# 732A62 Lab 1

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## Assignment 1

**a**)

```
set.seed(12345)
t1 \leftarrow c(0, 0, rnorm(100, 0, 1))
ts1 \leftarrow filter(t1, filter = c(0, -0.8),
               method = "recursive", sides = 1)
t2 <- 1:100
ts2 < -cos(2 * pi * t2 / 5)
vt1 <- filter(ts1, filter = c(rep(0.2, times = 5)),
               method = "convolution", sides = 1)
vt2 <- filter(ts2, filter = c(rep(0.2, times = 5)),
               method = "convolution", sides = 1)
                        ts1
                                                                        ts2
               20
                     40
                           60
                                 80
                                       100
                                                          0
                                                               20
                                                                      40
                                                                            60
                                                                                  80
                                                                                        100
                                                                        Time
                       Time
                 Smoothed ts1
                                                                  Smoothed ts2
¥
                                                     -1.0
     4
          0
               20
                     40
                           60
                                 80
                                       100
                                                          0
                                                               20
                                                                      40
                                                                            60
                                                                                  80
                                                                                        100
```

Time series 1 (ts1) show no noticeable change in its random pattern except the scale which is transformed in to a smaller scale. Time series 2 (ts2) is flattened by the smoothing filter and all values are now basically

Time

Time

0. This is because the average of ts2 lies around zero it is also reasonable to expect that a moving average smoother would generate the same (or similar) result.

#### b)

```
leftside <- c(1, -4, 2, 0, 0, 1) # the x's
rightside <- c(1, 0, 3, 0, 1, 0, -4) # The w's

causal <- polyroot(leftside) #Not causal
invertible <- polyroot(rightside) #Non invertible

complex_dist <- function(x) {
    sqrt(Re(x)^2 + Im(x)^2)
}

print("The causal")

## [1] "The causal"

sapply(causal, complex_dist)

## [1] 0.2936658 1.6793817 1.00000000 1.4239626 1.4239626

print("The invertible")

## [1] "The invertible"

sapply(invertible, complex_dist)</pre>
```

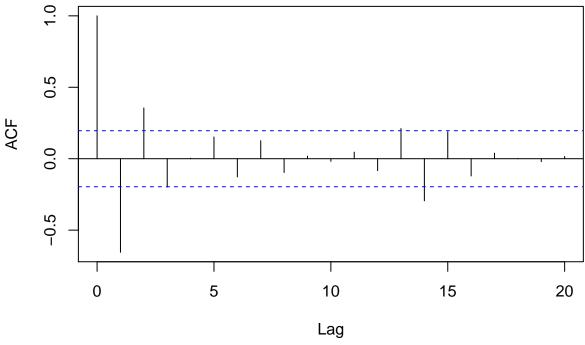
**##** [1] 0.6874372 0.6874372 0.6874372 0.6874372 1.0580446 1.0580446

Since both parts contains values below 1 they are inside the unit circle and the time series is therefore not causal nor invertible.

#### **c**)

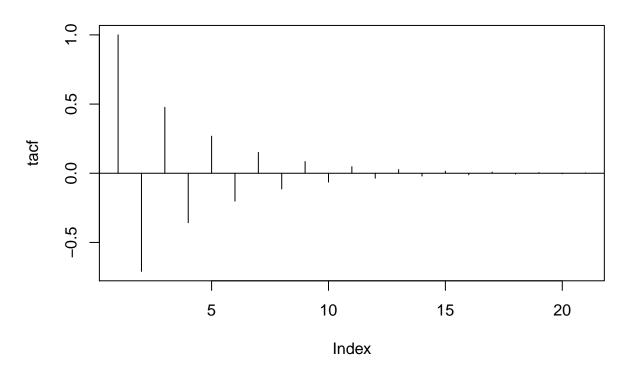
```
set.seed(12345)
model1c <- arima.sim(n = 100, list(ar = c(-3 / 4), ma = c(0, -1 / 9)))
acf(model1c)</pre>
```

## Series model1c



```
tacf <- ARMAacf(ar=c(-3 / 4), ma=c(0, -1/9), lag.max=20)
plot(tacf, type="n", main="Theoretical")
segments(1:length(tacf), rep(0, length(tacf)), 1:length(tacf), tacf)
abline(h=0)</pre>
```

### **Theoretical**



The ACF in the first plot shows a high correlation between all the lags except lag 11 and lag 12. Lag 2 has a larger correlation with the initial observation than the other lags. There seems to be no tendencies of the correlation dying down as the lags increases.

