

Linear Regression \rightarrow

math

eg. $\underbrace{\text{weight}, \text{gender}}_{x} - \dots$ height $\underbrace{\text{?}}_{y}$

x	y
1	2
2	3

$$D = \langle x_i, y_i \rangle$$

\Leftrightarrow Linear Regression

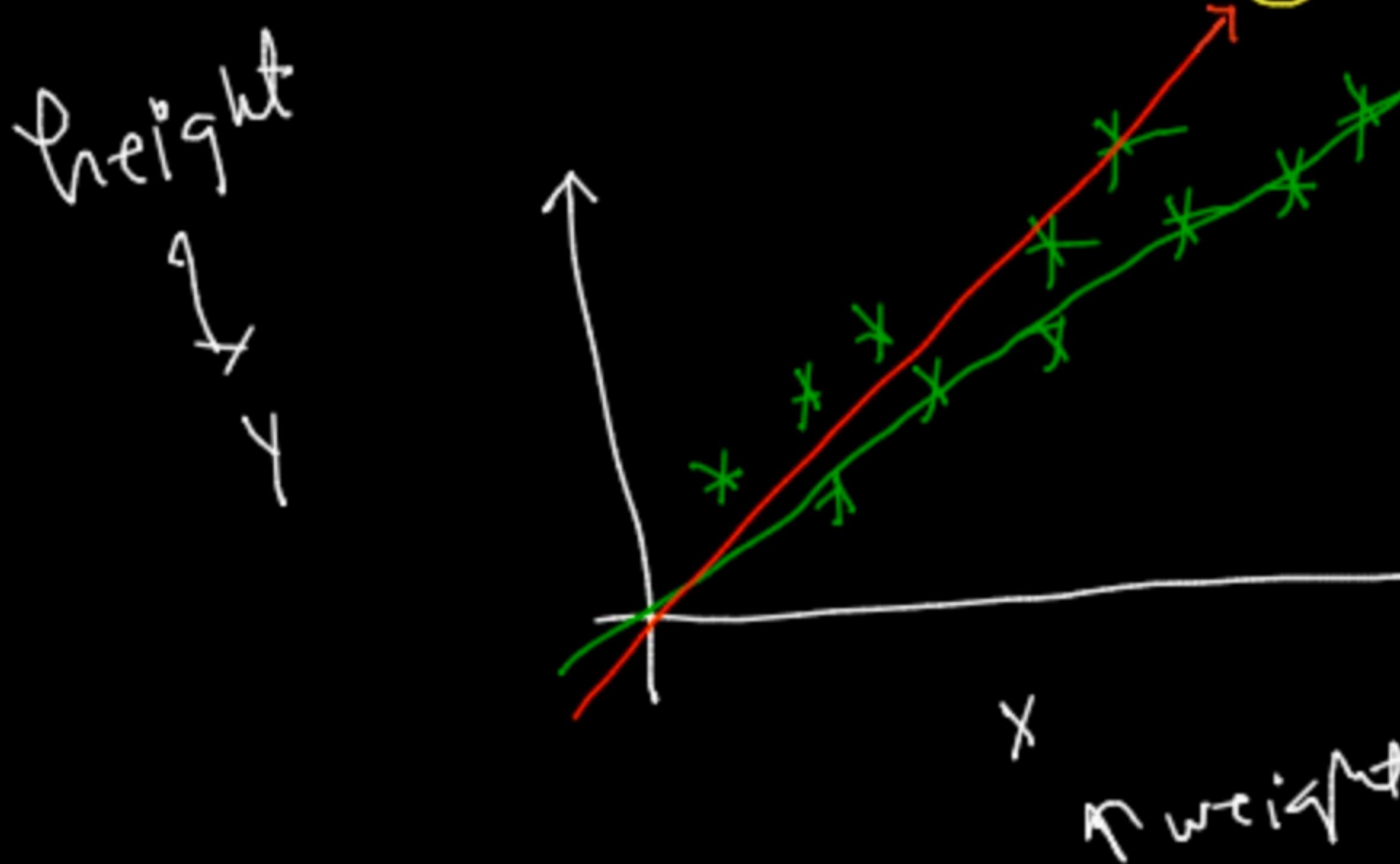
[RD]

$$x \in \mathbb{R}^d$$

$$y_i \in \text{Real}$$

\rightarrow find a line that fits the given data

i.e. $f_h = w_1 * \text{weight} + b_0$



$$(l_1, l_2) \rightarrow \begin{array}{|c|c|} \hline w_1 & b_0 \\ \hline \end{array}$$

