

# Hierarchical Clustering

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## Hierarchical Clustering

More info at: [https://uc-r.github.io/hc\\_clustering](https://uc-r.github.io/hc_clustering)

```
#setwd("/Users/Rahul/Documents/Rahul Office/IIMB/Concepts/R/ML_using_R/R_code/R_clustering")
knitr::opts_knit$set(root.dir = "/Users/Rahul/Documents/Rahul Office/IIMB/Concepts/R/ML_using_R/R_code/
```

## Preparing Data

Read data from a specified location

```
beer_df = read.csv('./data/Hclust_Beer.csv', header = TRUE, sep = ",",
                  na.strings = c("", " ", "NA"), row.names = c(2))
```

```
beer_df = beer_df[, -c(1)]
```

```
head(beer_df)
```

```
##           CAL SOD  ALC  COST
## Budweiser  144  15  4.7  0.43
## Schlitz    151  19  4.9  0.43
## Lowenbrau  157  15  4.9  0.48
## Kronenbourg 170   7  5.2  0.73
## Heineken   152  11  5.0  0.77
## Old Mil    145  23  4.6  0.28
```

## Summary of the data

Summary of the data on which model is built and Standardizing the variables

```
str(beer_df)
```

```
## 'data.frame':   20 obs. of  4 variables:
## $ CAL : int  144 151 157 170 152 145 175 149 99 113 ...
## $ SOD : int  15 19 15 7 11 23 24 27 10 8 ...
## $ ALC : num  4.7 4.9 4.9 5.2 5 4.6 5.5 4.7 4.3 3.7 ...
## $ COST: num  0.43 0.43 0.48 0.73 0.77 0.28 0.4 0.42 0.43 0.44 ...
```

```
beer_df = na.omit(beer_df)
```

```
beer_scaled = scale(beer_df[, c(1:4)])
```

## Hierarchical clustering - agnes package

Using euclidean as distance measure for hierarchical clustering. Note that if using `hclust()`, the distance matrix returned by `dist()` is used.

```
#beer_dist = dist(beer_scaled, method = "euclidean") # distance matrix
```

With the `agnes` package we can also get the agglomerative coefficient, which measures the amount of clustering structure found (values closer to 1 suggest strong clustering structure)

```
m = c( "average", "single", "complete", "ward")
names(m) = c( "average", "single", "complete", "ward")
```

```
# function to compute coefficient
ac = function(x) {
  agnes(beer_scaled, method = x)$ac
}
```

```
map_dbl(m, ac)
```

```
##   average   single  complete    ward
## 0.7660820 0.5930611 0.8328273 0.8767939
```

On this data set, Ward's method identifies the strongest clustering structure of the four methods assessed. Thus applying ward method for further evaluation.

## Dendrogram Plot

Plot using dendrogram plot to visualize the clusters. In the dendrogram, each leaf corresponds to one observation. As we move up the tree, observations that are similar to each other are combined into branches, which are themselves fused at a higher height.

The height of the fusion, provided on the vertical axis, indicates the (dis)similarity between two observations. The higher the height of the fusion, the less similar the observations are. Note that, conclusions about the proximity of two observations can be drawn only based on the height where branches containing those two observations first are fused. We cannot use the proximity of two observations along the horizontal axis as a criteria of their similarity.