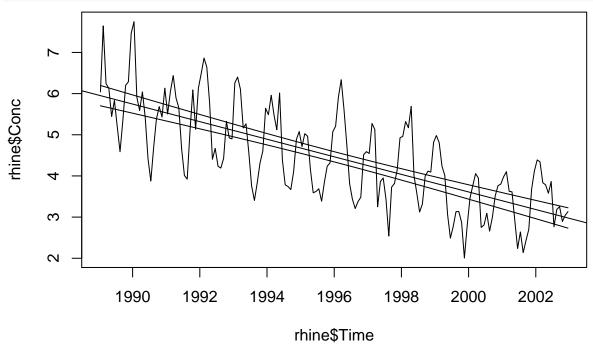
In the theoretical ACF it seems to indicate that the correlation should be dying down in a positive to negative correlations between the lags. This would indicate that the ARMA we fitted is apart from what is expected from the theoretical and therefore not appropriate for the data.

# Assignment 2

**a**)

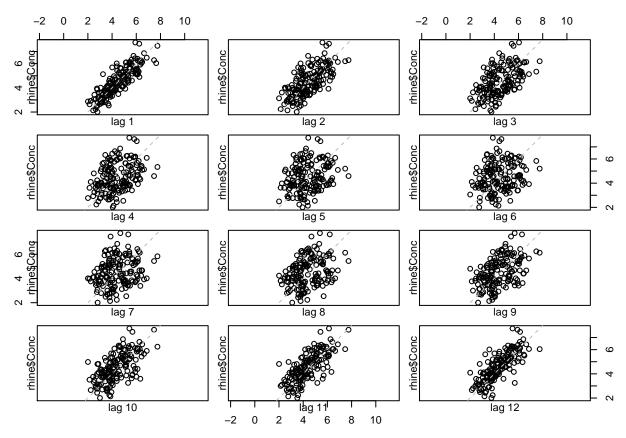
```
rhine <- read.csv2("../data/Rhine.csv")
colnames(rhine)[4] <- "Conc"

lmobj <- lm(Conc ~ Time, data = rhine)
predobj <- predict(lmobj, se.fit = TRUE)</pre>
```



In the first plot there seems a monthly variation over all years with a linear decreasing trend with what could be considered a constant variance. It could be debated that it might be a lower variance in the end series.

```
lag.plot(rhine$Conc, lags = 12)
```



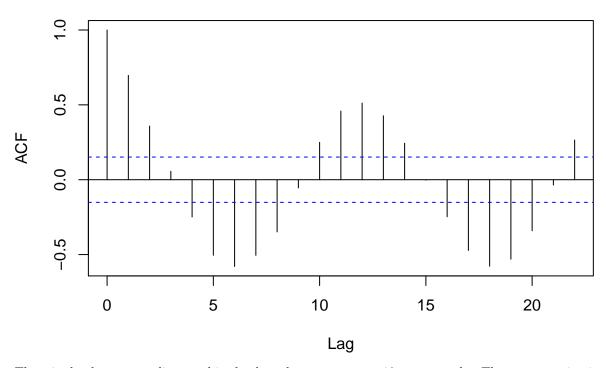
There seems to be a strong correlation between lags 1,11, and 12 and the original variable. A seasonal trend with a clear winter and summer period seems to be present.

