, Mirana: 73, Shadow Demon: 46, Sand King: 42, Juggernaut: 5 | |
| 130 | Vengeful Spirit: 49, Night Stalker: 19, Gyrocopter: 34, Alchemist: 31, Batrider: 26 Doom: 4, Vengeful Spirit: 49, Gyrocopter: 34, Shadow Fiend: 5, Batrider: 26 | |
| 119 | Slark: 26, Invoker: 43, Beastmaster: 40, Rubick: 19, Winter Wyvern: 19 Invoker: 43, Clinkz: 4, Earth Spirit: 6, Beastmaster: 40, Oracle: 15 | |

 $\textbf{Table 10:} \ \, \textbf{All clusters found by} \ \, \textit{k-modes on all observations from Valve events using modified dissimilarity measure.}$

Clustering of Shanghai Major 2016

k-modes

| | Clusters |
|------|--|
| Size | Samples |
| | Vengeful Spirit: 37, Witch Doctor: 57, Juggernaut: 12, Invoker: 40, Nature's Prophet: 30 |
| | Witch Doctor: 57, Batrider: 20, Lone Druid: 26, Earth Spirit: 28, Death Prophet: 23 |
| 221 | Witch Doctor: 57, Faceless Void: 14, Ember Spirit: 14, Earth Spirit: 28, Invoker: 40 |
| | Spirit Breaker: 18, Bounty Hunter: 15, Witch Doctor: 57, Invoker: 40, Death Prophet: 23 |
| | Faceless Void: 14, Witch Doctor: 57, Spectre: 10, Invoker: 40, Enchantress: 26 Sven: 14, Io: 23, Witch Doctor: 57, Tiny: 17, Dark Seer: 31 |
| | Vengeful Spirit: 37, Bristleback: 7, Witch Doctor: 57, Spectre: 10, Nature's Prophet: 30 |
| | Spirit Breaker: 18, Doom: 7, Witch Doctor: 57, Outworld Devourer: 18, Invoker: 40 |
| | Juggernaut: 12, Slardar: 8, Bane: 19, Tusk: 34, Invoker: 24 |
| 76 | Ancient Apparition: 6, Ember Spirit: 7, Tusk: 34, Invoker: 24, Dark Seer: 13 Legion Commander: 1, Beastmaster: 7, Tusk: 34, Invoker: 24, Gyrocopter: 13 |
| 76 | Vengeful Spirit: 38, Disruptor: 20, Drow Ranger: 6, Gyrocopter: 31, Nyx Assassin: 13 |
| | Vengeful Spirit: 38, Disruptor: 20, Drow Ranger: 6, Gyrocopter: 31, Nature's Prophet: 7 |
| | Vengeful Spirit: 38, Disruptor: 20, Gyrocopter: 31, Sand King: 1, Queen of Pain: 8 |
| 44 | Sven: 13, Vengeful Spirit: 25, Slardar: 4, Chen: 14, Invoker: 10 Sven: 13, Dark Seer: 7, Batrider: 6, Doom: 2, Vengeful Spirit: 25 |
| 40 | Spirit Breaker: 12, Dragon Knight: 2, Gyrocopter: 21, Oracle: 13, Zeus: 6 Spirit Breaker: 12, Abaddon: 4, Puck: 1, Gyrocopter: 21, Oracle: 13 |
| 40 | Lion: 20, Ember Spirit: 8, Beastmaster: 15, Clinkz: 3, Nature's Prophet: 15 Lion: 20, Ursa: 4, Beastmaster: 15, Razor: 1, Nature's Prophet: 15 |
| 38 | Puck: 10, Faceless Void: 27, Witch Doctor: 10, Gyrocopter: 19, Pudge: 1 Faceless Void: 27, Witch Doctor: 10, Gyrocopter: 19, Templar Assassin: 3, En- |
| | chantress: 8 Juggernaut: 11, Disruptor: 6, Tusk: 9, Invoker: 10, Nature's Prophet: 11 |
| 23 | Death Prophet: 3, Witch Doctor: 4, Tusk: 9, Juggernaut: 11, Nature's Prophet: 11 |
| 0.0 | Juggernaut: 10, Chen: 4, Tusk: 15, Invoker: 9, Tidehunter: 6 |
| 23 | Lion: 1, Juggernaut: 10, Tusk: 15, Invoker: 9, Tidehunter: 6 |
| 17 | Batrider: 5, Bane: 13, Terrorblade: 1, Invoker: 8, Chen: 5 Doom: 2, Bane: 13, Juggernaut: 3, Invoker: 8, Chen: 5 |