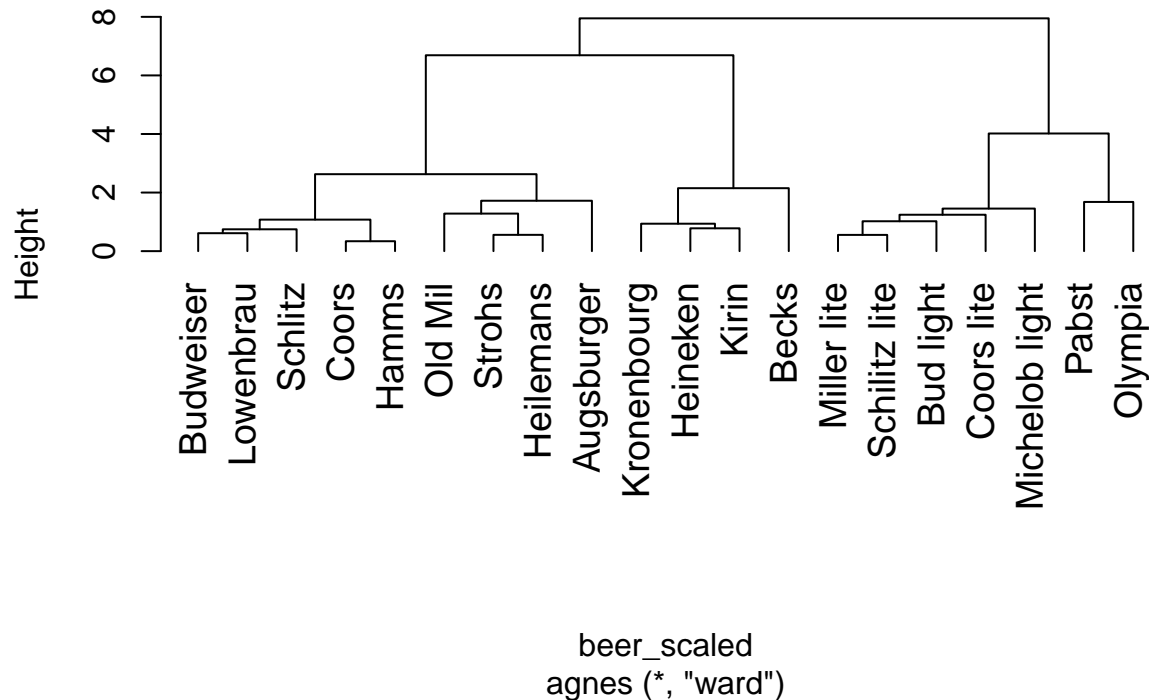
<https://stats.stackexchange.com/questions/109949/what-algorithm-does-ward-d-in-hclust-implement-if-it-is-not-wards-criterion>

Note that `agnes(, method="ward")` corresponds to `hclust(, "ward.D2")`. More at `?hclust`.

```
options(repr.plot.width=15, repr.plot.height=10)
```

```
beer_hclust1 = agnes(beer_scaled, method = "ward")
pltree(beer_hclust1, cex = 1.2, hang = -1, main = "Dendrogram based on Ward Linkage")
```

## Dendrogram based on Ward Linkage



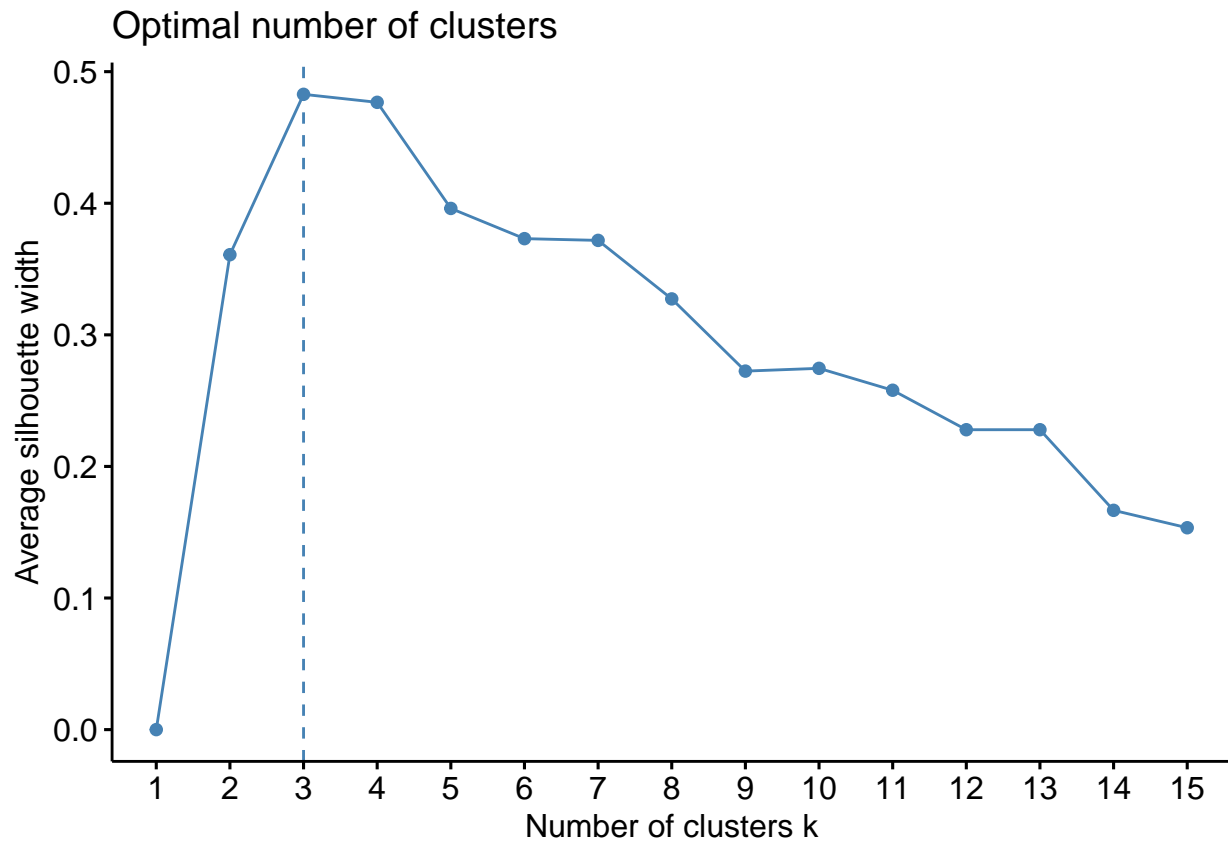
The height of the cut to the dendrogram controls the number of clusters obtained. It plays the same role as the  $k$  in  $k$ -means clustering. To identify the optimal  $k$ , we can use average silhouette width or wss as metric.

