

## Activity 5

1. Consider the potential energy of a particle in a 1D system shown in Fig. 1.

- (a) Draw the equilibrium points on the graph. Label each as stable or unstable.
- (b) For points A, B, and C shown on the plot, draw the direction the force  $\vec{F}$  points when the particle is at the corresponding position.
- (c) Rank the forces the particle experiences at point A, B, and C from largest to smallest in magnitude.

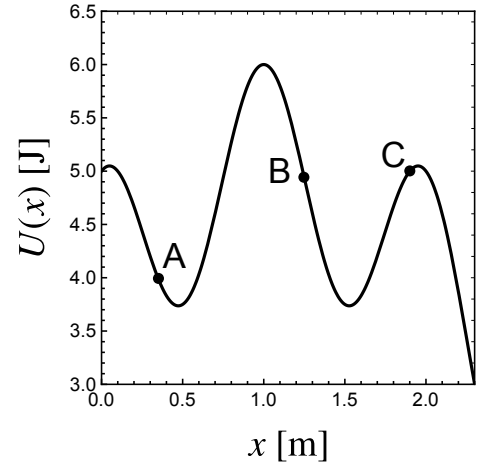


Figure 1: The path between Point A and Point B.

2. Consider the potential energy of a pair of atoms in a molecular bond as shown in Fig. 2. The  $x$ -axis displays  $r$ , the separation between the atoms. This plot is normalized to  $\epsilon$ , the binding energy, and  $\sigma$ , the average bond length, so that the axes are dimensionless.

- (a) Draw any/all equilibrium points on the graph. Label each as stable or unstable.
- (b) If the total mechanical energy  $E = -0.5\epsilon$ , at what values of  $r$  does the kinetic energy,  $T$ , equal 0? These are called “turning points.”

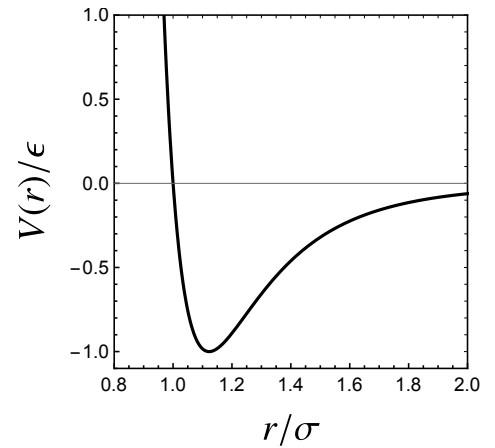


Figure 2: The path between Point A and Point B.

- (c) If the total mechanical energy  $E = +0.5\epsilon$ , what are the turning points?
- (d) At what value of  $E$  does the radius of separation between the atoms become unbounded?

### Activity 5

3. For 1D systems only subject to conservative forces, show that the following equation follows from conservation of mechanical energy:

$$\dot{x} = \pm \sqrt{\frac{2}{m}} \sqrt{E - U(x)} \quad (1)$$

4. Consider a ball dropped off a cliff. Let  $x$  be the vertical axis, and  $x = 0$  the position of the ball when it is dropped. Using Eq. (1) to find  $x(t)$  for the ball.

5. Find  $\vec{\nabla} \times \vec{F}$  for the following forces. Are they conservative? If so, find  $U(\vec{r})$ . Draw the path you used to evaluate  $U(\vec{r})$ , and check that  $\vec{\nabla}U = -\vec{F}$ . [Note: Useful integral:  $\int x e^x dx = (x - 1)e^x + C$ ]

- (a)  $F = x^2 \hat{x} + 3y \hat{y}$
- (b)  $F = y^2 x \hat{x} + x^2 y \hat{y}$
- (c)  $F = x e^{xy} \hat{x} - y e^{xy} \hat{y}$
- (d)  $F = y e^{xy} \hat{x} + x e^{xy} \hat{y}$