\downarrow

(Best)

min error

3D



plane

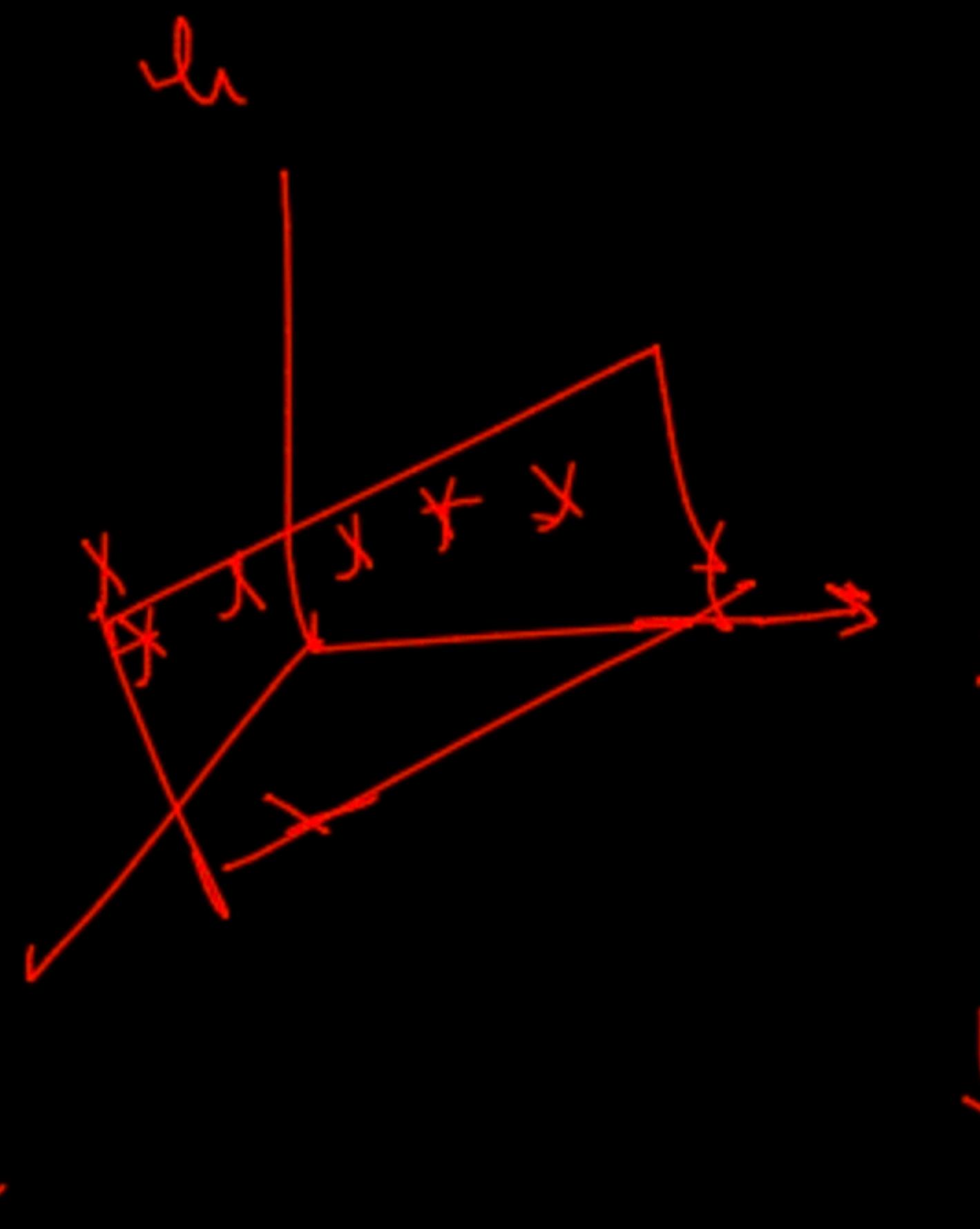


Best \rightarrow

n plane



Best $\rightarrow \min \text{error}$



our objective

{ find a plane | line (hyperplane) \rightarrow Best fit

