

Classification → Regression

Linear Regression

$(X, Y) \rightarrow \boxed{\phantom{x}} \rightarrow 3, 4, 3$   
↑  
Real  $x$



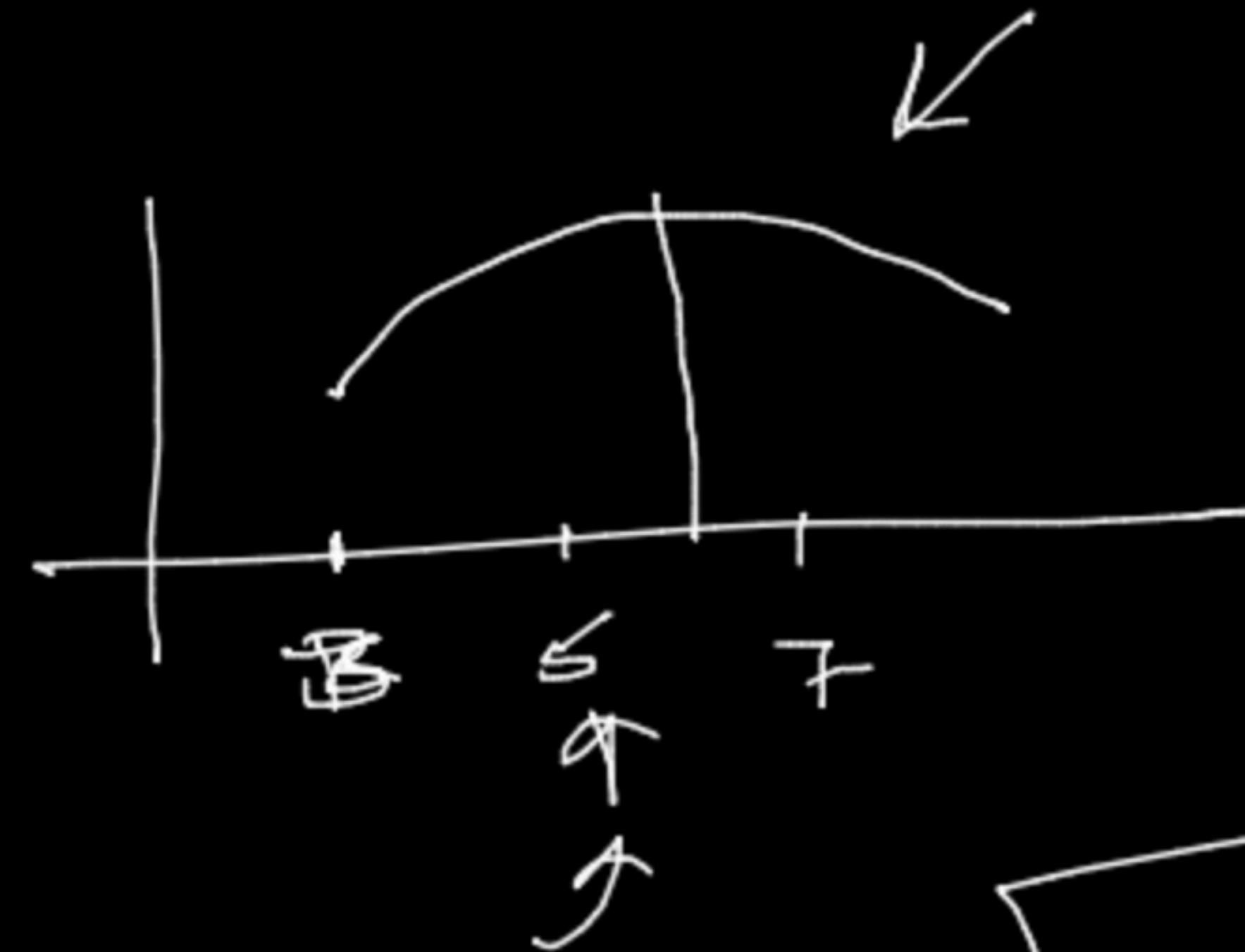
$(3, 2.1)$

KNN →  $(k)$  → Fine tuning

KNN

↓  
Gridsearch  $\rightarrow$  Parameter  
RandomSearch  $\rightarrow$   $\boxed{\phantom{x}}$

