ENGR I1100
Engineering Analysis

INTRO TO MATLAB

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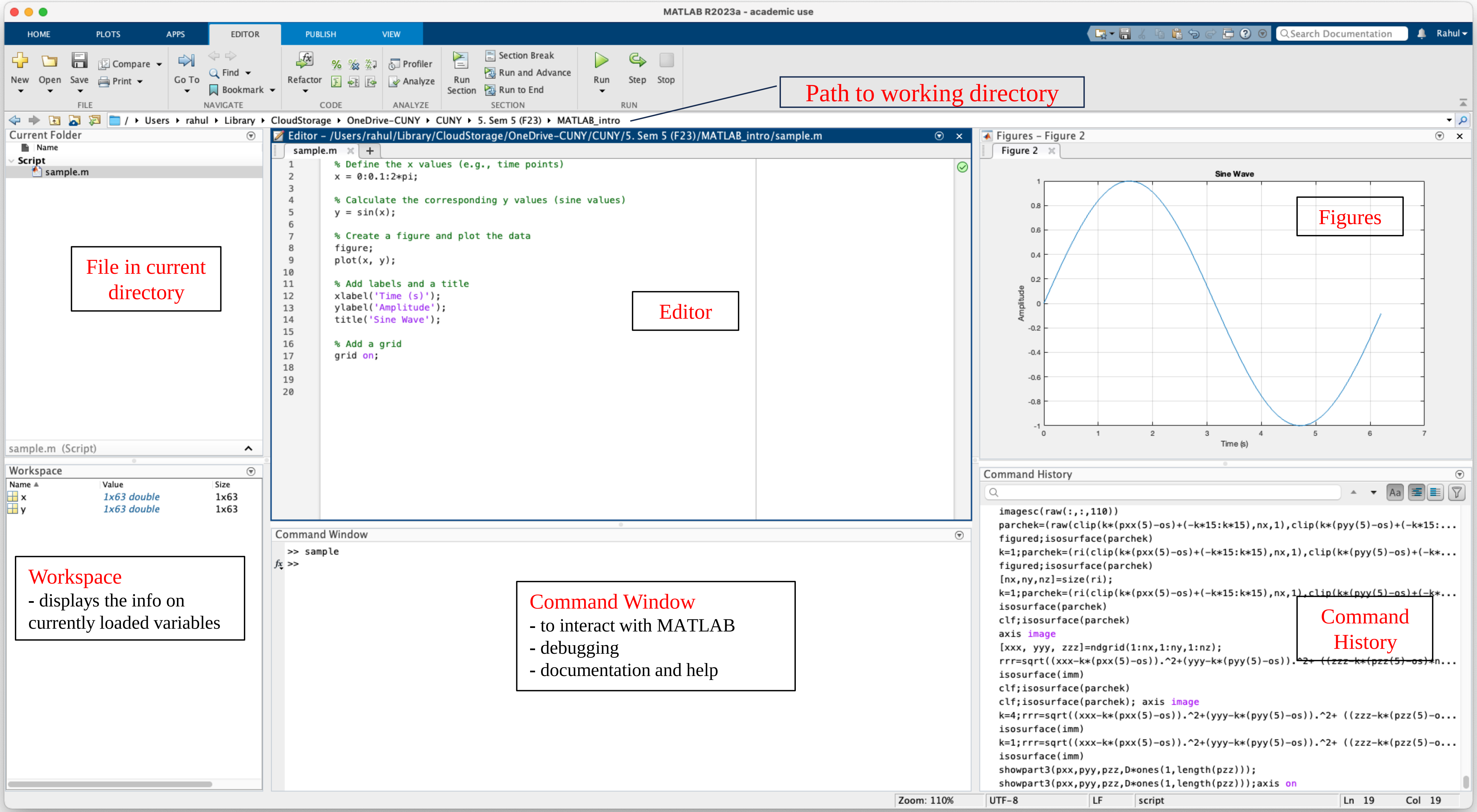
MATLAB vs PYTHON

MATLAB	Python
• Proprietary, high-level programming language primarily designed for numerical and matrix computations. Written in C/C++.	• Open-source, general-purpose programming language known for its versatility. Written in C.
• MATLAB offers toolboxes for various domains: Image Processing Toolbox, Aerospace Toolbox, Deep Learning Toolbox, SimBiology Toolbox, etc.	• Rich ecosystem of libraries and packages: NumPy, Matplotlib, openCV, etc.
• MATLAB provides its own integrated development environment (IDE)	• Python offers multiple IDE options: Jupyter Notebook, PyCharm, Visual Studio Code, etc.
• Common in academia, engineering, and simulation	• Widely used in diverse fields – Data analytics, Web development, FinTech, AI

MATLAB screen overview



MATLAB syntax

Variables

Command Window

```
>> 1+2*3

ans =

     7

>> x=1+2*3

x =

     7

>> x=1+2*3;
>>
```

(adding semicolon does not print the output)