 $\textbf{Table 11:} \ \ \textbf{All clusters found by} \ \textit{k-modes on all obervations from the Shanghai Major}.$

k-modes with modified dissimilarity measure

| | Clusters | |
|------|---|--|
| Size | Samples | |
| | Vengeful Spirit: 42, Witch Doctor: 54, Nature's Prophet: 33, Invoker: 66, Juggernaut: 28 Death Prophet: 22, Spirit Breaker: 17, Witch Doctor: 54, Invoker: 66, Bounty | |
| 205 | Hunter: 13 Vengeful Spirit: 42, Slark: 12, Nature's Prophet: 33, Invoker: 66, Disruptor: 18 Tusk: 22, Juggernaut: 28, Nature's Prophet: 33, Invoker: 66, Disruptor: 18 Faceless Void: 21, Witch Doctor: 54, Invoker: 66, Enchantress: 17, Spectre: 6 Vengeful Spirit: 42, Pugna: 4, Nature's Prophet: 33, Invoker: 66, Dazzle: 19 Spirit Breaker: 17, Dazzle: 19, Nature's Prophet: 33, Invoker: 66, Juggernaut: 28 | |
| | Oracle: 13, Faceless Void: 21, Witch Doctor: 54, Invoker: 66, Viper: 8 | |
| 94 | Bane: 22, Juggernaut: 16, Slardar: 9, Tusk: 42, Invoker: 34 Ancient Apparition: 6, Ember Spirit: 8, Tusk: 42, Dark Seer: 16, Invoker: 34 Gyrocopter: 17, Treant Protector: 2, Nature's Prophet: 10, Invoker: 34, Tusk: 42 Beastmaster: 8, Legion Commander: 1, Tusk: 42, Gyrocopter: 17, Invoker: 34 | |
| | Drow Ranger: 6, Vengeful Spirit: 40, Disruptor: 20, Nyx Assassin: 14, Gyrocopter: | |
| 82 | Drow Ranger: 6, Vengeful Spirit: 40, Disruptor: 20, Nature's Prophet: 8, Gyro- | |
| | copter: 35 Undying: 9, Vengeful Spirit: 40, Nature's Prophet: 8, Zeus: 13, Gyrocopter: 35 Sand King: 1, Vengeful Spirit: 40, Queen of Pain: 8, Disruptor: 20, Gyrocopter: 35 | |
| 48 | Clinkz: 3, Beastmaster: 17, Ember Spirit: 9, Nature's Prophet: 17, Lion: 21 Ursa: 4, Beastmaster: 17, Nature's Prophet: 17, Lion: 21, Razor: 1 | |
| 45 | Medusa: 6, Faceless Void: 23, Witch Doctor: 9, Zeus: 11, Vengeful Spirit: 15 Death Prophet: 9, Faceless Void: 23, Witch Doctor: 9, Enchantress: 9, Outworld Devourer: 8 | |
| 32 | Earthshaker: 4, Dazzle: 4, Lone Druid: 10, Earth Spirit: 17, Anti-Mage: 8 Ursa: 4, Crystal Maiden: 6, Lone Druid: 10, Death Prophet: 3, Earth Spirit: 17 | |
| 33 | Oracle: 12, Gyrocopter: 18, Dragon Knight: 5, Zeus: 3, Spirit Breaker: 11 Oracle: 12, Gyrocopter: 18, Puck: 1, Abaddon: 5, Spirit Breaker: 11 | |
| 19 | Beastmaster: 5, Tiny: 8, Io: 15, Enchantress: 4, Batrider: 4 Tiny: 8, Nature's Prophet: 1, Io: 15, Lich: 1, Beastmaster: 5 | |
| 23 | Witch Doctor: 11, Spectre: 5, Juggernaut: 4, Enchantress: 9, Disruptor: 5 Treant Protector: 1, Witch Doctor: 11, Zeus: 2, Enchantress: 9, Sven: 4 | |
| 17 | Chen: 6, Skywrath Mage: 2, Tusk: 6, Spectre: 3, Zeus: 6 Earthshaker: 2, Chen: 6, Outworld Devourer: 4, Tusk: 6, Queen of Pain: 3 | |