+ data \downarrow

$$\min_{\mathbf{w}} \sum_{i=1}^n \text{error}_i$$

$$y_i = w_1 f_1 + w_2 f_2 + w_0 \quad (\min \text{error})$$

i.e.

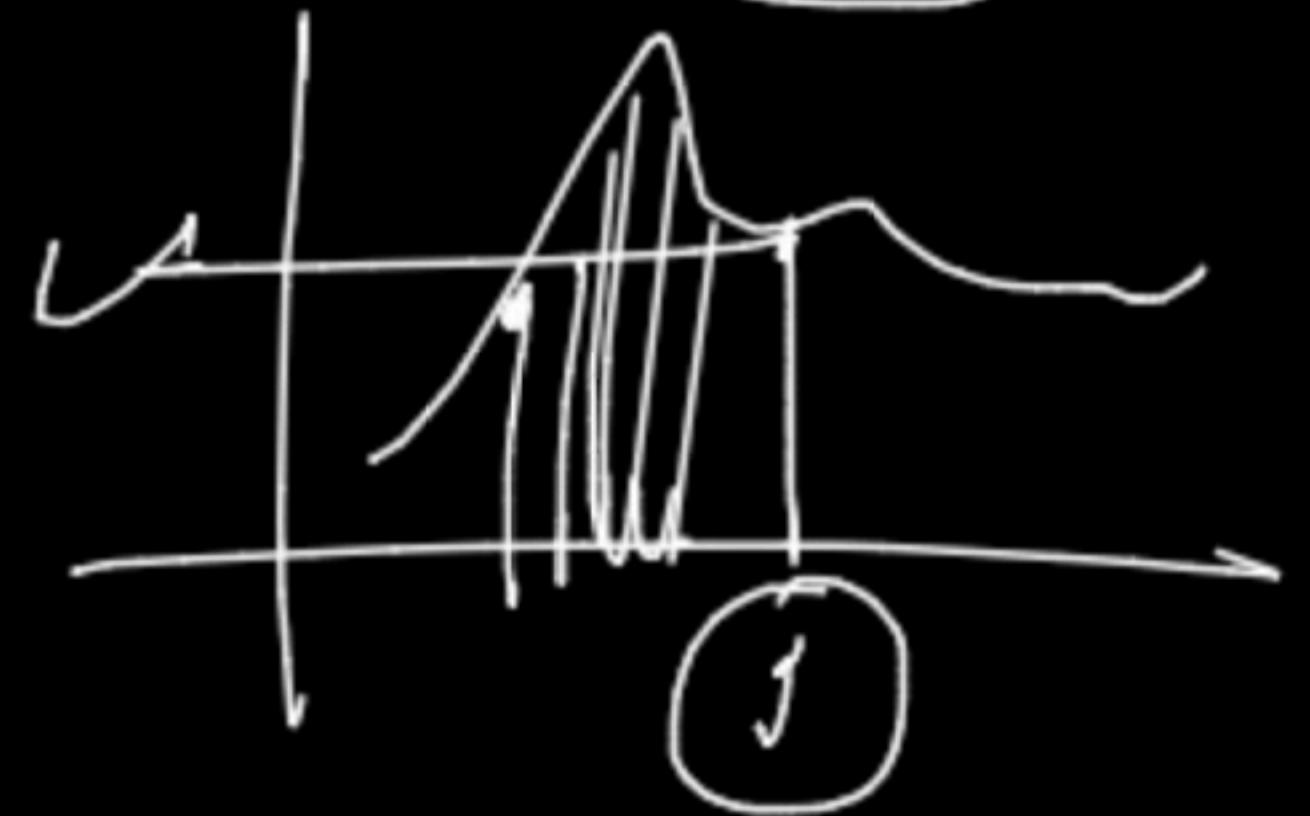
ND \rightarrow LR \rightarrow Hyperplane