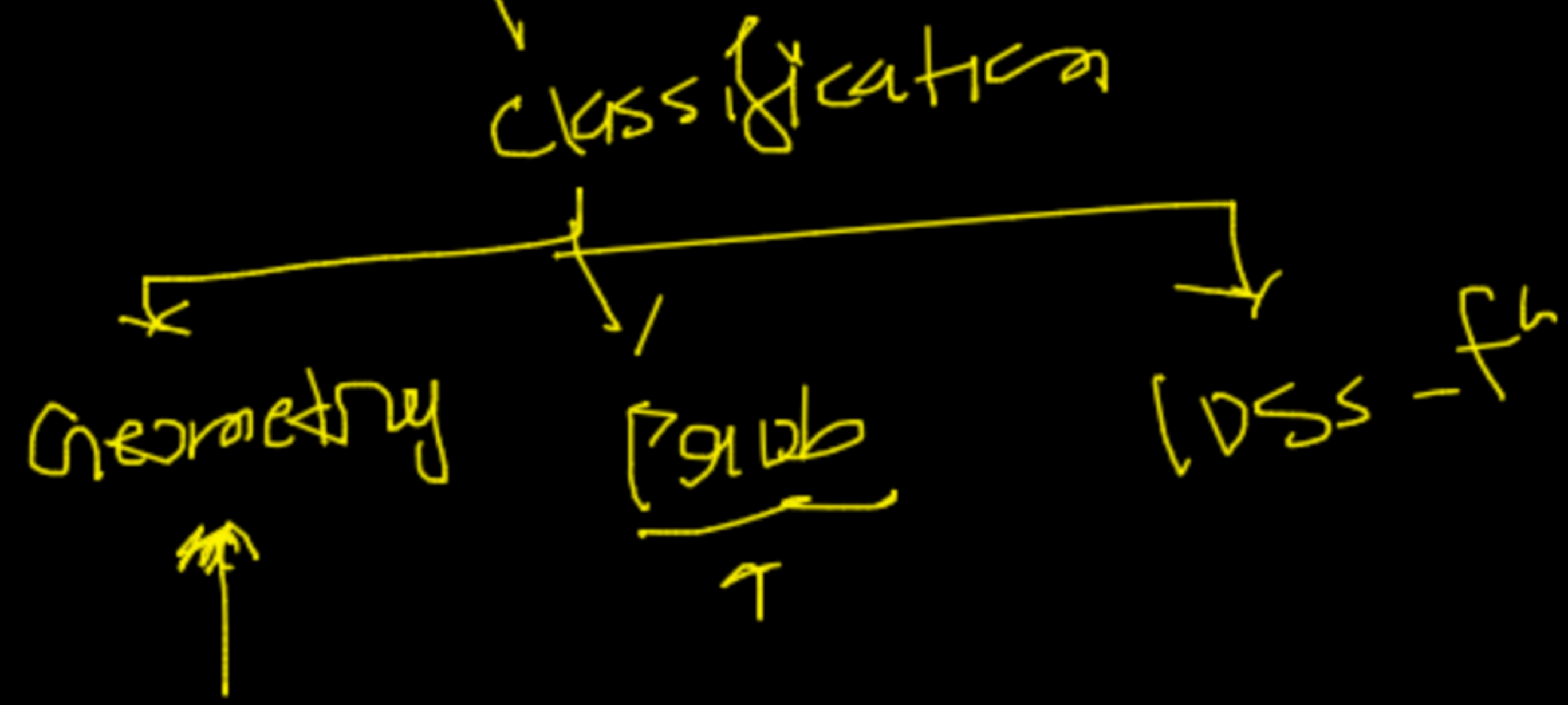
$(f)$   
 $\boxed{k}$  →  $f(x)$



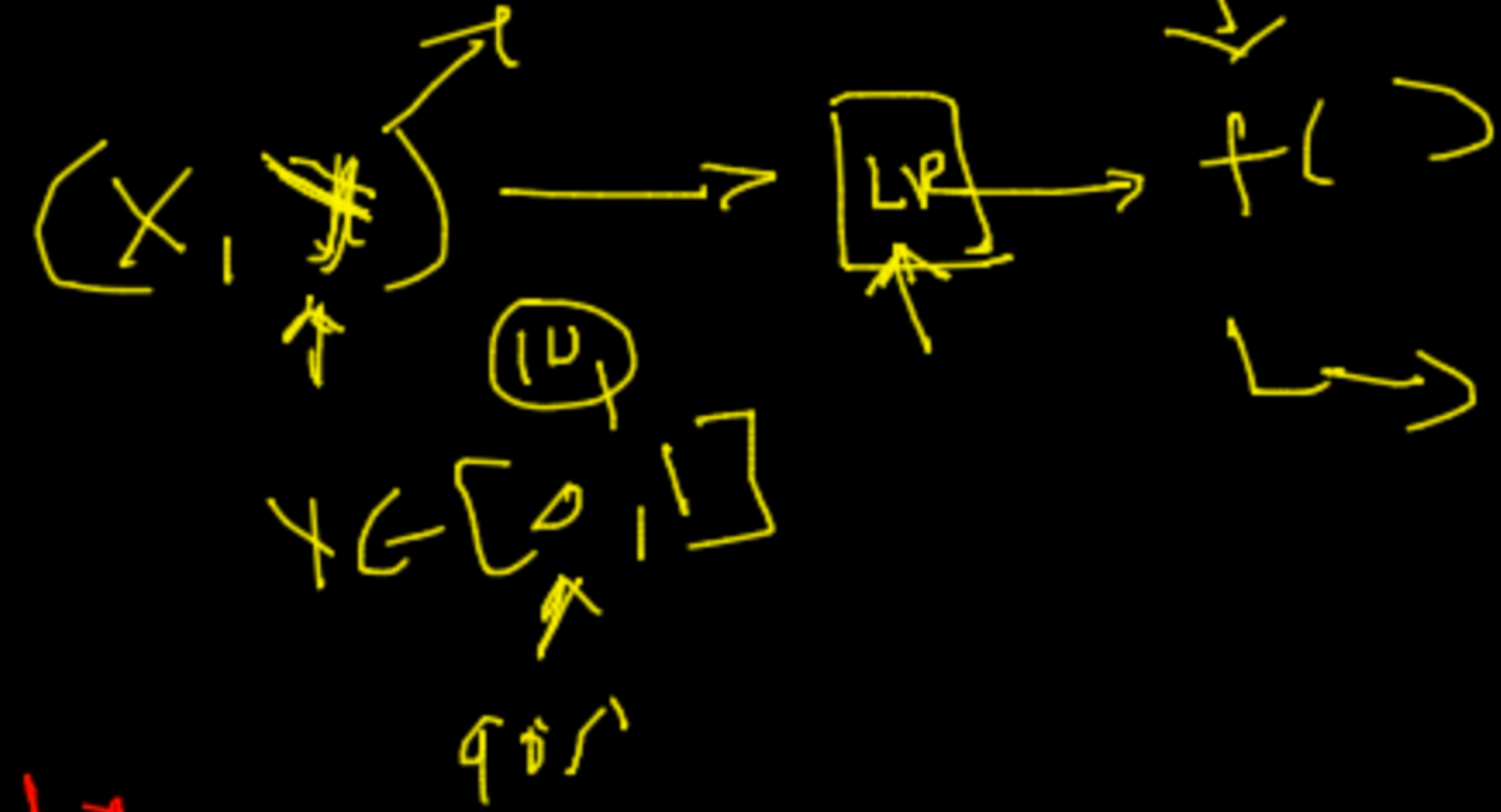
$\hookrightarrow KNN(3) \rightarrow f() \rightarrow 70.1$   
 $\hookrightarrow KNN(5) \rightarrow f() \rightarrow 80.1$