### b)

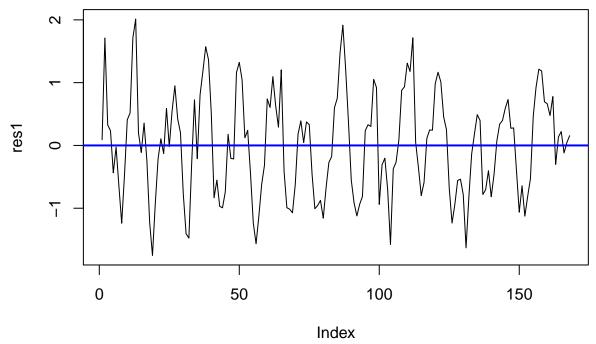
```
res1 <- residuals(lmobj)</pre>
summary(lmobj)
##
## Call:
## lm(formula = Conc ~ Time, data = rhine)
##
##
  Residuals:
##
        Min
                                     3Q
                                             Max
   -1.75325 -0.65296 0.06071 0.52453
##
                                         2.01276
##
## Coefficients:
##
                Estimate Std. Error t value Pr(>|t|)
   (Intercept) 430.70725
                            31.26570
##
                                       13.78
                                               <2e-16 ***
## Time
                -0.21355
                             0.01566
                                      -13.63
                                               <2e-16 ***
##
## Signif. codes:
                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.8205 on 166 degrees of freedom
## Multiple R-squared: 0.5282, Adjusted R-squared: 0.5254
## F-statistic: 185.9 on 1 and 166 DF, p-value: < 2.2e-16
```

We can see from the linear fit that the concentration is reduced over time which is statistical significant.

### Series res1



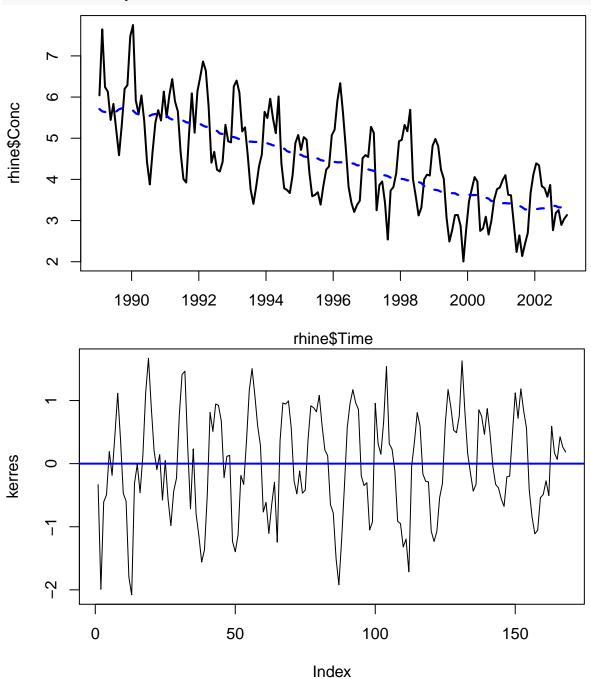
There is clearly a seasonality trend in the data that repeat every 12 or so months. The concentration increases during the winter months and decreases during the summer months.



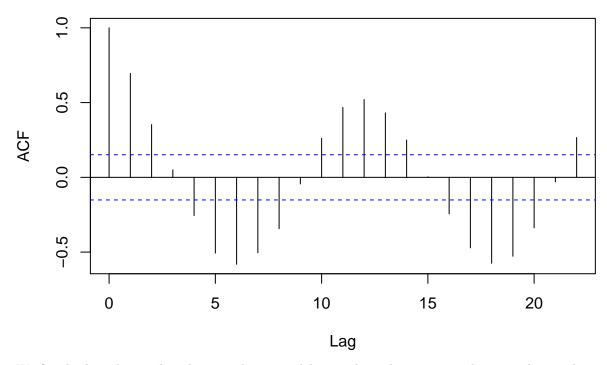
The same trend can be seen in the residuals.