$$\min \rightarrow (y - \hat{y}) \downarrow$$

$$\Rightarrow \boxed{y_i = \mathbf{w}^T \cdot \mathbf{x}_i + w_0} \quad \mathbf{x} \in \mathbb{R}^d$$

$$(y - \hat{y})$$

SAP



QJ

Outliers

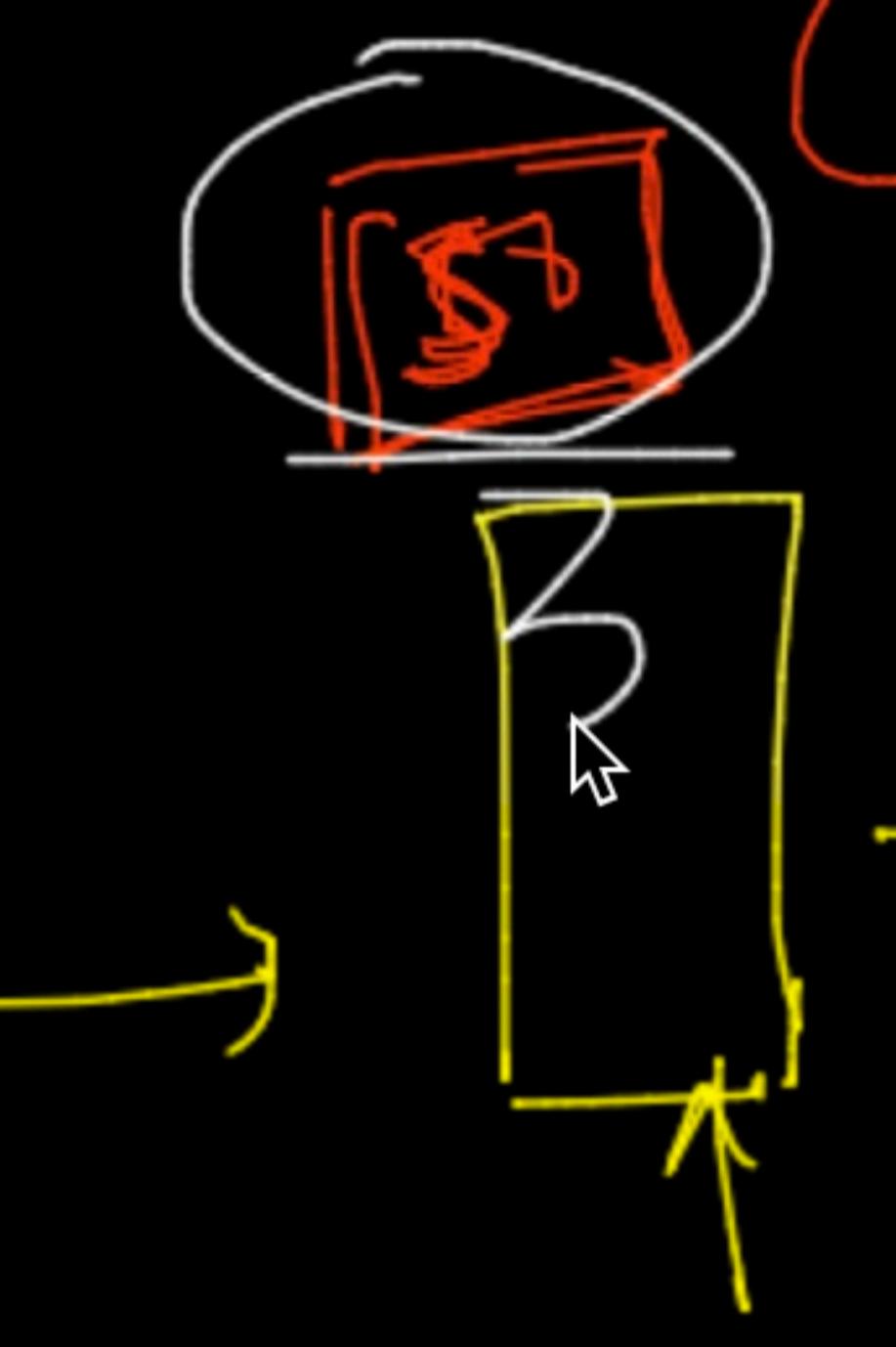
X	Y	
x_1	150	t_1
x_2	155	t_2
x_3	115	t_3