Using it as a calculator

Expressing variable as a function

$$y = e^{-a} * sin(\pi/x^2) + 10 * \sqrt{y}$$

Command Window

```
>> a=5;x=2;y=8;
>> y=exp(-a)*sin(pi/x^2)+10*sqrt(y)

y =

   28.2890
```

Note:
In programming we use numerical variables which are different than symbolic variables used in conventional math

Table 2.1: Elementary functions

`cos(x)`	Cosine	`abs(x)`	Absolute value
`sin(x)`	Sine	`sign(x)`	Signum function
`tan(x)`	Tangent	`max(x)`	Maximum value
`acos(x)`	Arc cosine	`min(x)`	Minimum value
`asin(x)`	Arc sine	`ceil(x)`	Round towards $+\infty$
`atan(x)`	Arc tangent	`floor(x)`	Round towards $-\infty$
`exp(x)`	Exponential	`round(x)`	Round to nearest integer
`sqrt(x)`	Square root	`rem(x)`	Remainder after division
`log(x)`	Natural logarithm	`angle(x)`	Phase angle
`log10(x)`	Common logarithm	`conj(x)`	Complex conjugate

Matrix

Command Window

```
>> v=[1 3 5 8 12 13] % Row vector

v =

     1     3     5     8    12    13

>> w=[1;6;9;12;20;21] % Column vector

w =

     1
     6
     9
    12
    20
    21

>> v' % transpose of a vector

ans =

     1
     3
     5
     8
    12
    13
```

comment

Command Window

```
>> A=[1 2 3; 4 5 6; 7 8 9] % 3 x 3 Matrix

A =

     1     2     3
     4     5     6
     7     8     9

>> A(2,1) % extracting an element from a matrix

ans =

     4

>> B = randi([0,100],5,8) % creating a 5x8 matrix with random integers between 0-100

B =

    44    49    27    50    75    96    84    35
    38    45    68    96    25    55    25    19
    77    65    66    34    51    14    82    25
    80    71    16    59    70    15    24    62
    18    76    12    22    89    26    93    47

>> C = B(2:end,3:7) % slicing the boxed part from the B matrix

C =

    68    96    25    55    25
    66    34    51    14    82
    16    59    70    15    24
    12    22    89    26    93

>> B % the orignal matrix B remains unaltered

B =

    44    49    27    50    75    96    84    35
    38    45    68    96    25    55    25    19
    77    65    66    34    51    14    82    25
    80    71    16    59    70    15    24    62
    18    76    12    22    89    26    93    47
```

Important:
in MATLAB indexing starts from 1

Matrix operations

```
>> x=0:0.1:5; % vector from 0-5 with increament of 0.1
>> length(x)

ans =

    51

>> y=linspace(0,10,100); % linspace creates a vector from 0-10 with 100 subintervals
>> length(y)

ans =

   100
```

Colon operator

linspace operator

```
>> a=[1 2 3 4];b=[10 11 12 13];c=[5;6;7;8]; % a and b row vectors and c column vector
>> a*c %matrix multiplication

ans =

    70

>> a*b %incompatible dimensions for matrix multiplication
Error using  *
Incorrect dimensions for matrix multiplication. Check that the number of columns in the first matrix matches the number of rows in the second
matrix. To operate on each element of the matrix individually, use TIMES (.*) for elementwise multiplication.

Related documentation

>> a.*b % elementwise multiplication

ans =

    10    22    36    52

>> b./a %elementwise division

ans =

   10.0000    5.5000    4.0000    3.2500
```

matrix operations

```
>> a+b % elementwise addition

ans =

    11    13    15    17

>> b-a % elementwise subtraction

ans =

     9     9     9     9
```

Plots

Plots

Q. Plot y as a function of x:

$y1 = 2\cos(x)$,

$y2 = \cos(x)$, and

$y3 = 0.5 * \cos(x)$,

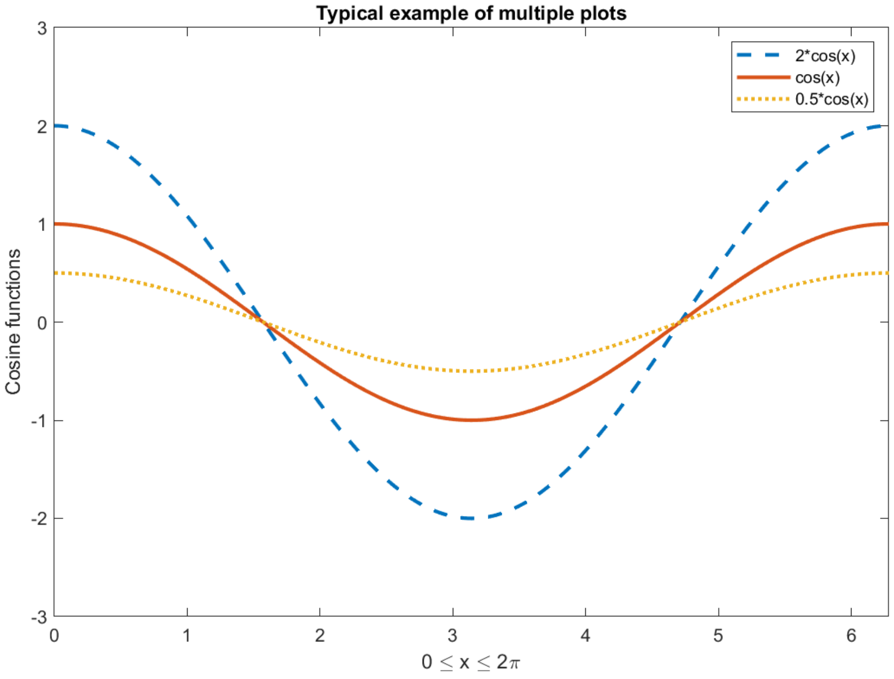
in the interval $0 \leq x \leq 2\pi$.