 $\textbf{Table 12:} \ \, \textbf{All clusters found by } \textit{k-modes on all observations from the Shanghai Major using modified dissimilarity measure.}$

ROCK

| | Clusters |
|------|--|
| Size | Samples |
| 11 | Death Prophet: 5, Earth Spirit: 4, Dark Seer: 4, Juggernaut: 5, Oracle: 7 Earth Spirit: 4, Juggernaut: 5, Oracle: 7, Nature's Prophet: 5, Outworld Devourer: 3 |
| 11 | Undying: 5, Gyrocopter: 3, Vengeful Spirit: 11, Zeus: 6, Nature's Prophet: 7 Ember Spirit: 4, Vengeful Spirit: 11, Undying: 5, Nature's Prophet: 7, Ursa: 1 |
| 29 | Io: 21, Beastmaster: 13, Tiny: 17, Witch Doctor: 9, Queen of Pain: 3 Io: 21, Dark Seer: 9, Sven: 7, Tiny: 17, Witch Doctor: 9 |
| 27 | Invoker: 6, Gyrocopter: 23, Oracle: 4, Dark Seer: 16, Rubick: 9 Invoker: 6, Gyrocopter: 23, Oracle: 4, Dark Seer: 16, Bane: 8 |
| 22 | Tidehunter: 5, Chen: 12, Juggernaut: 13, Invoker: 8, Tusk: 12 Chen: 12, Juggernaut: 13, Invoker: 8, Earthshaker: 5, Disruptor: 9 |
| 29 | Invoker: 19, Slark: 5, Vengeful Spirit: 20, Disruptor: 7, Nature's Prophet: 11 Vengeful Spirit: 20, Drow Ranger: 8, Invoker: 19, Nature's Prophet: 11, Viper: 2 |
| 16 | Death Prophet: 7, Juggernaut: 7, Witch Doctor: 14, Nature's Prophet: 7, Tusk: 5 |
| | Death Prophet: 7, Slardar: 1, Juggernaut: 7, Witch Doctor: 14, Tusk: 5 |
| 23 | Invoker: 14, Faceless Void: 13, Enchantress: 8, Witch Doctor: 11, Spectre: 4 Earth Spirit: 5, Faceless Void: 13, Invoker: 14, Witch Doctor: 11, Ember Spirit: 2 |
| 15 | Batrider: 3, Zeus: 8, Faceless Void: 8, Witch Doctor: 9, Gyrocopter: 5 Zeus: 8, Faceless Void: 8, Vengeful Spirit: 3, Witch Doctor: 9, Medusa: 3 |
