

## Homework 7

### Problem 2

$$A = \begin{bmatrix} 2 & -1 & 0 \\ -1 & 2 & 1 \\ 0 & 1 & 2 \end{bmatrix}$$

as form of  $O\Lambda O^T$

O =

$$\begin{bmatrix} -0.5000 & 0.7071 & 0.5000 \\ -0.7071 & -0.0000 & -0.7071 \\ 0.5000 & 0.7071 & -0.5000 \end{bmatrix}$$

D =

$$\begin{bmatrix} 0.5858 & 0 & 0 \\ 0 & 2.0000 & 0 \\ 0 & 0 & 3.4142 \end{bmatrix}$$

### Problem 6

If Matrix A is positive definite or semi-positive definite, then A =

Part a:

$$A = \begin{bmatrix} 1 & 3 \\ 3 & 9 \end{bmatrix}$$

$$O_a = \begin{bmatrix} -0.9487 & 0.3162 \\ 0.3162 & 0.9487 \end{bmatrix}$$

$$D_a = \begin{bmatrix} 0 & 0 \end{bmatrix}$$

$$\begin{matrix} 0 & 10 \\ 1 & 3 \end{matrix}$$

The matrix is Semi-Positive Definite by observing the eigenvalues.

$$A_{\text{root}} = \begin{matrix} 0 & 0 \\ 1 & 3 \end{matrix}$$

**Part b:**

$$B = \begin{bmatrix} 6 & 10 & 11 \\ 10 & 19 & 19 \\ 11 & 19 & 21 \end{bmatrix}$$

$$O_b =$$

$$\begin{matrix} -0.8745 & 0.3270 & 0.3583 \\ -0.0244 & -0.7674 & 0.6407 \\ 0.4845 & 0.5515 & 0.6791 \end{matrix}$$

$$D_b =$$

$$\begin{matrix} 0.1856 & 0 & 0 \\ 0 & 1.0842 & 0 \\ 0 & 0 & 44.7302 \end{matrix}$$

The matrix is Positive Definite by observing the eigenvalues.

$$B_{\text{root}} =$$

$$\begin{matrix} -0.3767 & -0.0105 & 0.2087 \\ 0.3405 & -0.7991 & 0.5743 \\ 2.3963 & 4.2850 & 4.5417 \end{matrix}$$

**Part c:**

$$C = \begin{bmatrix} 2 & 6 & 10 \\ 6 & 10 & 14 \\ 10 & 14 & 18 \end{bmatrix}$$

O\_c =

0.8424	0.4082	0.3516
0.1647	-0.8165	0.5534
-0.5130	0.4082	0.7551

D\_c =

-2.9165	0	0
0	0.0000	0
0	0	32.9165

The matrix is **neither** Positive Definite **nor** Semi-Positive Definite by observing the eigenvalues.