# Logistic Regression



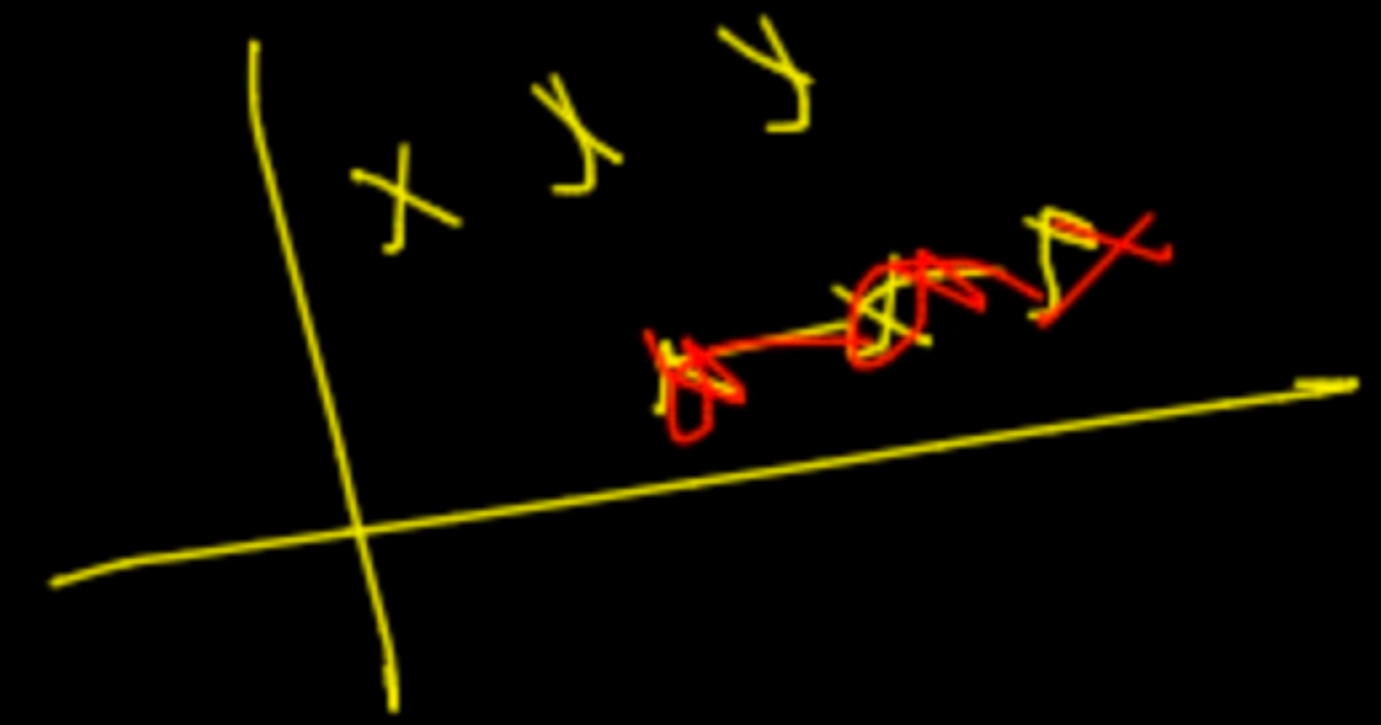
(Data)