Command Window

```
>> x = 0:pi/100:2*pi; % or x=linspace(0,2*pi,201)
>> y1 = 2*cos(x); %function 1
>> y2 = cos(x); %function 2
>> y3 = 0.5*cos(x); %function 2
>> figure; %create a new figure handle
>> plot(x,y1,'--',x,y2,'-',x,y3,':') %plot takes in agruments: x, y and line style
>> xlabel('0 \leq x \leq 2\pi') %x label
>> ylabel('Cosine functions') % y label
>> legend('2*cos(x)','cos(x)','0.5*cos(x)') %legends
>> title('Typical example of multiple plots') % title of the plot
>> axis([0 2*pi -3 3]) % setting the axis bounds for plots
```

Function details

Plot details



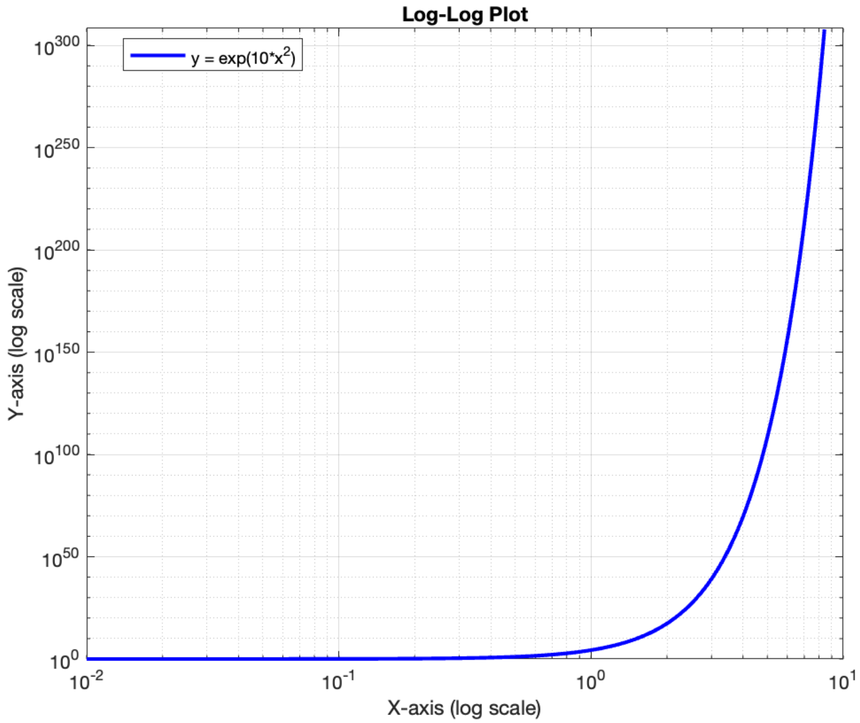
<u>Note</u>:

- Multiple (x, y) pairs arguments create multiple graphs with a single call to plot
- Plot function also has the attributes for line style, symbol color and line weight