| 13 | Morphling: 7, Vengeful Spirit: 5, Dark Seer: 9, Invoker: 2, Disruptor: 5 Morphling: 7, Dark Seer: 9, Tiny: 4, Disruptor: 5, Bane: 3 |
| 11 | Death Prophet: 6, Lone Druid: 4, Vengeful Spirit: 9, Tusk: 6, Dazzle: 4 Death Prophet: 6, Chen: 5, Wraith King: 1, Vengeful Spirit: 9, Tusk: 6 |
| 14 | Zeus: 8, Chen: 4, Gyrocopter: 11, Dragon Knight: 2, Tusk: 8 Zeus: 8, Juggernaut: 1, Oracle: 4, Tusk: 8, Gyrocopter: 11 |
| 11 | Vengeful Spirit: 6, Clinkz: 5, Enigma: 6, Invoker: 3, Tidehunter: 9 Tidehunter: 9, Razor: 3, Vengeful Spirit: 6, Clinkz: 5, Lion: 6 |
| 11 | Night Stalker: 3, Invoker: 5, Ember Spirit: 8, Nature's Prophet: 7, Lion: 4 Ember Spirit: 8, Outworld Devourer: 1, Witch Doctor: 4, Nature's Prophet: 7, Lion: 4 |
| 10 | Earth Spirit: 5, Beastmaster: 5, Invoker: 6, Slark: 3, Lion: 4 Ancient Apparition: 5, Earth Spirit: 5, Dark Seer: 2, Invoker: 6, Slark: 3 |
| 19 | Phoenix: 7, Gyrocopter: 8, Faceless Void: 4, Invoker: 6, Tusk: 16 Gyrocopter: 8, Enchantress: 4, Tusk: 16, Nature's Prophet: 6, Viper: 4 |
| 10 | Juggernaut: 5, Razor: 5, Night Stalker: 8, Vengeful Spirit: 3, Disruptor: 3 Ancient Apparition: 2, Juggernaut: 5, Razor: 5, Night Stalker: 8, Clockwerk: 4 |
| 11 | Earth Spirit: 3, Batrider: 8, Zeus: 5, Anti-Mage: 6, Undying: 3 Batrider: 8, Slark: 3, Vengeful Spirit: 5, Zeus: 5, Undying: 3 |
| 16 | Faceless Void: 5, Enigma: 2, Vengeful Spirit: 10, Drow Ranger: 6, Outworld Devourer: 10 |
| | Vengeful Spirit: 10, Outworld Devourer: 10, Enchantress: 4, Ember Spirit: 3, Mirana: 5 |