errors

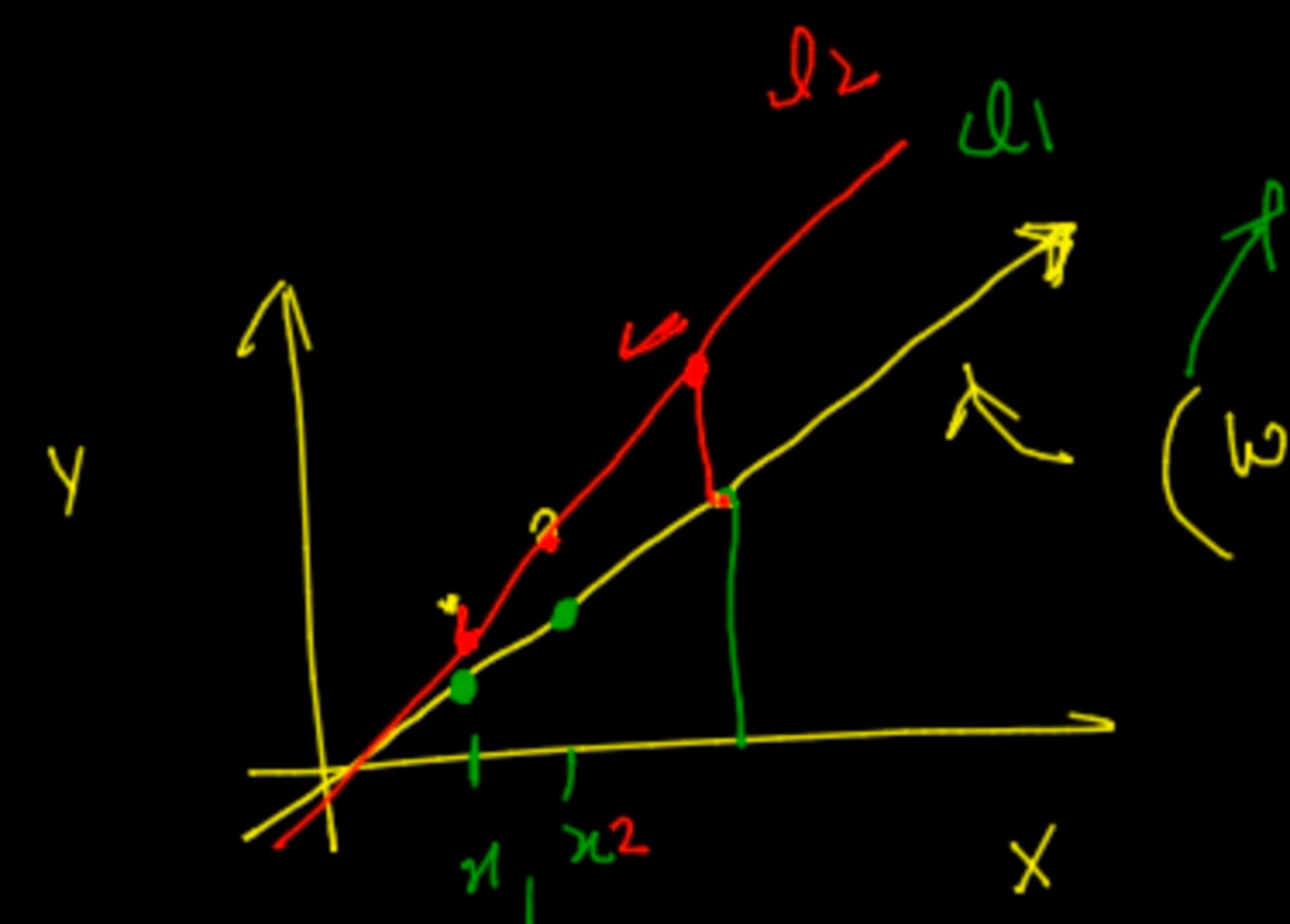
$(-5)^2$

$(+1)^2$

$(-10)^2$



(x_1, y)



