

## Homework solutions

### Question 1:

The below are solutions obtained from code where

$x\_sol$  is the estimated solution for  $x$ ;  
 $cov$  is the covariance of the estimate;

#### Part a:

$cov =$

4.0000	-2.7500
-2.7500	2.0000

$x\_sol =$

0.6194
0.4591

#### Part b

$cov =$

0.0679	-0.0260
-0.0260	0.1129

$x\_sol =$

-1.4303
1.8791

#### Part c

$cov =$

0.0487	0.0054
0.0054	0.0618

$x_{sol} =$

-1.2201

1.5368

## Question 4

The below are solutions obtained from code where

$x_{sol}$  is the estimated solution for  $x$ ;

*covariance* is the covariance of the estimate;

### Part a:

covariance =

0.1938 -0.0812

-0.0812 0.1188

$x_{sol} =$

0.4504

0.4963

### Part b

covariance =

0.0545 -0.0105

-0.0105 0.0828

$x_{sol} =$

-1.0134

1.2402

### Part c

covariance =

0.0437	0.0072
0.0072	0.0538

x\_sol =

-1.0296
1.2667

## Question 5

### Part a:

The below are solutions obtained from code where  
 $x\_sol\_wls$  is the estimated solution for x from WLS;

x\_sol\_wls =

-1.3169
1.4368

### Part b:

The below are solutions obtained from code where  
 $x\_sol\_blue$  is the estimated solution for x from BLUE;  
 $cov\_blue$  is the covariance of the estimated solution;

cov\_blue =

0.0317	-0.0079
-0.0079	0.0198

x\_sol\_blue =

-1.3169  
1.4368

### Part c:

The below are solutions obtained from code where

*x\_sol\_less* is the estimated solution for x from MVE with  $P = 100I$ ;

*covariance\_less* is the covariance of the estimated solution with  $P = 100I$ ;

*covariance\_less* =

0.0317 -0.0079  
-0.0079 0.0198

*x\_sol\_less* =

-1.3163  
1.4365

The below are solutions obtained from code where

*x\_sol\_more* is the estimated solution for x from MVE with  $P = 1e6I$ ;

*covariance\_more* is the covariance of the estimated solution with  $P = 1e6I$ ;

*covariance\_more* =

0.0327 -0.0086  
-0.0070 0.0182

*x\_sol\_more* =

-1.3169  
1.4368

### Part d:

All the solutions are close to each other. Having the e variance of identity matrix is close to performing WLS and the variance of the model is also not affecting much because of this.

## Question 6

The below are solutions obtained from code where

$x\_sol$  is the estimated solution for  $x$  from MVE;

*covariance* is the covariance of the estimated solution;

covariance =

0.0437	0.0072
0.0072	0.0538

$x\_sol$  =

-0.8836
1.0802