

Total No. of Questions: 4]  
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LNCT- University

1<sup>st</sup> MID SEM EXAMINATION (Nov – 2023)  
B.TECH I SEM Engg. Mathematics-I – [BT-102]  
(COMMON FOR ALL BRANCH)

Time: 1:30 Hrs

Max Marks :20

**NOTE:** All questions are compulsory & all questions carry equal marks.

Que1. Compute the approximate value of  $\sqrt{11}$  to the four decimal places by taking the first five terms of an appropriate Taylor's expansion.

[ CO-1]

OR

Que1. If  $u = f(r)$ , where  $r^2 = x^2 + y^2$  then show that

$$\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} = f''(r) + \frac{1}{r} f'(r).$$

[ CO-1]

Que2. If  $u = (x^2 + y^2 + z^2)^{-1/2}$  then prove that  $x \frac{\partial u}{\partial x} + y \frac{\partial u}{\partial y} + z \frac{\partial u}{\partial z} = -u$ .

[ CO-1].

OR

Que2. Verify the Rolle's Theorem for the function  $f(x) = x(x+3)e^{-x/2}$ .

[ CO-1]

Que3. Discuss the maxima and minima of function  $u = x^3 + y^3 - 3axy$ .

OR

[ CO-1]

Que3. Find the expansion of  $\sin^{-1} x$  by Maclaurin Theorem.

[ CO-1]

Que4. Evaluate  $\lim_{n \rightarrow \infty} \left[ \left(1 + \frac{1}{n^2}\right) \left(1 + \frac{2^2}{n^2}\right) \left(1 + \frac{3^2}{n^2}\right) \dots \left(1 + \frac{n^2}{n^2}\right) \right]^{(1/n)}$ .

[ CO-2]

OR

Que4. Evaluate from the definition as the limit of sum  $\int_1^3 (x^2 + x) dx$ .

[ CO-2]