 $\mathbf{c})$ 

```
kersmo <- ksmooth(y = rhine$Conc, x = rhine$Time, bandwidth = 5)
kerres <- kersmo$y - rhine$Conc</pre>
```



## Series kerres



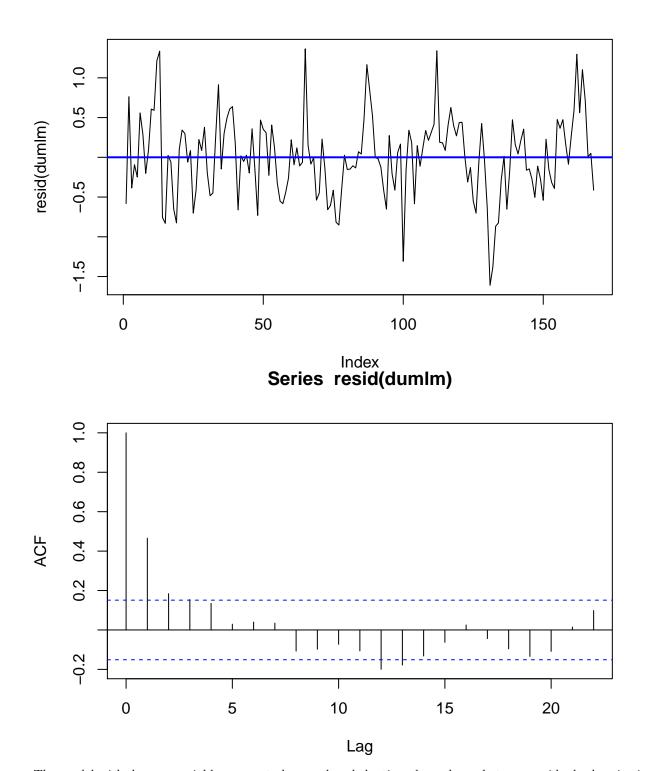
We fitted a kernel smoother close to a linear model since the task given is to eliminate the trend, as seen in the first plot the fit seems to follow the general trend nicely.

For the Residual-plot the values seems to be around 0 but with a very high time dependence between the residuals which isn't that big of suprise seeing how the model is fitted straight through the fluctuations between winters and summers.

The AFC comfirms what has been seen in the previous plots, a strong seasonal pattern presents it self in the correlations between the lags.

d)

```
rhine$Month.f <- as.factor(rhine$Month)
dumlm <- lm(Conc ~ Time + Month.f, rhine)</pre>
```



The model with dummy-variables seems to have reduced the time-dependency between residuals close in time and varies around zero.

Judging from the AFC we come to a similar conclusion where most of the correlation between lags have dissapeard, some correlation seem to remain in the second lag.

**e**)

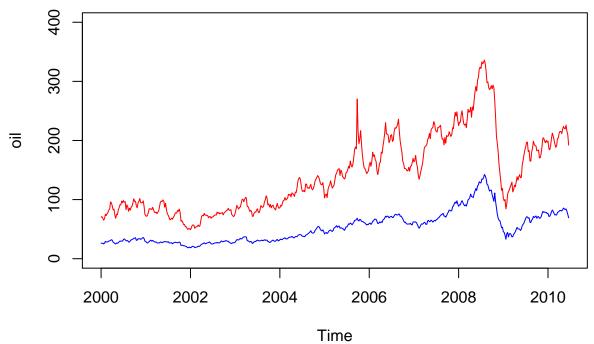
#### library(MASS) ## Warning: package 'MASS' was built under R version 3.3.2 stepAIC(dumlm, direction = "backward", steps = 1000) ## Start: AIC=-202.02 ## Conc ~ Time + Month.f ## ## Df Sum of Sq RSS AIC ## <none> 43.237 -202.023 ## - Month.f 11 68.524 111.761 -64.477 ## - Time 1 118.387 161.624 17.499 ## ## Call: ## lm(formula = Conc ~ Time + Month.f, data = rhine) ## ## Coefficients: ## (Intercept) Time Month.f2 Month.f3 Month.f4 420.82746 0.27659 0.04006 -0.34643 ## -0.20824 Month.f6 Month.f9 ## Month.f5 Month.f7 Month.f8 -0.86165 -1.26114 -1.71242 -1.23669 ## -1.60808 ## Month.f10 Month.f11 Month.f12 ## -0.87446 -0.75127 -0.17745

The backward-elimination procedure ends up with the full model with all dummy variables as the optimal model.