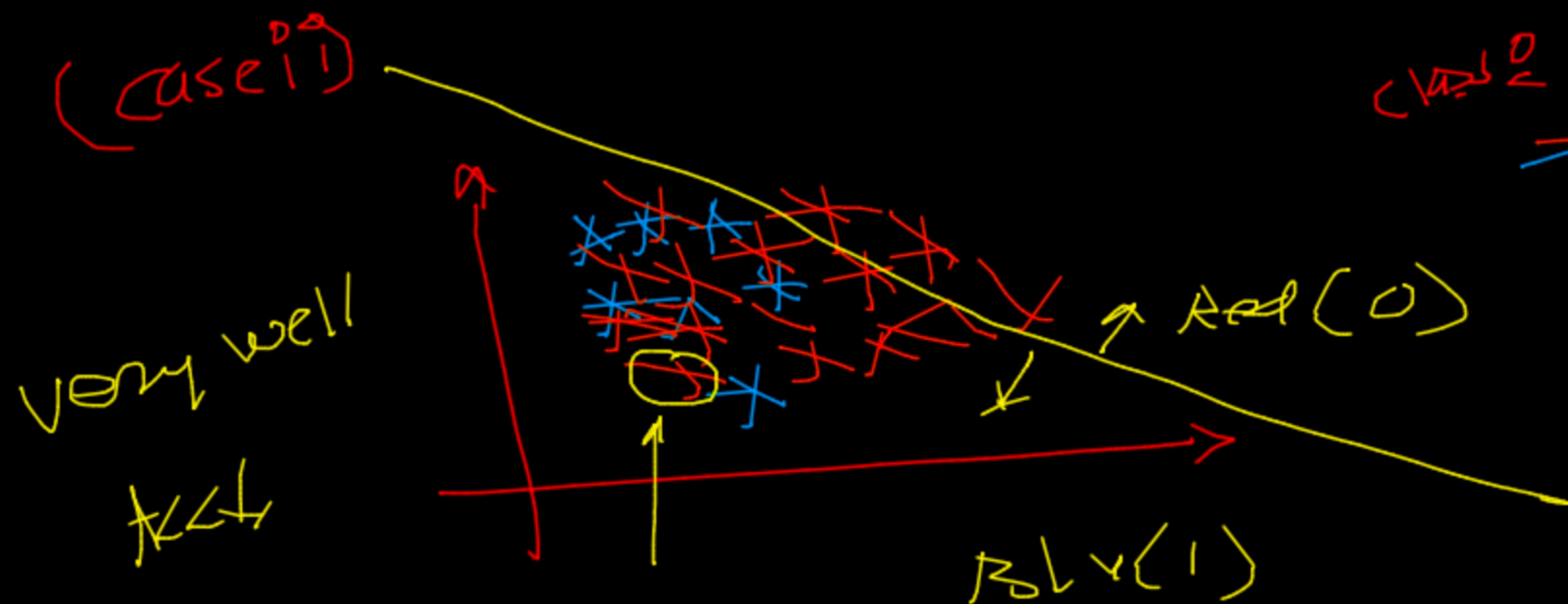
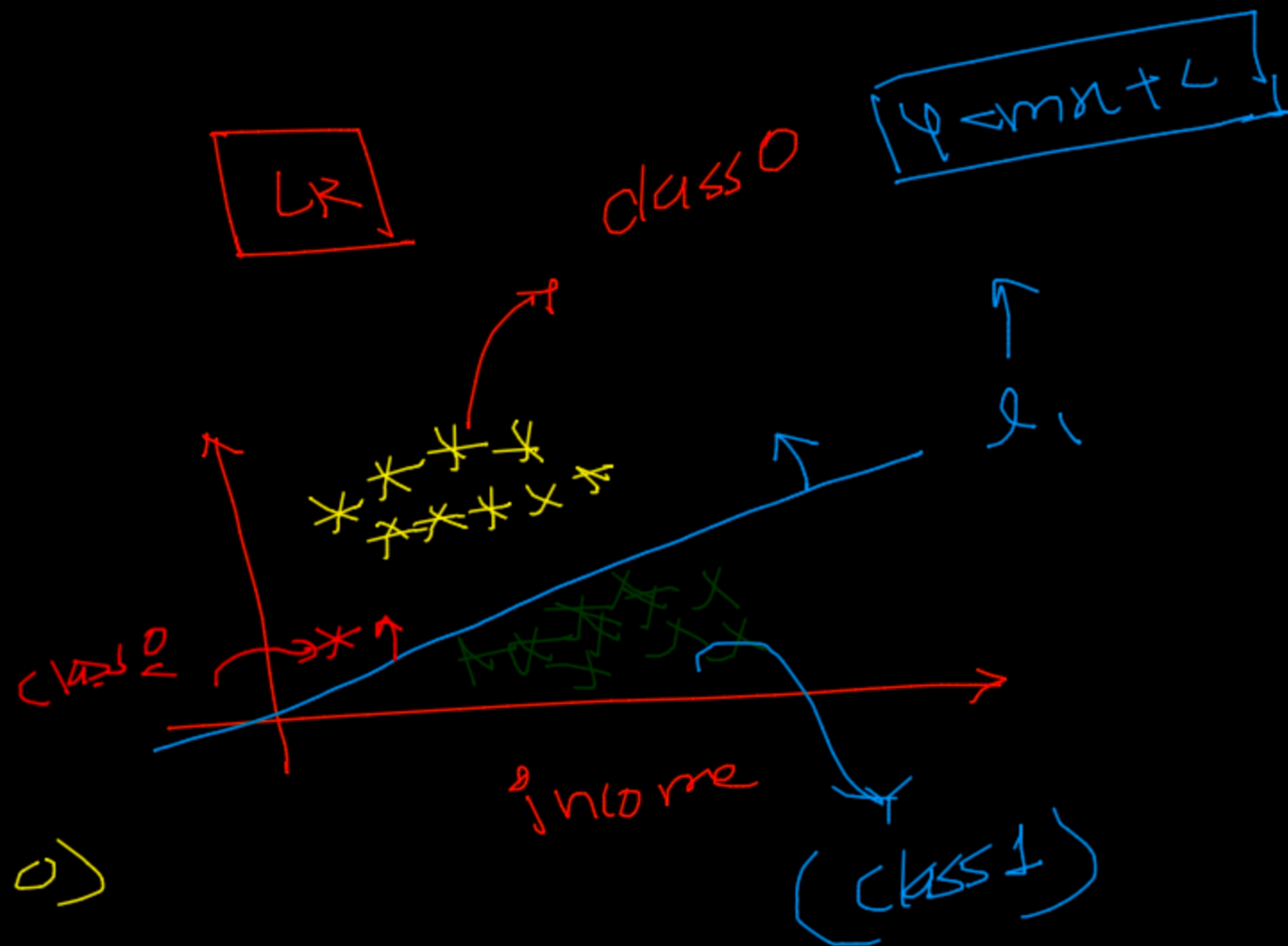
