Total No. of Questions: 4]
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**LNCT- University** 

1<sup>st</sup>MID SEM EXAMINATION (Nov – 2023) B.TECH I SEM Engg. Mathematics-I – [BT-102] (COMMON FOR ALL BRANCH)

Time: 1:30 Hrs

Max Marks :20

NOTE: All questions are compulsory & all questions carry equal marks.

Que1. Compute the approximate value of  $\sqrt{11}$  to the four decimal places by taking the first five terms of an appropriate Taylor's expansion.

[CO-1]

OR

Que1. If u = f(r), where  $r^2 = x^2 + y^2$  then show that

$$\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} = f''(r) + \frac{1}{r} f'(r).$$

[CO-1]

Que2. If 
$$u = (x^2 + y^2 + z^2)^{-1/2}$$
 then prove that  $z = \frac{\partial u}{\partial z} + y \frac{\partial u}{\partial z} + z \frac{\partial u}{\partial z} = -u$ .

OR

Que2. Verify the Rolle's Theorem for the function  $f(x) = x(x + 3)e^{-x/2}$ .

[CO-1]

Que3. Discuss the maxima and minima of function  $u = x^2 + y^2 - 3axy$ .

OR

[CO-1]

Que3. Find the expansion of sin-1 x by Maclaurin Theorem.

Que4. Evaluate 
$$\lim_{n\to\infty} \left[ (1+\frac{1}{n^2})(1+\frac{2^2}{n^2})(1+\frac{2^2}{n^2}).....(1+\frac{n^2}{n^2}) \right]^{(1/n)}$$
.

OR

Que4. Evaluate from the definition as the limit of sum  $\int_{1}^{3} (x^2 + x) dx$ .