### LNCT UNIVERSITY, BHOPAL

Enrollment No. .....

#### B.TECH (CS/AIML) I SEMESTER EXAMINATION [DEC-2024] ADVANCED CALCULUS CS - 102

Maximum Marks: 70

Time Allowed: 3Hours

(SECTION -A)

Note:- Attempt all questions. Internal choices are given.

# Short Answer Type Questions (Attempt Any Five) [5x6=30]

- Verify Lagrange's Mean value Theorem for the function  $f(x) = x^3 + x^2 - 6x$  in [-1, 4]
- If  $\log \sec x = \frac{1}{2} \cdot x^2 + A \cdot x^4 + B \cdot x^6 + \cdots$ , find A and B.
- ₽ Prove that  $\beta(m, n) = \beta(m + 1, n) + \beta(m, n + 1)$ .
- ? Evaluate  $\int_0^1 \int_0^{x^2} e^{y/x} dy dx$ .
- Solve the Differential Equation  $\frac{dy}{dx} + y = 1$ .
- ≤. Define Fuzzy subset of a set
- Reduce the Matrix A to its normal form. Hence find the

where 
$$A = \begin{bmatrix} 2 & 1 & -3 & -6 \\ 3 & -3 & 1 & 2 \\ 1 & 1 & 1 & 2 \end{bmatrix}$$
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#### (SECTION -B)

## 2. Long Answer Type Questions (Attempt Any Four) [4x10=40]

- Expand  $\log(1 + e^x)$  in ascending power of x as far as the term containing x4
- =: Prove that:  $\lceil n \rceil \rceil - n = \frac{\pi}{\sin n\pi}$  when 0 < n < 1.
- Ξi Evaluate  $\int_{0}^{1} \int_{0}^{1-x} \int_{0}^{1-x-y} xyz \ dz \ dy \ dx$ .
- ₹. Solve  $\frac{d^2y}{dx^2} + 3\frac{dy}{dx} + 2y = 4\cos^2 x$ .
- Verify Cayley-Hamilton theorem of the Matrix A =

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$$\begin{bmatrix} 2 & -1 & 1 \\ -1 & 2 & -1 \\ 1 & -1 & 2 \end{bmatrix}$$
 and hence find  $A^{-1}$ .

Find the Eigen values and Eigen vectors of 
$$A = \begin{bmatrix} 3 & 1 & 4 \\ 0 & 2 & 6 \\ 0 & 0 & 5 \end{bmatrix}$$

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