### Problem 3

$O^T A O$

final\_matrix = 

-1	0	0
0	2	0
0	0	2

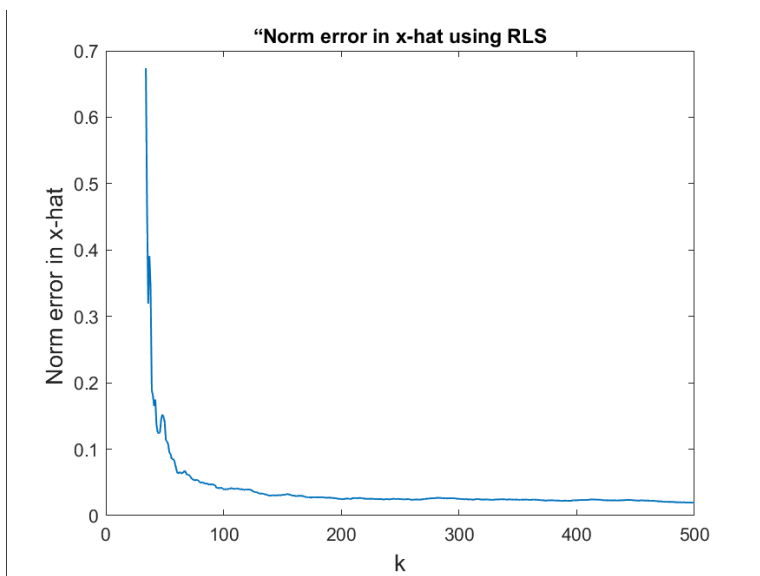
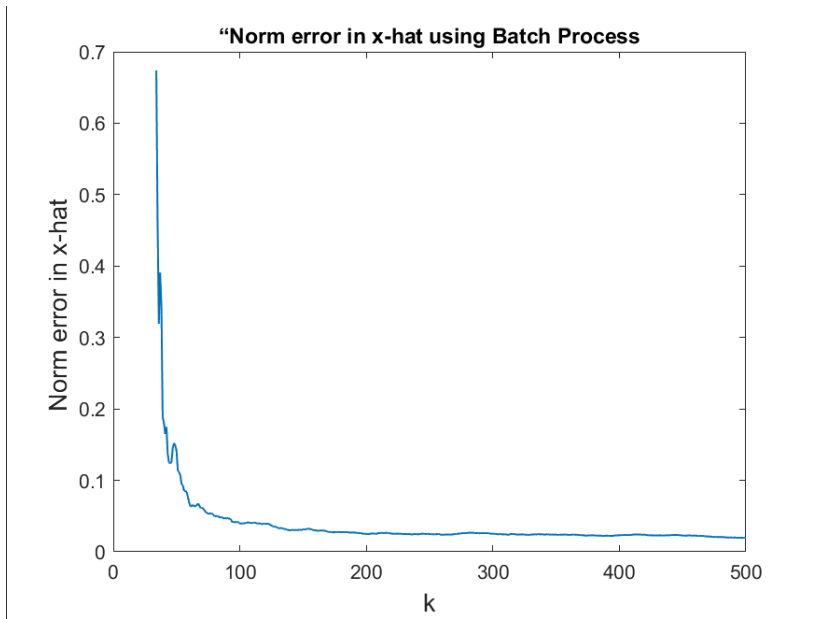
### Problem 4

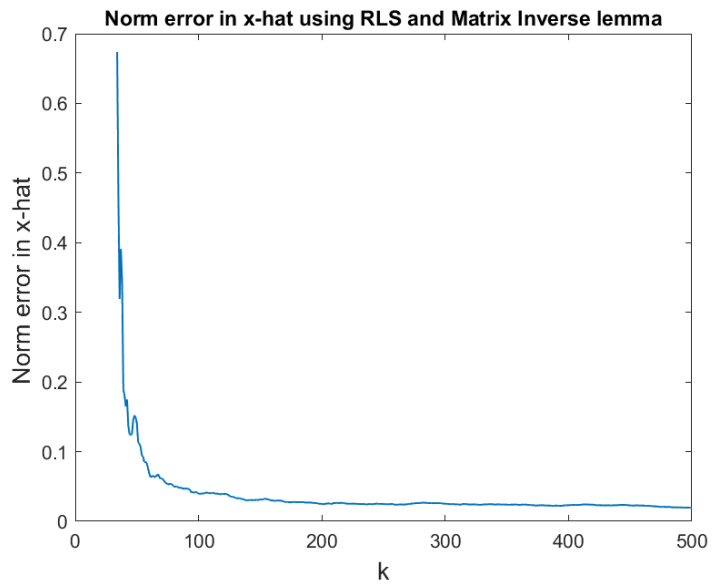
Step (a): n = 34

Total\_time for batch process = 3.1442 sec

Total\_time for RLS without Matrix Inversion lemma = 0.4463 sec

Total\_time for RLS with Matrix Inversion lemma = 0.2729 sec





### Problem 5:

N value is 7