### Optimal cluster - Average Silhouette width

Using average silhouette width as the metric, the optimal number of clusters  $k$  is the one that maximizes the average silhouette over a range of possible values for  $k$ .

The results show that 2 clusters maximize the average silhouette values with 3 clusters coming in as second optimal number of clusters.

```
fviz_nbclust(beer_scaled, FUNcluster = hcut, hc_func = "agnes", hc_method = "ward.D2", hc_metric = "euclidean",
             method = "silhouette", k=15)
```

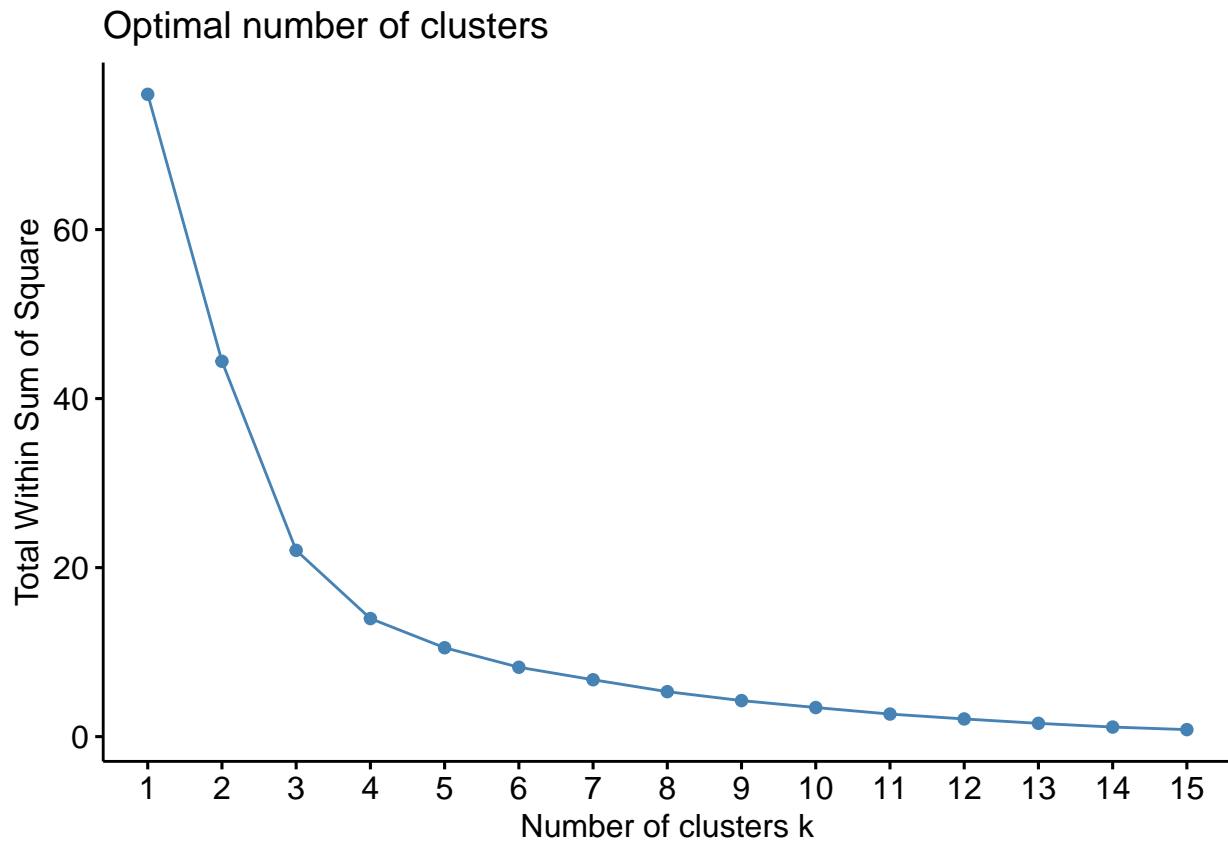


### Optimal Cluster - Elbow method (wss)

The total within-cluster sum of square (wss) measures the compactness of the clustering and we want it to be as small as possible. The location of a bend (knee) in the plot is generally considered as an indicator of the appropriate number of clusters.