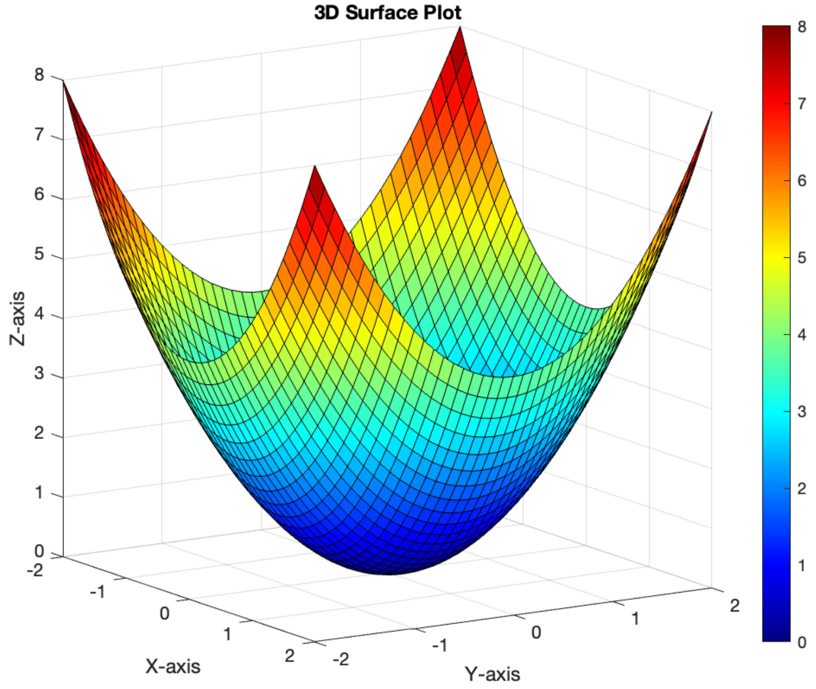
Table 2.3: Attributes for `plot`

Symbol	Color	Symbol	Line Style	Symbol	Marker
k	Black	–	Solid	+	Plus sign
r	Red	– –	Dashed	o	Circle
b	Blue	:	Dotted	*	Asterisk
g	Green	–.	Dash-dot	.	Point
c	Cyan	none	No line	×	Cross
m	Magenta			s	Square
y	Yellow			d	Diamond

Plots



Log-log plot



Surf plot

more plot types: scatter, bar, histogram, contour, heatmap etc.

Discretization

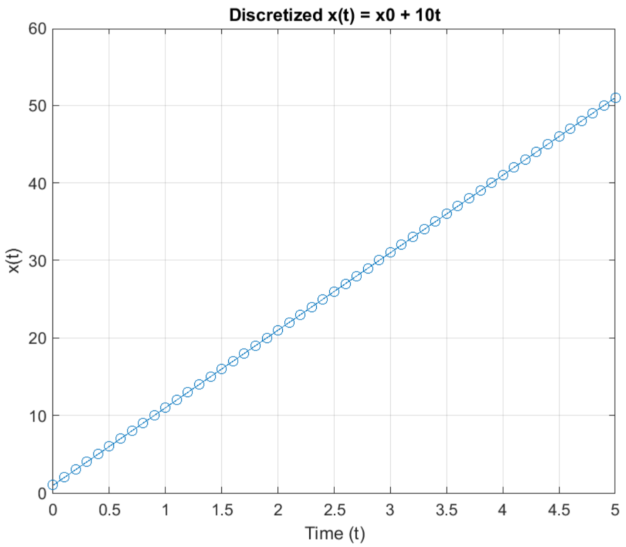
Discretization (example 1)

- Discretization is the process to convert a continuous equation into a form that can be used to calculate numerical solutions

Q. let' s say an object is traveling along the + x direction with a speed of 10 m/s, we would write its position vector as : **x (t) = x0 + 10t**. compute the position for time interval 0s to 5s.

We know that the particle will travel a distance of $10*\Delta t$ for a time interval of Δt, so that we can write:

$$x(i) = x(i-1) + 10*\Delta t$$



Editor – /Users/rahul/Library/CloudStorage/OneDrive-CUNY/CUNY/5. Sem 5 (F23)/MATLAB_intro/discretization_1.m *

discretization_1.m *

```
%% code for  discretization of eq: x(t) = x0 + 10t

clc;    % clearing all output in command window
clear;  % clearing all variables in workspace
clf;    % clearing only the current figure handle

% Define the initial position, time and time step
x0=1;                  %initial position
t0 = 0;                % Initial time
t_step = 0.1;          % Time step
tf = 5;                % Final time

%listing all the t values
t_values = t0:t_step:tf;

% Initialize array to store x values
x_values = zeros(1, length(t_values));

% Initial condition
x_values(1)=x0;

% Loop to discretize and calculate x(t)
for i = 2:length(t_values)
    x_values(i) = x_values(i-1) + 10 * t_step;
end

% Plot the results
plot(t_values, x_values, '-o');
xlabel('Time (t)');
ylabel('x(t)');
title('Discretized x(t) = x0 + 10t');
grid on;
```

Discretization (example 2)

$$\frac{dy}{dx} = -2y + x^2$$

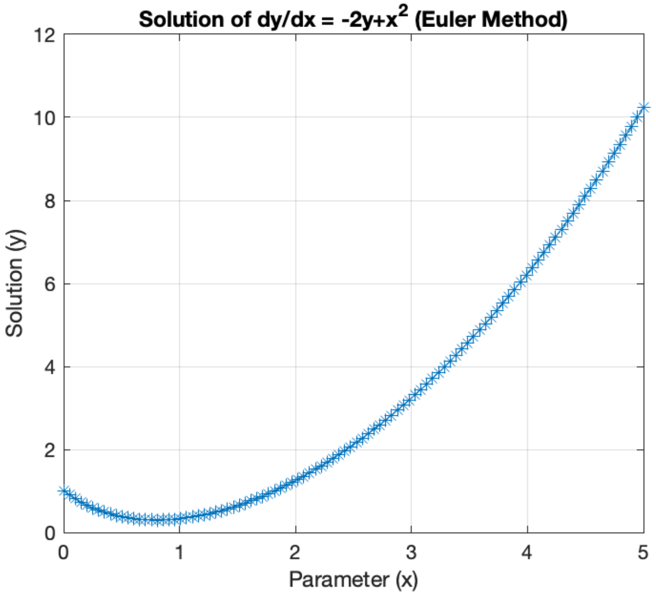
Q. Numerically solve the above-mentioned ordinary differential equation (ode) by discretization for the x interval [0,5]

Discretizing using the Euler's method:

$$y_{i+1} = y_i + hf(x_i, y_i)$$

where,

- y_{i+1} is the next estimated solution value;
- y_i is the current value;
- h is the interval between steps;
- $f(x_i, y_i)$ is the value of the derivative at the current (x_i, y_i) point.



