

# 2551 - Put Marbles in Bag

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Link: <https://leetcode.com/problems/put-marbles-in-bags>

You have  $k$  bags. You are given a 0-indexed integer array `weights` where `weights[i]` is the weight of the  $i^{\text{th}}$  marble. You are also given the integer  $k$ .

Divide the marbles into the  $k$  bags according to the following rules:

- No bag is empty.
- If the  $i^{\text{th}}$  marble and  $j^{\text{th}}$  marble are in a bag, then all marbles with an index between the  $i^{\text{th}}$  and  $j^{\text{th}}$  indices should also be in that same bag.
- If a bag consists of all the marbles with an index from  $i$  to  $j$  inclusively, then the cost of the bag is `weights[i] + weights[j]`.

The score after distributing the marbles is the sum of the costs of all the  $k$  bags.

Return the difference between the maximum and minimum scores among marble distributions.

Example 1:

Input: `weights = [1,3,5,1]`,  $k = 2$

Output: 4

Explanation:

The distribution `[1],[3,5,1]` results in the minimal score of  $(1+1) + (3+1) = 6$ .

The distribution `[1,3],[5,1]`, results in the maximal score of  $(1+3) + (5+1) = 10$ .

Thus, we return their difference  $10 - 6 = 4$ .

Example 2:

Input: `weights = [1, 3]`,  $k = 2$

Output: 0

Explanation: The only distribution possible is `[1],[3]`.

Since both the maximal and minimal score are the same, we return 0.

**Constraints:**

- $1 \leq k \leq \text{weights.length} \leq 10^5$
- $1 \leq \text{weights}[i] \leq 10^9$

**Solution:**

Given array, `[1, 3, 5, 1]`,  $k=2 \Rightarrow$  Two groups.

These groups should be continuous.

Cost = Sum of the Weight of the start and end index.

Score = Sum (Costs)

We need max Score - Min Score

Simple Solution:

Say the array is longer,  $[1, 2, 3, 4, 5, 6, 7]$

Now ① and ⑦ are fixed ( $k \geq 1$ )

$$\Rightarrow \text{Min} = 1 + 7 + u + v, \text{ Max} = 1 + 7 + i + j$$

First and last element sum is always a part of the Overall cost

$[1, 2, 3, 4, 5, 6, 7]$

$$\text{cost} = 1 + 7 + 3 + 4$$

This True for any number of splits.

For any  $k$ , we have to compare the split.

if  $k == 1$ : return 0.

splits  $[] \rightarrow$  Create Array

for  $i$  in range( $\text{len}(\text{Weight}) - 1$ ):

add  $\text{Weight}[i] + \text{weight}[i+1]$  to split

sort splits

sort split

max. score = weight[0] + weights[-1] + sum[last k values]

min. score = weight[0] + weight[-1] + sum[first k values]

return the difference