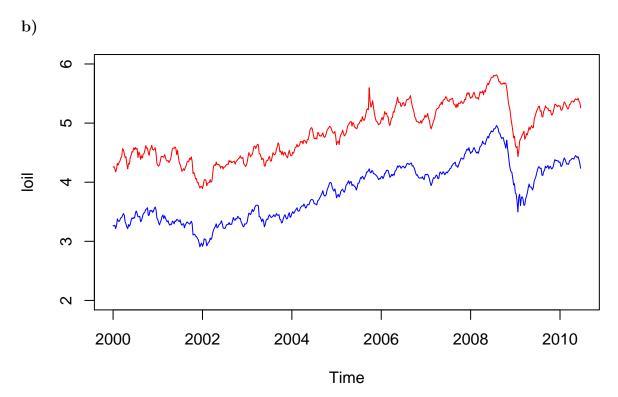
# Assignment 3

**a**)

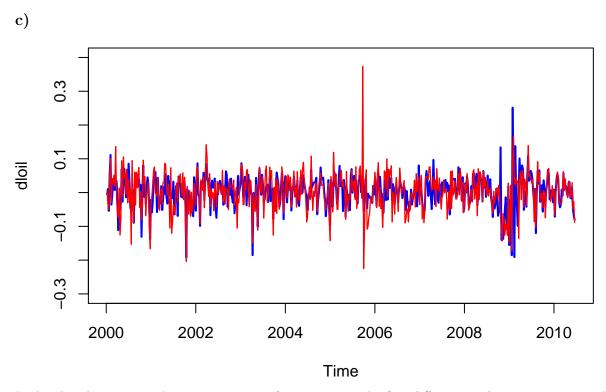
## Warning: package 'astsa' was built under R version 3.3.2



The time series do not look stationary, the mean value seem to change depending on time, and there is no particular pattern happening over time. However, the two time series do have similar shapes indicating that they are related to each other.



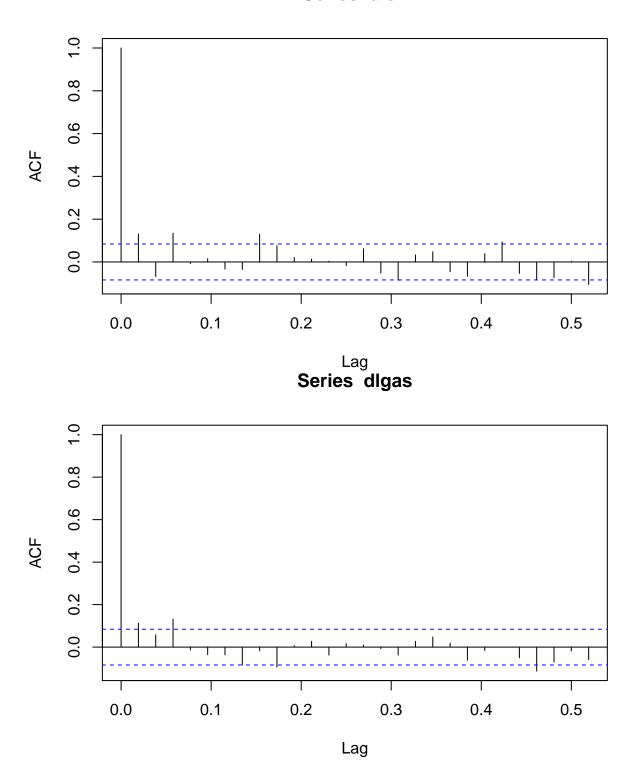
The log-transformation put the two time series in similar scales which makes it easier to compare them in detail. The fluctuations are clearly similar in both time series. Although we can not call the time series stationary.



In the plot above we see the two time series after computing the first difference and we can see a resemblance of the two with a few different peaks, but otherwise quite similar. The mean seems more stable except a wild

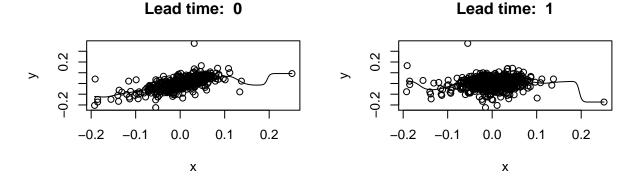
fluctuation around 2009 and could be considerd stationary now.

