

Activity 5

1. Consider the potential energy of a particle in a 1D system shown in Fig. 1.
 - (a) Draw the equilibrium points on the graph. Label each as stable or unstable.
 - (b) For points A, B, and C shown on the plot, draw the direction the force \vec{F} points when the particle is at the corresponding position.
 - (c) Rank the forces the particle experiences at point A, B, and C from largest to smallest in magnitude.

2. Consider the potential energy of a pair of atoms in a molecular bond as shown in Fig. 2. The x -axis displays r , the separation between the atoms. This plot is normalized to ϵ , the binding energy, and σ , the average bond length, so that the axes are dimensionless.
 - (a) Draw any/all equilibrium points on the graph. Label each as stable or unstable.
 - (b) If the total mechanical energy $E = -0.5\epsilon$, at what values of r does the kinetic energy, T , equal 0? These are called “turning points.”
 - (c) If the total mechanical energy $E = +0.5\epsilon$, what are the turning points?
 - (d) At what value of E does the radius of separation between the atoms become unbounded?

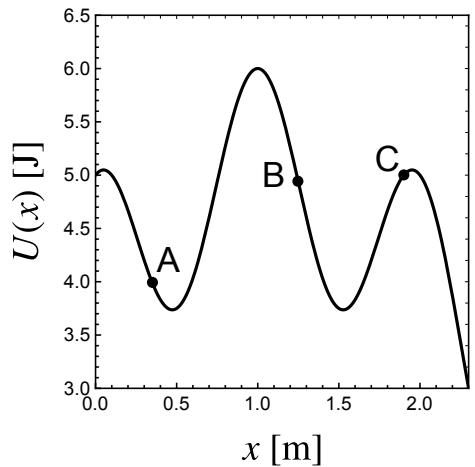


Figure 1: The path between Point A and Point B.

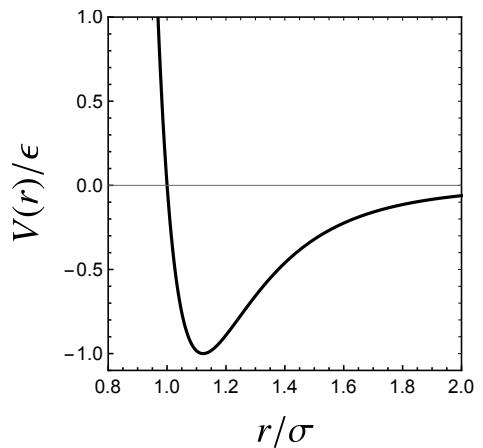


Figure 2: The path between Point A and Point B.

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3. For 1D systems only subject to conservative forces, show that the following equation follows from conservation of mechanical energy:

$$\dot{x} = \pm \sqrt{\frac{2}{m}} \sqrt{E - U(x)} \quad (1)$$

4. Consider a ball dropped off a cliff. Let x be the vertical axis, and $x = 0$ the position of the ball when it is dropped. Using Eq. (1) to find $x(t)$ for the ball.

5. Find $\vec{\nabla} \times \vec{F}$ for the following forces. Are they conservative? If so, find $U(\vec{r})$. Draw the path you used to evaluate $U(\vec{r})$, and check that $\vec{\nabla}U = -\vec{F}$. [Note: Useful integral: $\int xe^x dx = (x-1)e^x + C$]

- (a) $F = x^2 \hat{x} + 3y \hat{y}$
- (b) $F = y^2 x \hat{x} + x^2 y \hat{y}$
- (c) $F = xe^{xy} \hat{x} - ye^{xy} \hat{y}$
- (d) $F = ye^{xy} \hat{x} + xe^{xy} \hat{y}$