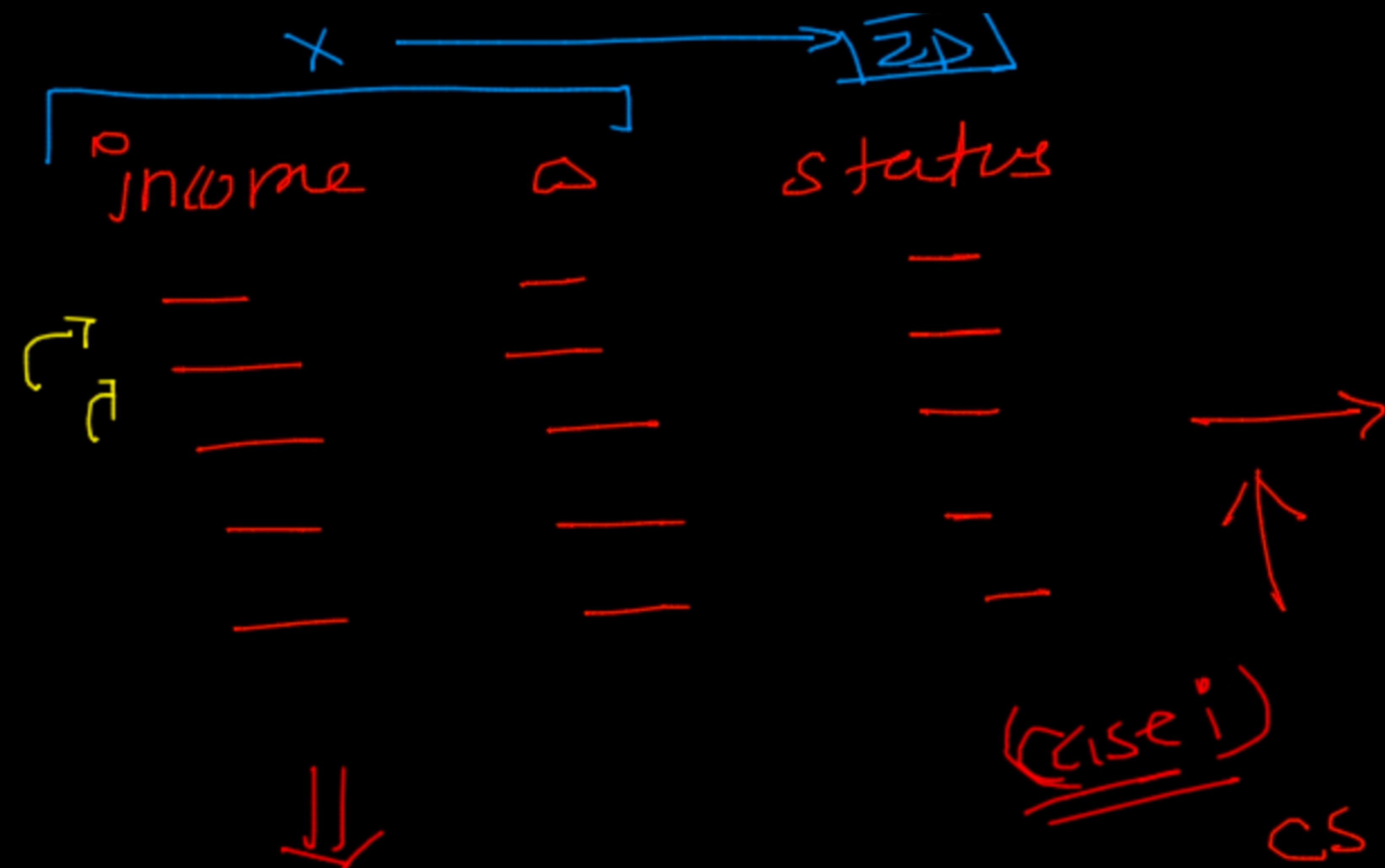
Big Assumption