# Series dloil

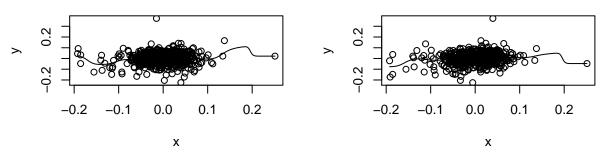


The autocorrelation plots show that there is not much correlation in the data after transformations.

d)



Lead time: 2 Lead time: 3



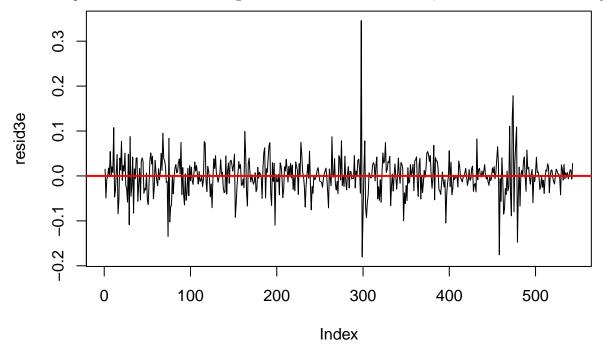
It does not seem to be any relationship between oil and gas when oil has a lead time. Otherwise they do have a positive correlation as shown in the top-left plot. There are some outliers in the data, especially the two points that have high oil respectively gas values.

**e**)

```
tss <- ts.intersect(yt=yt, xt=xt, lag1xt=lag(xt, 1), dummy=xt > 0)
model3e <- lm(yt ~ xt + lag1xt + dummy, data = tss)</pre>
resid3e <- resid(model3e)</pre>
summary(model3e)
##
## Call:
## lm(formula = yt ~ xt + lag1xt + dummy, data = tss)
##
## Residuals:
##
                   1Q
                        Median
                                      3Q
   -0.18044 -0.02103 0.00003 0.02170
                                         0.34592
##
## Coefficients:
##
                Estimate Std. Error t value Pr(>|t|)
## (Intercept) -0.006176
                            0.003470
                                      -1.780
                                                0.0757 .
## xt
                0.694200
                            0.058898
                                      11.786
                                                <2e-16 ***
                                       0.327
                                                0.7439
## lag1xt
                0.012660
                            0.038729
## dummy
                0.012376
                            0.005542
                                        2.233
                                                0.0259 *
## ---
```

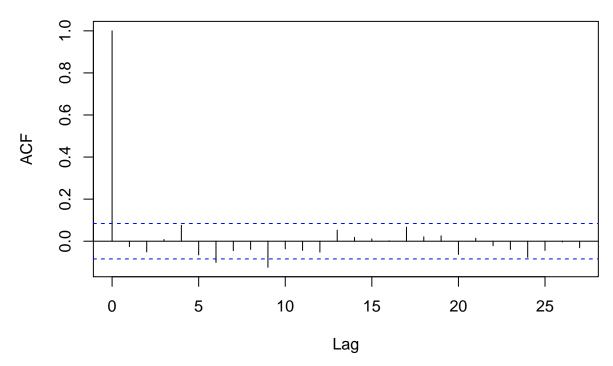
```
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.04202 on 539 degrees of freedom
## Multiple R-squared: 0.445, Adjusted R-squared: 0.4419
## F-statistic: 144.1 on 3 and 539 DF, p-value: < 2.2e-16</pre>
```

We can see from the linear fit that lag is not significant which supports our analysis so far that there does not seem be any correlation from previous/future data, only from present. The dummy variable is significant and has a positive coefficient indicating that if there is an increase in oil, there is also an increase in gas.



The residuals do look stationary with a few outlying peaks. There seems to be no dependency in shorter time or over time either.

# Series resid3e



The autocorrelation for the residuals also indicate that there is no linear relationship between past/future values.