We can write it as:

$$y_i = y_{i-1} + hf(x_{i-1}, y_{i-1})$$

Editor - C:\Users\panda\OneDrive - CUNY\CUNY\5. Sem 5 (F23)\MATLAB_intro\myode.m

discretization_2.m | myode.m

```
%% This function is an ode
% this function is used in the script discretization_2.m to evalute the
% derivation at a certain point.

function dydx = myode(x, y)
% Define the ODE dy/dx = -2y +x^2
dydx = -2*y+x^2;
end
```

discretization_2.m

```
%% code for discretization of ode: y'= -2y+x^2

clc;    % clearing all output in command window
clear;  % clearing all variables in workspace
clf;    % clearing only the current figure handle

%Define the ODE function
%we can define the ode as shown below or write it into a function and use
%it in this script. But here we use the function myode.m
%myode = @(x, y) -2 * y+x^2;

% Define the time span for the solution
xspan = [0, 5];  % Start at t=0 and end at t=5

% Define the initial condition
y0 = 1;

% Discretize the time span into discrete time points
x_values = linspace(xspan(1), xspan(2), 100); % 100 time points
h = x_values(2) - x_values(1); %delta x (spacing)

% Initialize array to position values (y)
y_values = zeros(1, length(x_values));

% Set the initial values
y_values(1) = y0;

% Apply the Euler method for numerical integration
for i = 2:length(x_values)
    y_values(i) = y_values(i-1) + h * myode(x_values(i-1), y_values(i-1));

end

% Plot the solution
plot(x_values, y_values, '-*', 'LineWidth', .5);
xlabel('Parameter (x)');
ylabel('Solution (y)');
title('Solution of dy/dx = -2y+x^2 (Euler Method)');
grid on;
```

ODE function

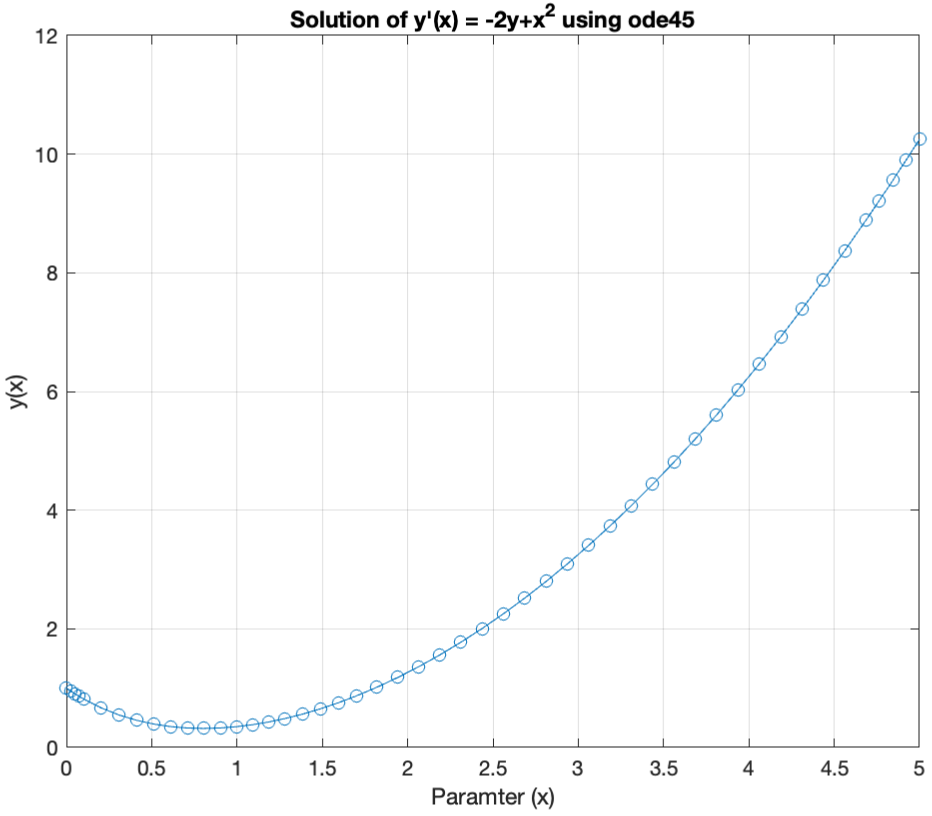
$$\frac{dy}{dx} = -2y + x^2$$

MATLAB has an inbuilt function called **ODE** to numerically solve ordinary differential equations. Here we use ode45 which uses Runge-Kutta approximation to solve the ode.