$$y = w_1 x_1 + w_0$$

$$|w_1 = 0.1|$$

$$(w_1, w_0)$$

$$=$$

mode

err

w	0.1	0.5
err	-0.25	0.25

Best

$$(-0.25, -0.8)$$

$$(B_{\text{est}}, f)$$

→ mathematical formulation

2)

$$\underset{w, w_0}{\operatorname{argmin}} \sum_{i=1}^n \left(y_i - (w^T x_i + w_0) \right)^2 + \lambda \|w\|_2^2$$

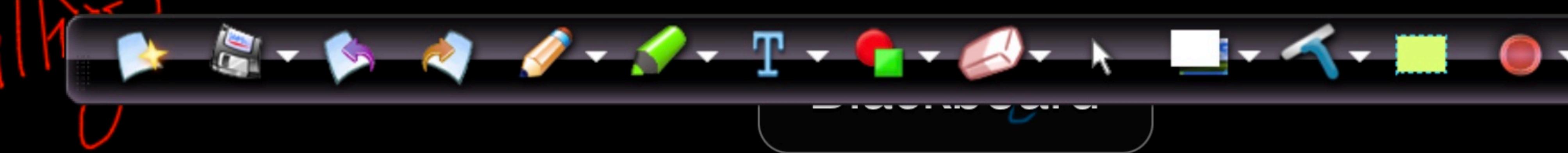
↑
bias
square-loss

log. regression

↓

overfitting

and
underfitting



$\overset{\text{GKreal}}{=} \lambda$

Hypotenuse

$$\boxed{\lambda = 0}$$

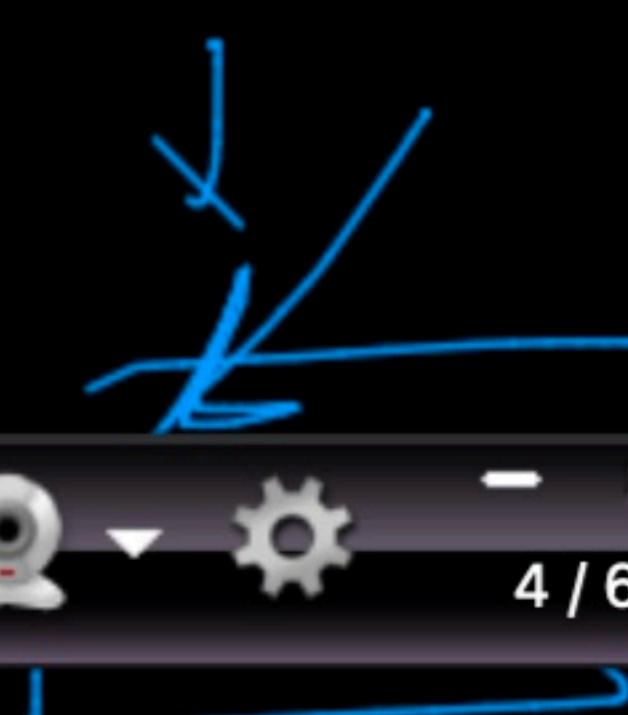