Result shows  $k = 3$  to be the optimal.

```
fviz_nbclust(beer_scaled, FUNcluster = hcut, hc_func = "agnes", hc_method =  
             "ward.D2", hc_metric = "euclidean", method = "wss", k=15)
```



In order to identify sub-groups (i.e. clusters), we can cut the dendrogram with `cutree`. We will set  $k = 3$

```
# Ward's method
# beer_hclust = hclust(beer_dist, method = "ward.D2" )
k = 3
beer_hclust2 = as.hclust(agnes(beer_scaled, method = "ward"))
#cutree((beer_hclust2), k = k)

# Cut tree into 4 groups
sub_grp = cutree(beer_hclust2, k = k)

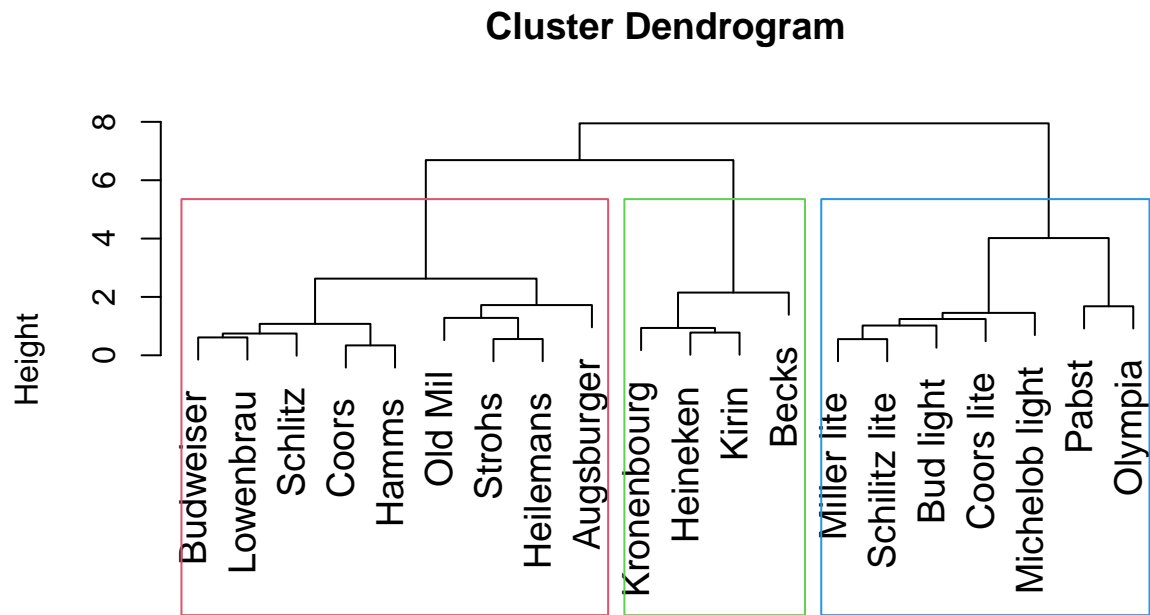
# Number of members in each cluster
table(sub_grp)

## sub_grp
## 1 2 3
## 9 4 7
```