Editor – /Users/rahul/Library/CloudStorage/OneDrive-CUNY/CUNY/5. Sem 5 (F23)/MATLAB_intro/ode45_.m

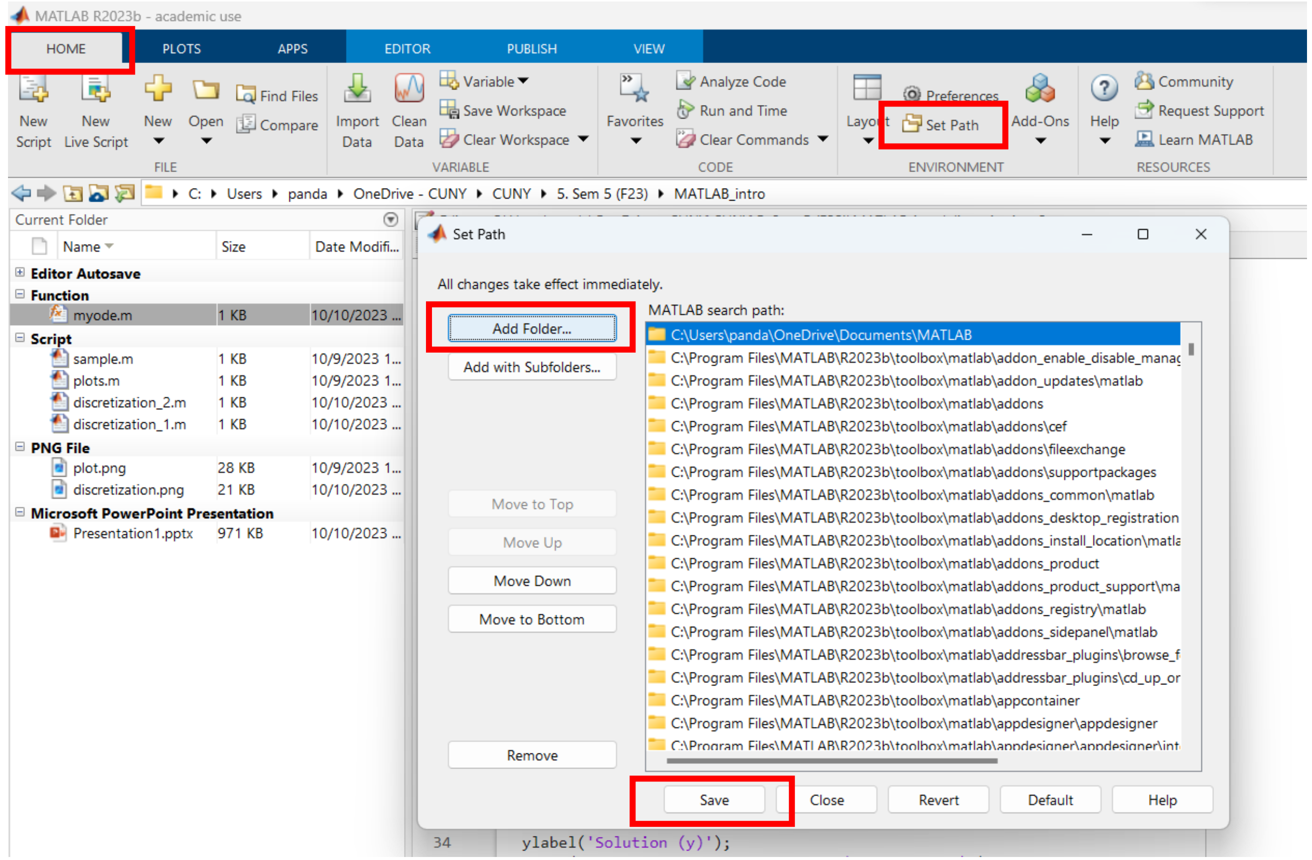
ode45_.m | myode.m | +

```matlab
%% code for discretization of ode: y'= -2y+x^2

clc;    % clearing all output in command window
clear;  % clearing all variables in workspace
clf;    % clearing only the current figure handle

% Define the time span for the solution
xspan = [0, 5];  % Start at t=0 and end at t=5

% Define the initial condition
y0 = 1;

% Use the ode45 solver to solve the ODE using the custom ODE function
[x, y] = ode45(@myode, xspan, y0);

% Plot the results
plot(x, y, '-o');
xlabel('Paramter (x)');
ylabel('y(x)');
title('Solution of y''(x) = -2y+x^2 using ode45');
grid on;
```



Points to remember

1. When working with a script which requires a function (e.g., the ODE function) make sure the script and the function are in the same directory or else add the directory which contains the function file to the path



Adding a directory to the path:

