LNCT UNIVERSITY, BHOPAL

Enrollment No.

CS - 102

B.TECH (CS/AIML) I SEMESTER EXAMINATION [DEC-2024] ADVANCED CALCULUS

Maximum Marks: 70

Time Allowed: 3Hours

Note:- Attempt all questions. Internal choices are given.

(SECTION -A)

Short Answer Type Questions (Attempt Any Five) [5x6=30]

- Verify Lagrange's Mean value Theorem for the function $f(x) = x^3 + x^2 - 6x$ in [-1, 4]
- =: If $\log \sec x = \frac{1}{2} \cdot x^2 + A \cdot x^4 + B \cdot x^6 + \cdots$, find A and B.
- ₽ Prove that $\beta(m, n) = \beta(m+1, n) + \beta(m, n+1)$.
- ? Evaluate $\int_0^1 \int_0^{x^*} e^{y/x} dy dx$.
- Solve the Differential Equation $\frac{dy}{dx} + y = 1$.
- ≦. Define Fuzzy subset of a set
- Rank; Reduce the Matrix A to its normal form. Hence find the

where
$$A = \begin{bmatrix} 2 & 1 & -3 & -6 \\ 3 & -3 & 1 & 2 \\ 1 & 1 & 1 & 2 \end{bmatrix}$$
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Long Answer Type Questions (Attempt Any Four) [4x10=40]

- Expand $log(1 + e^x)$ in ascending power of x as far as the term containing x4
- =: Prove that: $\lceil n \rceil \rceil - n = \frac{\pi}{\sin n\pi}$ when 0 < n < 1.
- ₽ Evaluate $\int_0^1 \int_0^{1-x} \int_0^{1-x-y} xyz \, dz \, dy \, dx$.
- Solve $\frac{d^2y}{dx^2} + 3\frac{dy}{dx} + 2y = 4\cos^2 x$.
- Verify Cayley-Hamilton theorem of the Matrix A =

$$\begin{bmatrix} 2 & -1 & 1 \\ -1 & 2 & -1 \\ 1 & -1 & 2 \end{bmatrix} and hence find A^{-1}.$$

Find the Eigen values and Eigen vectors of $A = \begin{bmatrix} 0 \\ 0 \end{bmatrix}$

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