## Visualize cluster

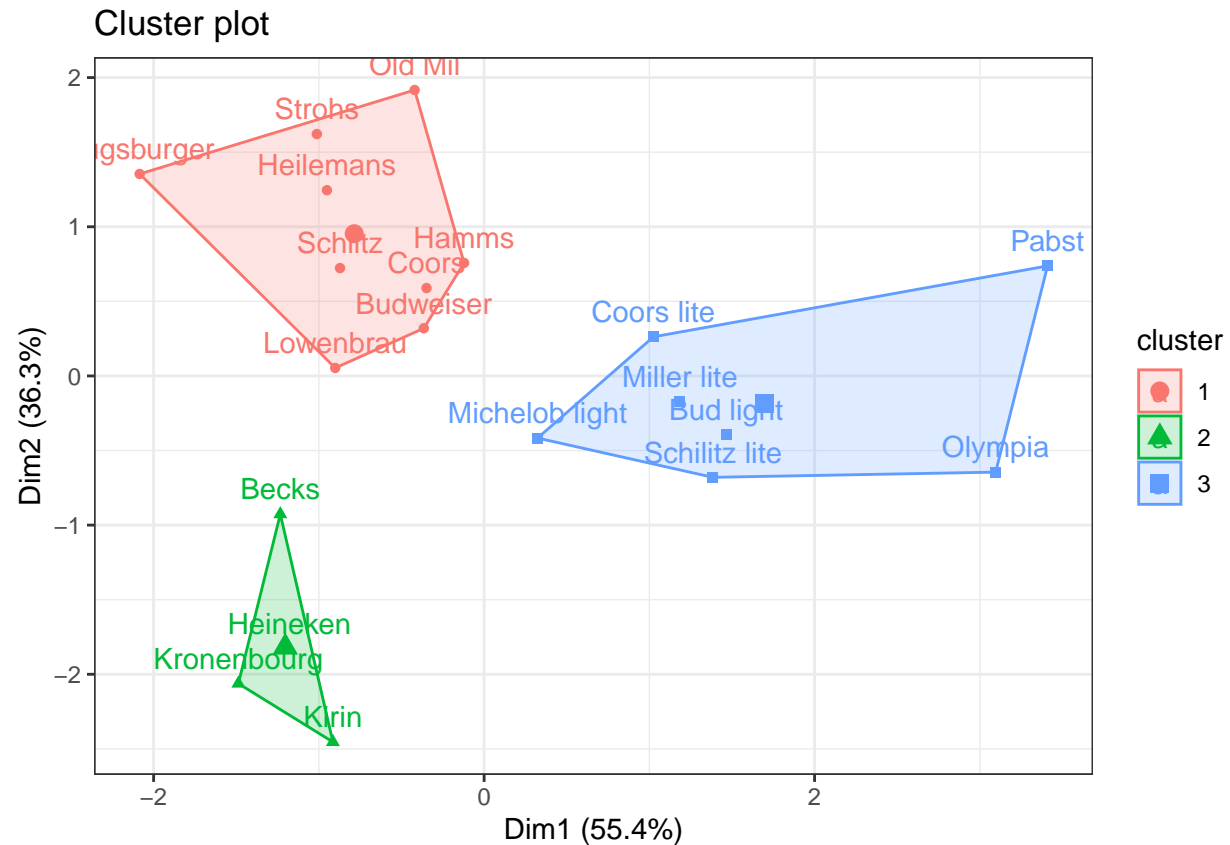
We can visualize the cluster as below:

```
plot(beer_hclust2, cex = 1.2)
rect.hclust(beer_hclust2, border = 2:4, cluster = sub_grp, k=k)
```



beer\_scaled  
agnes (\*, "ward")

```
fviz_cluster(list(data = beer_scaled, cluster = sub_grp)) +  
theme_bw()
```



The cluster can be tagged to the original dataframe as below:

```
beer_df %>%
mutate(cluster = sub_grp, name = row.names(beer_df)) %>%
head(10)
```

##	CAL	SOD	ALC	COST	cluster	name
## 1	144	15	4.7	0.43	1	Budweiser
## 2	151	19	4.9	0.43	1	Schlitz
## 3	157	15	4.9	0.48	1	Lowenbrau
## 4	170	7	5.2	0.73	2	Kronenbourg
## 5	152	11	5.0	0.77	2	Heineken
## 6	145	23	4.6	0.28	1	Old Mil
## 7	175	24	5.5	0.40	1	Augsburger
## 8	149	27	4.7	0.42	1	Strohs
## 9	99	10	4.3	0.43	3	Miller lite
## 10	113	8	3.7	0.44	3	Bud light

```
beer_df %>%
mutate(cluster = sub_grp, name = row.names(beer_df)) %>%
write.csv("beer_hirarchial_output.csv")
```