Classes are almost perfectly

linearly separable







MLL



$D(x)$

no

$[+ve, -ve]$

Best

$\Rightarrow$

plot

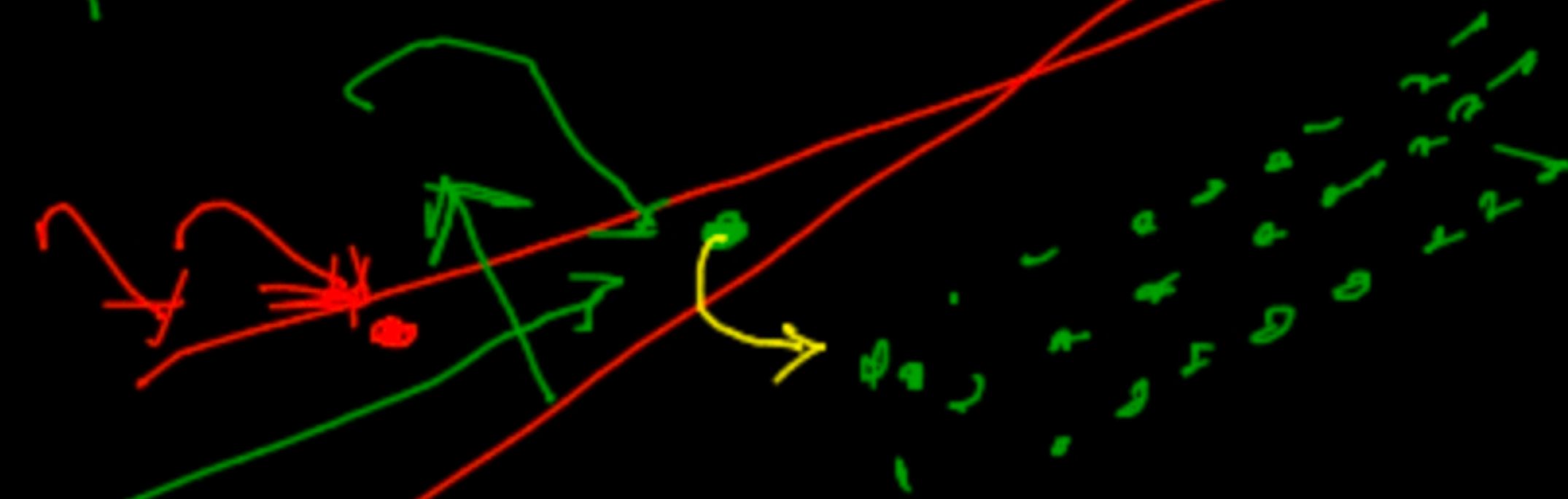
no

class  $\rightarrow$   $(-ve)$   
 $\times \times \times \times \times \times$   
 $\times \times \times \times \times \times$

$\Pi_2$

Best<sup>math</sup>  
 $(\times \times)$

Plane?



'Minimum'

$(\odot \odot \odot)$

Best

km

training 1x

plane for  $\Pi_2$

equation of plane  $\Rightarrow$

$$\Pi = w^T (\odot) + w_0$$

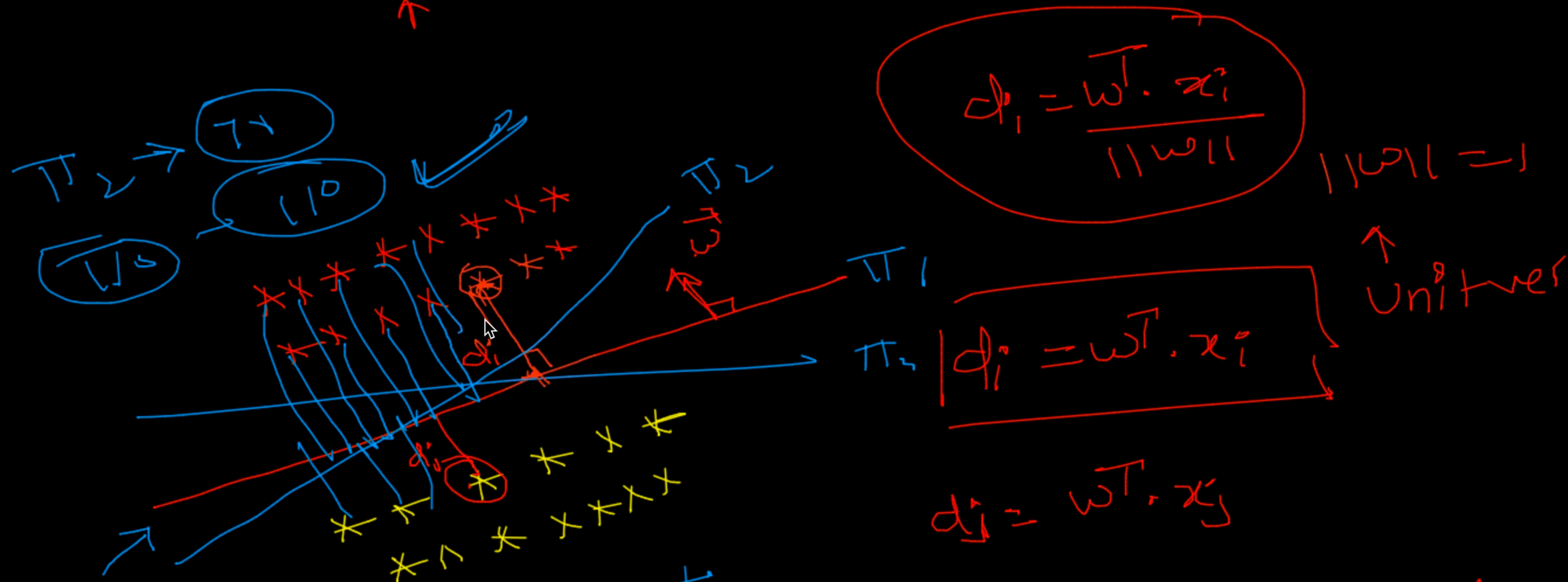
$[w_1, w_2]$   
 $[0.5, 0.3, 0.2]$   
 $w_0 = [0.4]$