$$\lambda \|w\|_2^2$$

penalty

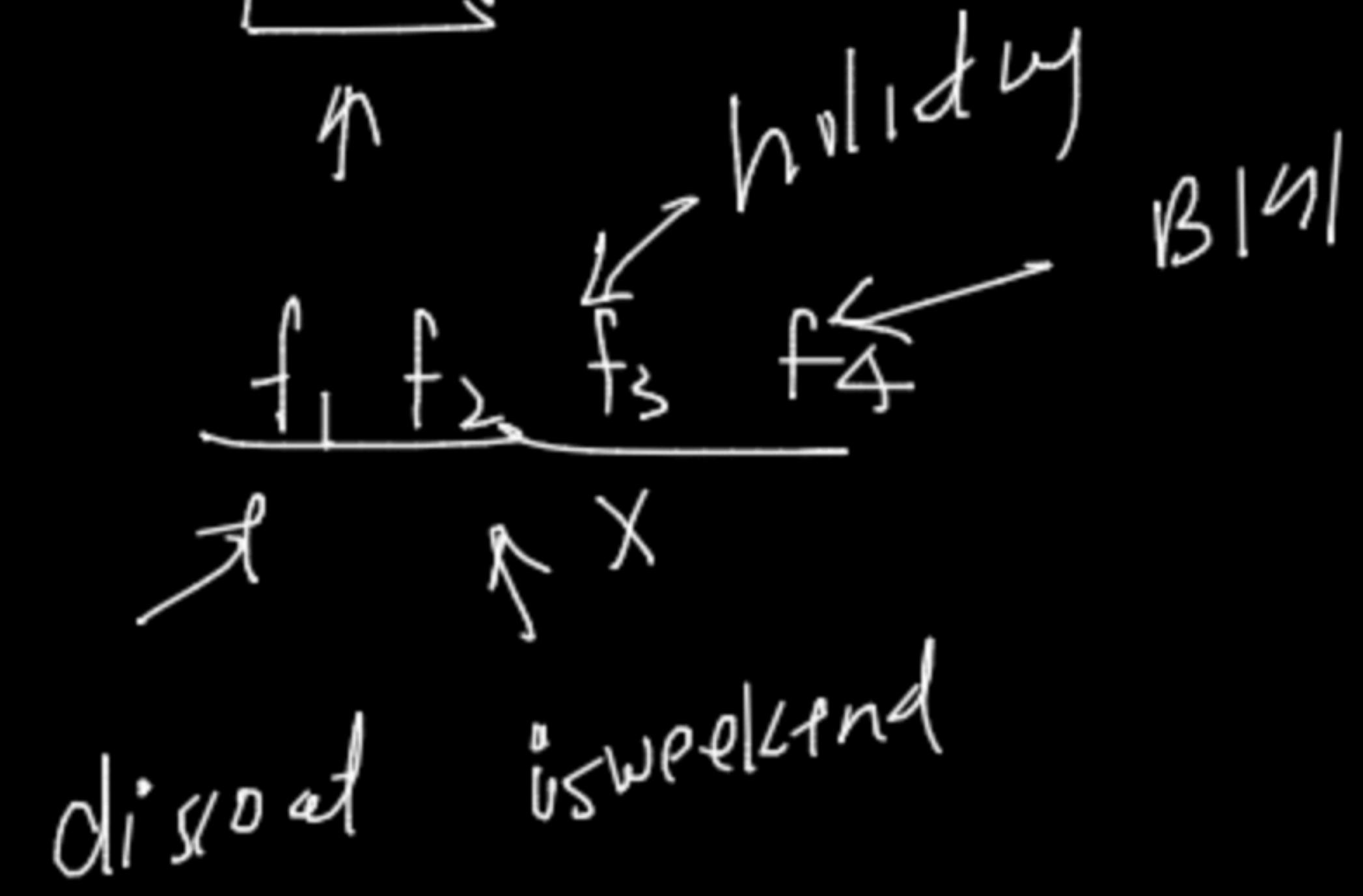


regularization



Retail domain

$\rightarrow [LR]$



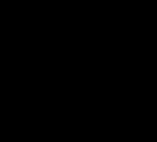
(RFE)



sales

Assign

[FS]



Basic



Lasso Ridge



(LR)



Reasoning $\rightarrow [LR]$

Regression

Log. Regression

(D) $\rightarrow [] \rightarrow \downarrow$

w₁ w₂

'0'

\Rightarrow Cases

Not

① Assumption

\hookrightarrow Data should be linearly separable

② Imbalance \rightarrow [No]

③ Feature Importance

\hookrightarrow —

④ Outliers

$\uparrow \downarrow$