 $\textbf{Table 13:} \ \, \textbf{All clusters with a size of at least 10 found by ROCK with a threshold of 0.6 for cluster merging on observations from the Shanghai Major}$

Clustering of Manila Major 2016

k-modes

| | Clusters | | |
|------|---|--|--|
| Size | Samples | | |
| 234 | Lion: 60, Dragon Knight: 37, Wraith King: 4, Doom: 52, Batrider: 51 Nature's Prophet: 30, Lion: 60, Batrider: 51, Juggernaut: 27, Enchantress: 27 Lion: 60, Dragon Knight: 37, Nature's Prophet: 30, Doom: 52, Axe: 10 Lion: 60, Alchemist: 18, Io: 31, Doom: 52, Juggernaut: 27 Lion: 60, Dragon Knight: 37, Earth Spirit: 32, Slark: 33, Dark Seer: 24 Lion: 60, Dark Seer: 24, Dragon Knight: 37, Phoenix: 29, Slark: 33 Lion: 60, Dragon Knight: 37, Doom: 52, Lich: 17, Lifestealer: 14 Lion: 60, Dragon Knight: 37, Doom: 52, Tidehunter: 12, Spectre: 14 Lion: 60, Dragon Knight: 37, Juggernaut: 27, Slardar: 24, Enchantress: 27 Lion: 60, Queen of Pain: 18, Doom: 52, Spectre: 14, Nature's Prophet: 30 Dragon Knight: 37, Witch Doctor: 22, Doom: 52, Slark: 33, Nature's Prophet: 30 | | |
| 111 | Vengeful Spirit: 41, Beastmaster: 62, Clinkz: 10, Slardar: 33, Queen of Pain: 15 Vengeful Spirit: 41, Beastmaster: 62, Earth Spirit: 16, Slardar: 33, Morphling: 2 Vengeful Spirit: 41, Beastmaster: 62, Lone Druid: 4, Lich: 7, Slardar: 33 Lion: 17, Vengeful Spirit: 41, Beastmaster: 62, Lycan: 7, Invoker: 12 Vengeful Spirit: 41, Beastmaster: 62, Witch Doctor: 18, Juggernaut: 13, Viper: 3 | | |
| 45 | Witch Doctor: 31, Windranger: 10, Doom: 10, Phoenix: 10, Slardar: 13 Witch Doctor: 31, Storm Spirit: 1, Doom: 10, Phoenix: 10, Slardar: 13 | | |
| 52 | Witch Doctor: 27, Axe: 13, Doom: 21, Lifestealer: 16, Queen of Pain: 12 Witch Doctor: 27, Puck: 10, Doom: 21, Lifestealer: 16, Nature's Prophet: 8 | | |
| 60 | Disruptor: 27, Ember Spirit: 4, Lifestealer: 14, Slardar: 9, Bounty Hunter: 25 Broodmother: 1, Disruptor: 27, Puck: 7, Lifestealer: 14, Bounty Hunter: 25 Disruptor: 27, Gyrocopter: 3, Tidehunter: 10, Invoker: 6, Bounty Hunter: 25 | | |
| 39 | Vengeful Spirit: 23, Ember Spirit: 11, Doom: 9, Invoker: 12, Dark Seer: 9 Vengeful Spirit: 23, Ember Spirit: 11, Tidehunter: 6, Invoker: 12, Chen: 2 | | |
| 27 | Dragon Knight: 8, Disruptor: 17, Doom: 13, Tidehunter: 9, Gyrocopter: 9 Disruptor: 17, Death Prophet: 1, Doom: 13, Gyrocopter: 9, Tidehunter: 9 | | |
| 20 | Sven: 6, Alchemist: 8, Disruptor: 8, Beastmaster: 9, Earth Spirit: 9 Alchemist: 8, Beastmaster: 9, Earth Spirit: 9, Lifestealer: 5, Lich: 3 | | |
| 27 | Lion: 16, Night Stalker: 8, Juggernaut: 8, Invoker: 4, Enchantress: 6 Lion: 16, Dark Seer: 11, Puck: 6, Lifestealer: 4, Tusk: 3 | | |
| 27 | Lion: 6, Invoker: 7, Slardar: 16, Juggernaut: 3, Enchantress: 7 Mirana: 9, Earth Spirit: 3, Witch Doctor: 4, Slardar: 16, Enchantress: 7 | | |

 $\textbf{Table 14:} \ \, \textbf{All clusters found by} \ \, \textit{k-modes on all observations from the Manila Major}. \\$