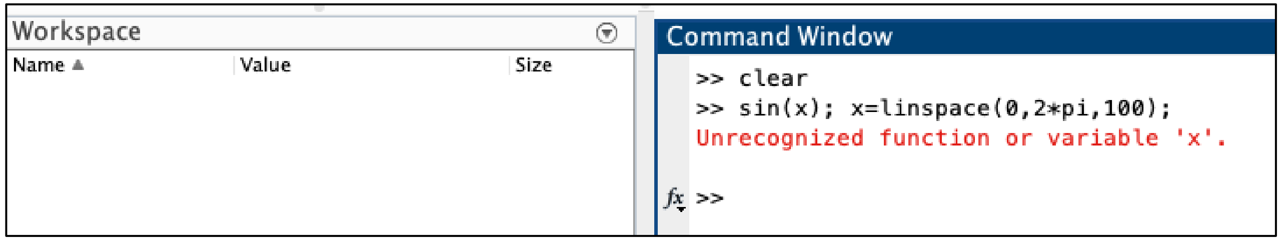
1. in the HOME tab
2. click on set path
3. add the folder you wish to work with
4. save

Points to remember

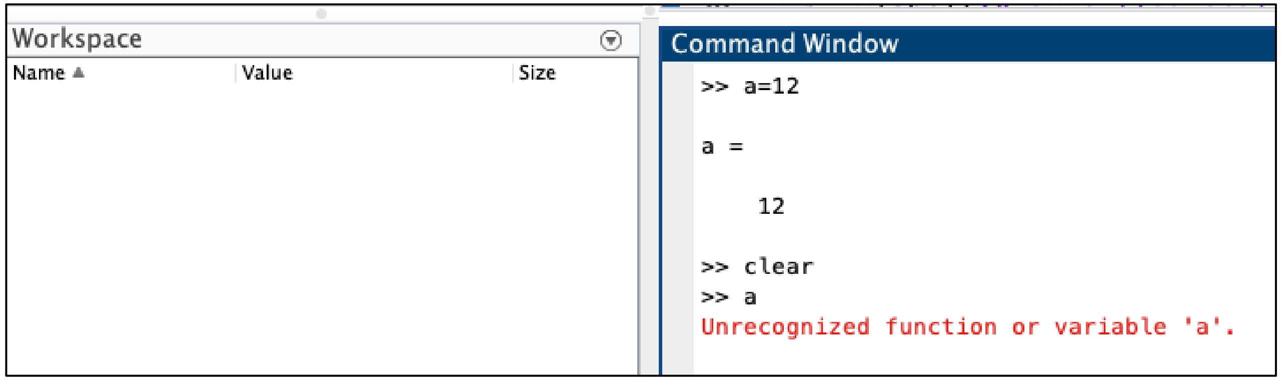
2. Make sure your workspace is clear before you execute your code so that the script does not use variables already in the memory.

```
clc;    % clearing all output in command window
clear;  % clearing all variables in workspace
clf;    % clearing only the current figure handle
```

3. You can only use variables after they are stored in the workspace



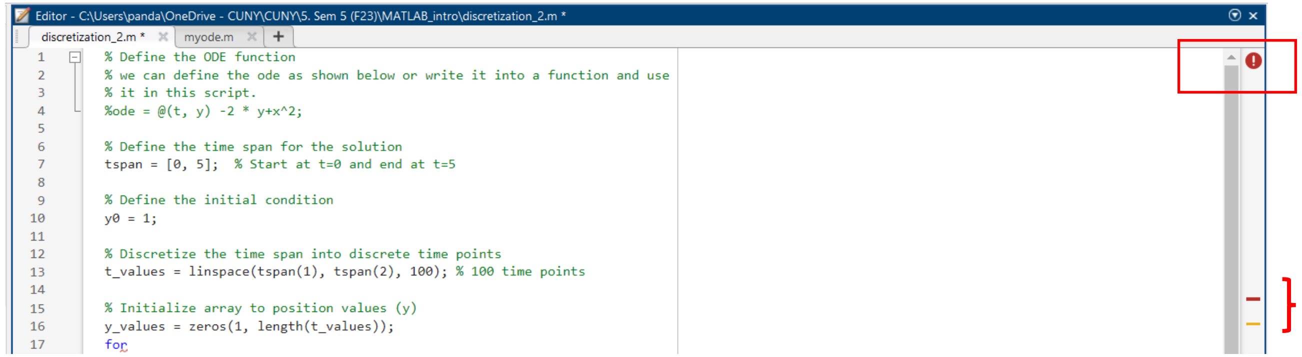
here we called in the variable x without defining it first. Also, the workspace has no variable stored



cannot call in a variable when it is not stored in workspace even though you see it in the command window.