(Rule)

$(w^T, w_0)$



Task  $\uparrow$   $\Pi$  Best separated  $\rightarrow$  (true) pts from -w pts



$\Pi_1 \rightarrow$  summation st  $\rightarrow$  (100)

$d_i = w^T x_i > 0$  (same side of normal vector)

$d_i = \underline{w^T \cdot x_i} < 0$  (both on op)



Classification rule

if  $w^T x_i > 0$   
 then  $y_i \rightarrow +1$   
 if  $w^T x_i < 0$   
 then  $y_i \rightarrow -1$

$y_i, w^T x_i$   
 $(+ve) (-ve) \rightarrow (+ve) \rightarrow (+ve)$   
 $\rightarrow$  How to test

correct  $\leftarrow$   $y_i w^T x_i > 0$   
 $(+ve) (-ve) > 0$

$$w \rightarrow [0.5, 0.7]$$

	$x_1$	$x_2$	$y$	
	(-)	(-)	+ve	(+ve)
	(-)	(-)	-ve	(-ve)
	(-)	(-)	+ve	(+ve)

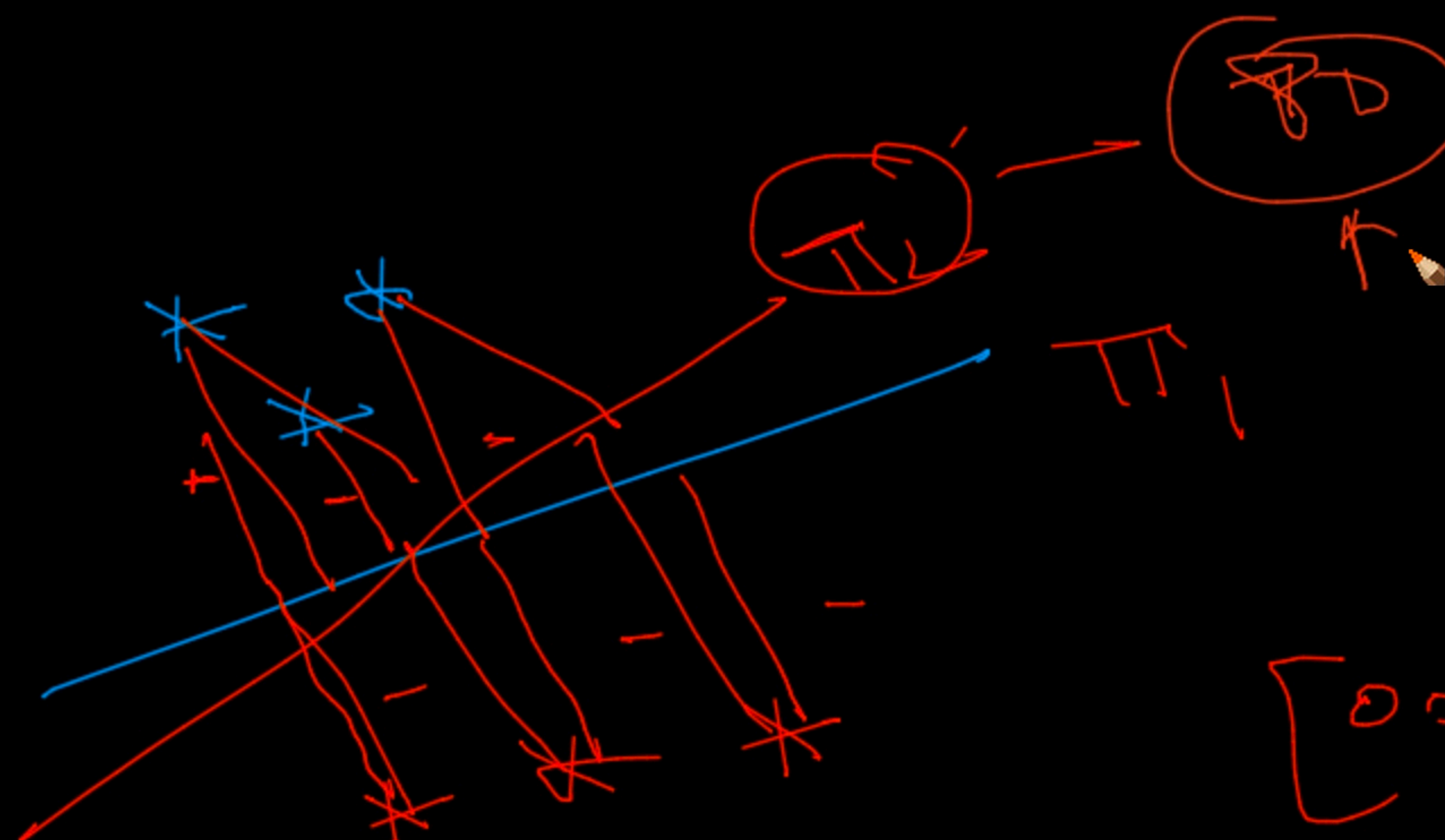
$$\hat{y} = w^T x_i \rightarrow (-ve)$$