k-modes with modified dissimilarity measure

| | Clusters | | |
|------|---|--|--|
| Size | Samples | | |
| | Dragon Knight: 48, Wraith King: 4, Doom: 103, Lion: 50, Batrider: 49 | | |
| | Dragon Knight: 48, Doom: 103, Lich: 19, Lion: 50, Lifestealer: 23 | | |
| | Dragon Knight: 48, Doom: 103, Nature's Prophet: 26, Lion: 50, Axe: 16 | | |
| | Dragon Knight: 48, Doom: 103, Lion: 50, Tidehunter: 14, Spectre: 14 | | |
| | Dragon Knight: 48, Nature's Prophet: 26, Doom: 103, Witch Doctor: 26, Slark: | | |
| 234 | 17 | | |
| | Queen of Pain: 21, Doom: 103, Lion: 50, Dark Seer: 21, Lifestealer: 23 | | |
| | Lion: 50, Juggernaut: 25, Doom: 103, Io: 24, Alchemist: 13 | | |
| | Dragon Knight: 48, Queen of Pain: 21, Doom: 103, Crystal Maiden: 15, Phoenix: | | |
| | 28 | | |
| | Queen of Pain: 21, Doom: 103, Nature's Prophet: 26, Lion: 50, Spectre: 14 | | |
| | Dragon Knight: 48, Lich: 19, Doom: 103, Witch Doctor: 26, Slark: 17 | | |
| | Dragon Knight: 48, Doom: 103, Lion: 50, Weaver: 5, Abaddon: 6 | | |
| | Clinkz: 9, Beastmaster: 71, Queen of Pain: 15, Vengeful Spirit: 39, Slardar: 33 | | |
| 110 | Earth Spirit: 16, Slardar: 33, Morphling: 2, Vengeful Spirit: 39, Beastmaster: 71 | | |
| 118 | Slardar: 33, Beastmaster: 71, Lone Druid: 4, Lich: 7, Vengeful Spirit: 39 Beastmaster: 71, Lycan: 6, Lion: 18, Vengeful Spirit: 39, Invoker: 14 | | |
| | Beastmaster: 71, Eyean. 6, Elon. 18, Vengerul Spirit. 39, Invoker. 14 Beastmaster: 71, Witch Doctor: 20, Juggernaut: 13, Viper: 3, Vengeful Spirit: 39 | | |
| | Slardar: 48, Witch Doctor: 40, Batrider: 16, Lifestealer: 12, Vengeful Spirit: 18 | | |
| | Slardar: 48, Witch Doctor: 40, Earth Spirit: 11, Invoker: 13, Gyrocopter: 10 | | |
| 88 | Slardar: 48, Witch Doctor: 40, Lich: 5, Ember Spirit: 13, Batrider: 16 | | |
| | Slardar: 48, Witch Doctor: 40, Earth Spirit: 11, Invoker: 13, Sven: 6 | | |
| | Earthshaker: 5, Puck: 15, Slark: 13, Enchantress: 27, Disruptor: 25 | | |
| 57 | Faceless Void: 11, Disruptor: 25, Chaos Knight: 1, Enchantress: 27, Puck: 15 | | |
| 6.0 | Alchemist: 4, Queen of Pain: 9, Lifestealer: 9, Lion: 6, Bounty Hunter: 21 | | |
| 36 | Lifestealer: 9, Queen of Pain: 9, Witch Doctor: 8, Broodmother: 1, Bounty | | |
| | Hunter: 21 | | |
| 32 | Death Prophet: 10, Slardar: 5, Slark: 9, Earth Spirit: 13, Disruptor: 6 | | |
| | Dragon Knight: 4, Slark: 9, Earth Spirit: 13, Lion: 5, Dark Seer: 5 | | |
| 24 | Bounty Hunter: 2, Ember Spirit: 7, Lion: 14, Dark Seer: 13, Spectre: 5 | | |
| | Dark Seer: 13, Invoker: 5, Lion: 14, Winter Wyvern: 1, Lifestealer: 7 | | |
| 20 | Medusa: 5, Puck: 7, Witch Doctor: 7, Nature's Prophet: 5, Vengeful Spirit: 6 | | |
| | Medusa: 5, Beastmaster: 7, Witch Doctor: 7, Phoenix: 4, Puck: 7 | | |
| 22 | Night Stalker: 5, Medusa: 1, Lion: 12, Dark Seer: 5, Invoker: 7 | | |
| | Juggernaut: 3, Queen of Pain: 1, Night Stalker: 5, Lion: 12, Phoenix: 6 | | |
| 11 | Bane: 2, Faceless Void: 2, Enigma: 3, Invoker: 2, Phantom Lancer: 4 | | |
| | Bane: 2, Slardar: 1, Enigma: 3, Io: 4, Alchemist: 3 | | |

 $\textbf{Table 15:} \ \, \textbf{All clusters found by } \textit{k-modes on all observations from the Manila Major using modified dissimilarity measure.}$