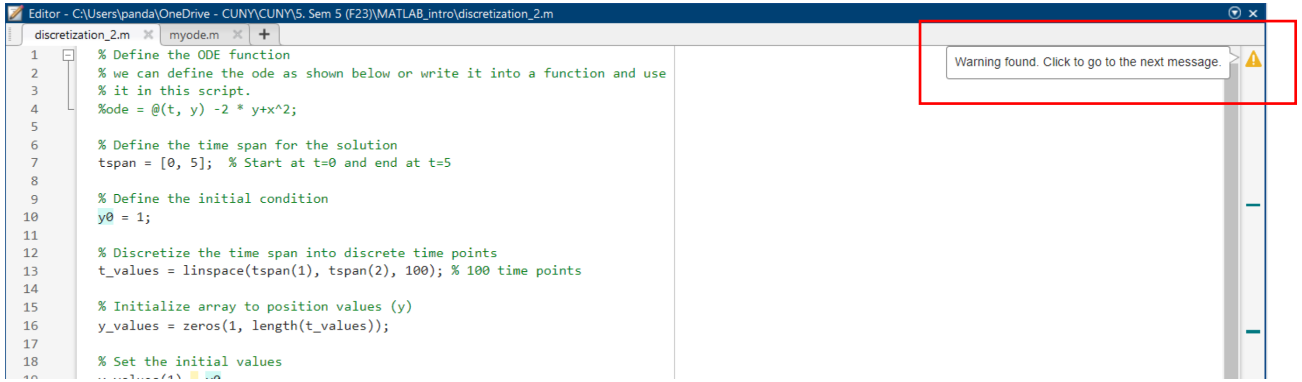
Points to remember

4. Good practice to look for warnings before executing the script



red exclamation – script won't run

click on these line markers to view more info on the error



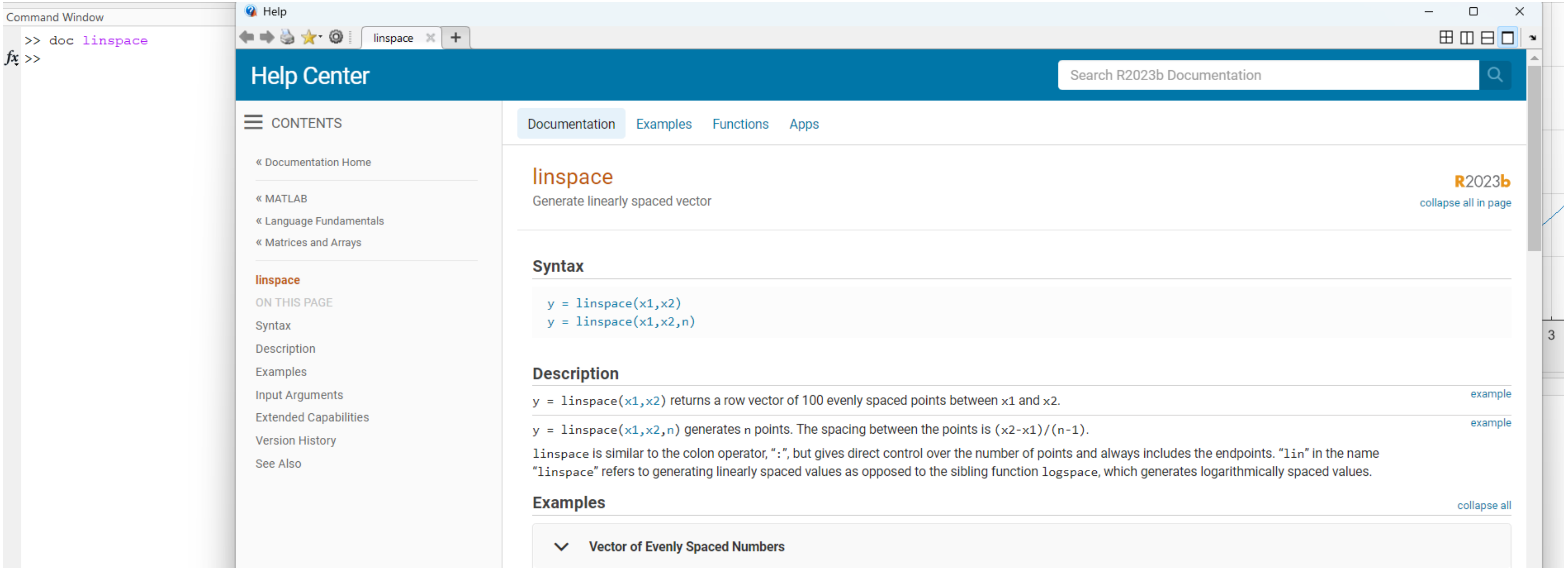
yellow exclamation – script might execute but with some issue

green tick – script is error free

Points to remember

5. To look up documentation on any MATLAB function/ feature just type :
<u>doc <function/feature></u> OR <u>help <function/feature></u> in the command window.
A new help window will pop up.

Looking up info on **linspace**



Thank you!

Project due – Second week in November

Office hours: Tentatively one week before submission

To access scripts used here and additional study material click [here]

For question: rpandar000@citymail.cuny.edu ; ST-305

Download MATLAB: https://www.mathworks.com/academia/tah-portal/city-university-of-new-york-1111017.html (sign in with your cuny.edu email ID)