$$\leftarrow [0.5, 0.7] \times \begin{bmatrix} 1 \\ 1 \end{bmatrix}$$

$$w^T x_i > 0$$



$y_i w^T x_i > 0$   $\rightarrow$  LR is correctly classified  
pts  $(x_i)$



$[0.5, 0.7]$

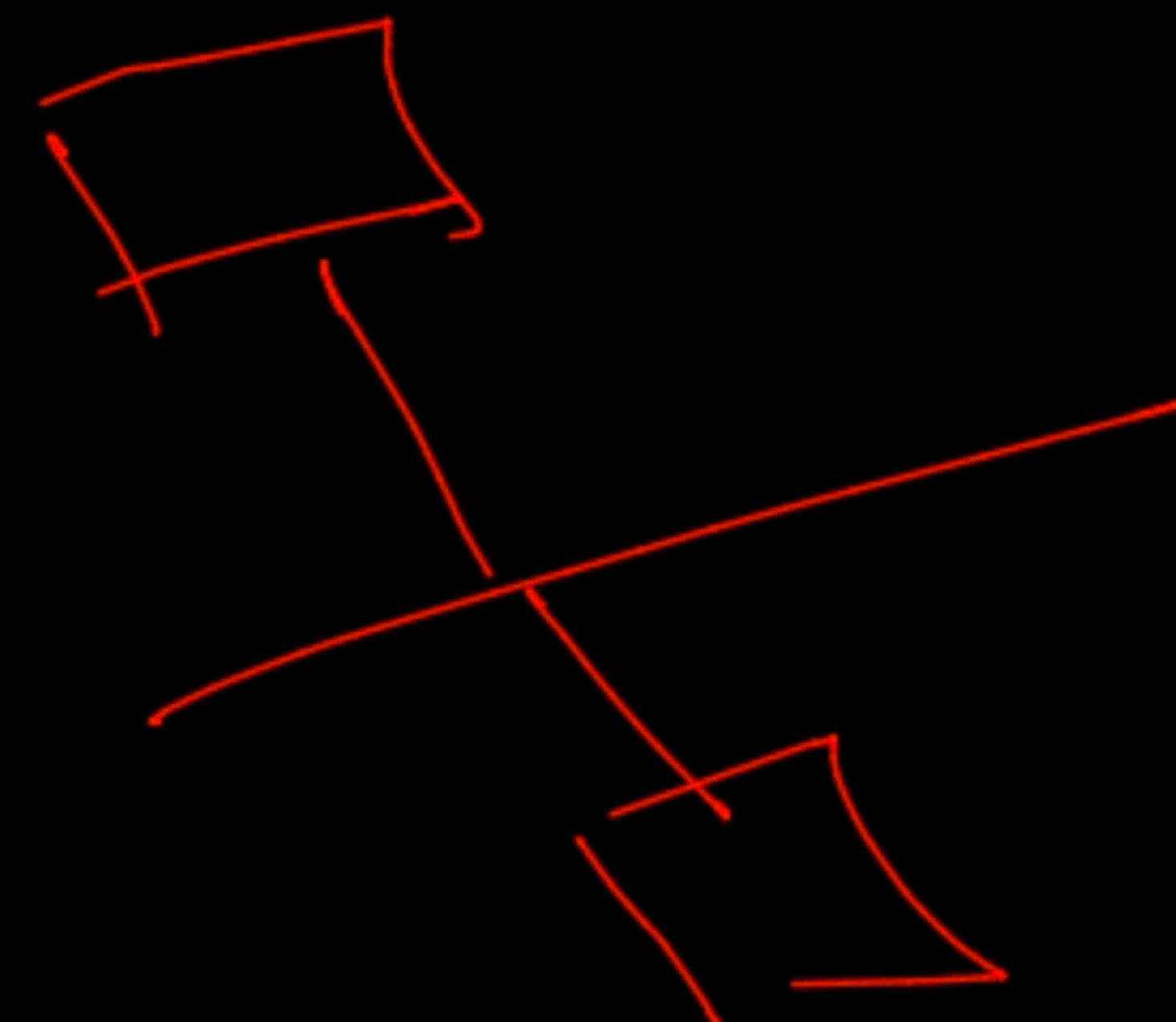
$\rightarrow$   $\Rightarrow$   $\pi_0$





$$\max \sum_{i=1}^n y_i w^T x_i$$

$w^0$  is only  $\rightarrow$  find



$w^*$  which maximizes  $\sum_{i=1}^n y_i w^T x_i$

plot it max optimization



$$\pi_1 \rightarrow [0.5, 0.7] \rightarrow \text{1st}$$

$$\pi_2 \rightarrow [0.1, 0.8] \rightarrow \text{2nd}$$

$$\pi_3 \rightarrow [0.8, -0.4]$$

↑

$$(y_i w^T x_i) + y_i w^T v$$

$$y_i w^T x_i > 0 \rightarrow$$

$y$	$\hat{y}$	$\hat{y}$	$\hat{y}$
1	1	1	1
1	1	1	1
1	1	1	1
1	1	1	1
1	1	1	1
1	1	1	1
1	1	1	1
1	1	1	1
1	1	1	1
1	1	1	1

$w^T x_i$

$$w^T x_i$$

$$w^T x_i$$



$$y = f(x)$$