\mathbf{ROCK}

| | Clusters |
|------|--|
| Size | Samples |
| 21 | Queen of Pain: 11, Dark Seer: 12, Lifestealer: 9, Doom: 10, Lion: 9 Earth Spirit: 6, Dark Seer: 12, Queen of Pain: 11, Lifestealer: 9, Lion: 9 |
| 16 | Lifestealer: 6, Lich: 4, Doom: 13, Dragon Knight: 7, Lion: 9 Spectre: 1, Tidehunter: 3, Doom: 13, Dragon Knight: 7, Lion: 9 |
| 13 | Dark Seer: 5, Gyrocopter: 3, Vengeful Spirit: 13, Doom: 11, Queen of Pain: 2 Vengeful Spirit: 13, Dark Seer: 5, Puck: 4, Doom: 11, Lifestealer: 1 |
| 12 | Batrider: 10, Slark: 2, Puck: 6, Doom: 4, Crystal Maiden: 6 Morphling: 2, Batrider: 10, Puck: 6, Doom: 4, Crystal Maiden: 6 |
| 13 | Tidehunter: 6, Mirana: 6, Doom: 10, Disruptor: 12, Queen of Pain: 1 Slardar: 2, Disruptor: 12, Doom: 10, Mirana: 6, Gyrocopter: 4 |
| 12 | Beastmaster: 8, Juggernaut: 8, Vengeful Spirit: 7, Mirana: 5, Enigma: 2 Earth Spirit: 4, Beastmaster: 8, Vengeful Spirit: 7, Invoker: 3, Juggernaut: 8 |
| 20 | Slardar: 6, Puck: 10, Witch Doctor: 17, Nature's Prophet: 7, Lifestealer: 10 Lifestealer: 10, Puck: 10, Doom: 5, Nature's Prophet: 7, Witch Doctor: 17 |
| 11 | Slardar: 10, Dark Seer: 6, Doom: 4, Templar Assassin: 5, Witch Doctor: 6 Slardar: 10, Dark Seer: 6, Witch Doctor: 6, Templar Assassin: 5, Bane: 1 |
| 16 | Earth Spirit: 9, Dark Seer: 16, Slark: 5, Dragon Knight: 5, Lion: 10 Earth Spirit: 9, Dark Seer: 16, Invoker: 2, Spectre: 6, Lion: 10 |
| 23 | Slardar: 20, Earth Spirit: 6, Gyrocopter: 6, Invoker: 7, Witch Doctor: 19 Slardar: 20, Earth Spirit: 6, Sven: 5, Invoker: 7, Witch Doctor: 19 |
| 11 | Slardar: 9, Morphling: 1, Beastmaster: 8, Vengeful Spirit: 9, Earth Spirit: 6 Slardar: 9, Beastmaster: 8, Vengeful Spirit: 9, Clinkz: 1, Queen of Pain: 3 |
| 10 | Slardar: 7, Phoenix: 3, Dragon Knight: 9, Disruptor: 4, Lifestealer: 4 Slardar: 7, Phoenix: 3, Vengeful Spirit: 5, Dragon Knight: 9, Lone Druid: 1 |
| 12 | Dazzle: 10, Tidehunter: 5, Lycan: 5, Invoker: 4, Earth Spirit: 7 Dazzle: 10, Earth Spirit: 7, Batrider: 4, Lycan: 5, Timbersaw: 2 |
| 15 | Slardar: 8, Morphling: 5, Beastmaster: 5, Lion: 12, Lich: 6 Morphling: 5, Beastmaster: 5, Elder Titan: 4, Mirana: 7, Lion: 12 |
| 12 | Puck: 4, Beastmaster: 9, Lifestealer: 7, Enchantress: 4, Lion: 8 Beastmaster: 9, Lion: 8, Tinker: 4, Disruptor: 3, Lifestealer: 7 |
| 34 | Puck: 10, Juggernaut: 19, Faceless Void: 12, Enchantress: 19, Lion: 20 Slardar: 5, Invoker: 8, Juggernaut: 19, Enchantress: 19, Lion: 20 |

 $\textbf{Table 16:} \ \, \textbf{All clusters with a size of at least 10 found by ROCK with a threshold of 0.6 for cluster merging on observations from the Manila Major}$