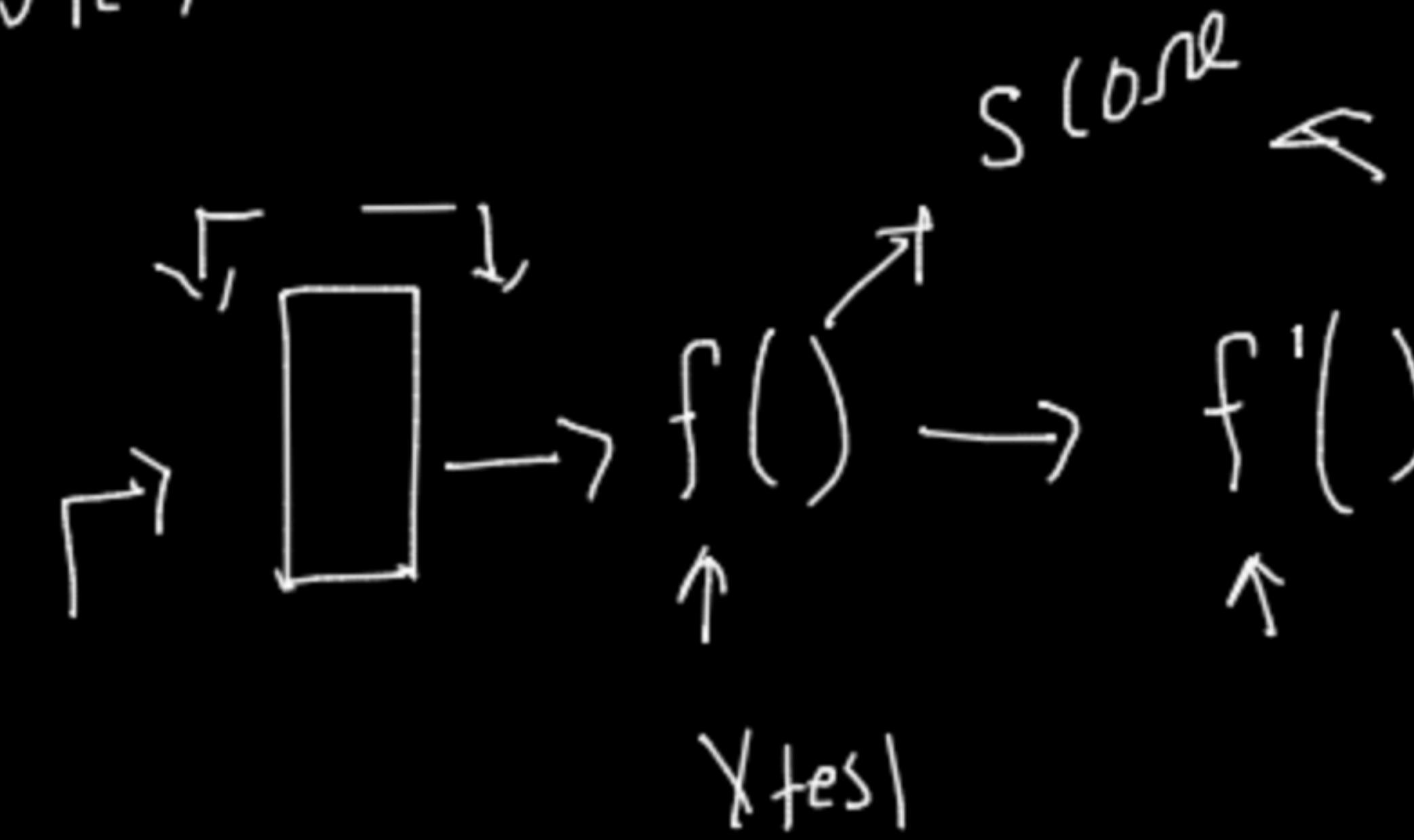


# ROC and AUC

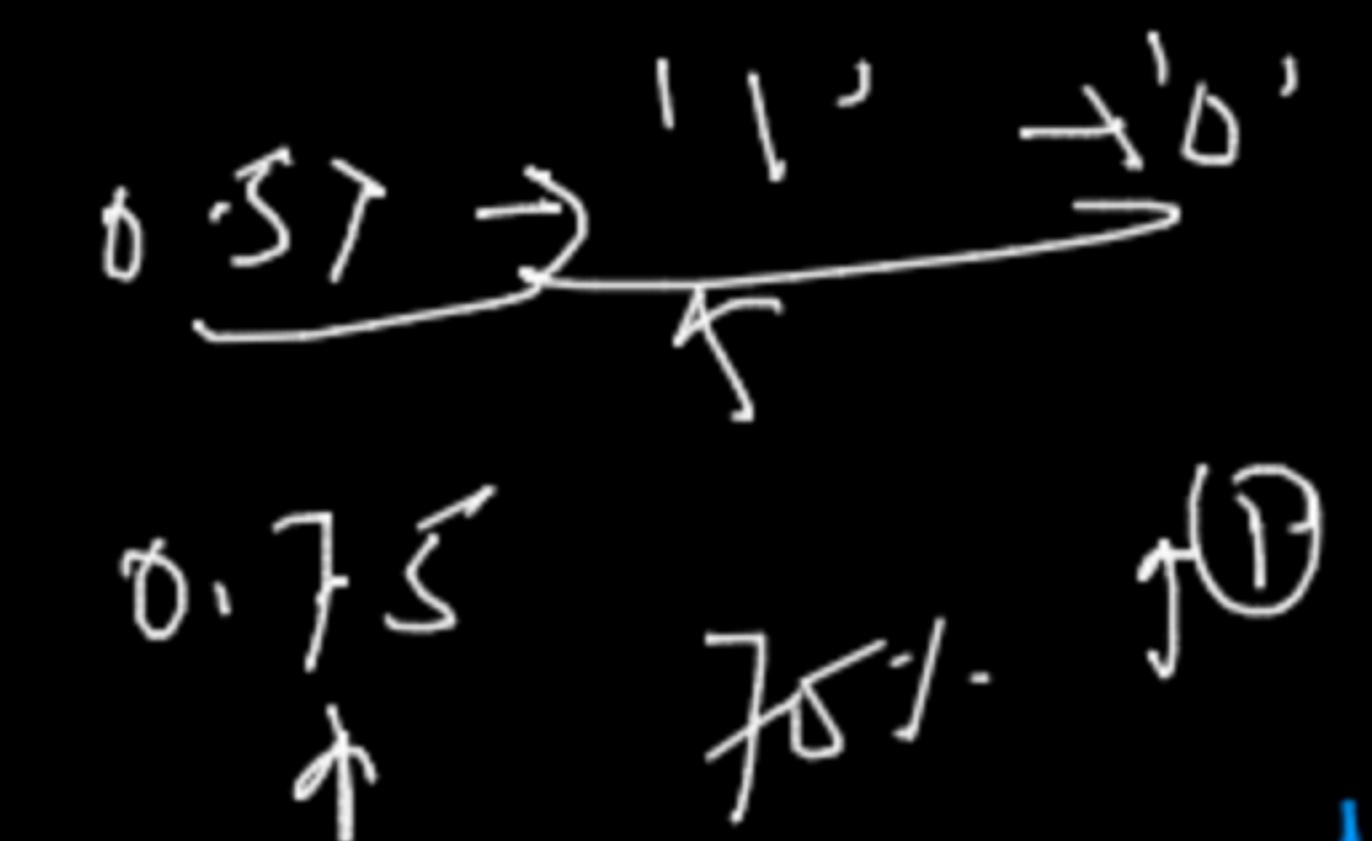
↑  
Receiving operating characteristics

↳  
Binary classification

Area under curve



$$(x, y) \in [0, 1]$$



Step 1 → Compute Prob-Score and sort it in decreasing order

$\sigma \leftarrow$

$x$	$y$	$y$	$y_{\sigma=0.95}$	$y_{\sigma=0.92}$	$y_{\sigma=0.80}$	$y_{\sigma=0.76}$	$y_{\sigma=0.71}$
$x_1$	1	0.95	1 ✓	1	1	1	1
$x_2$	1	0.92	0 ✗	1	1	1	1
$x_3$	0	0.80	0 ✓	0	0	1	1
$x_4$	1	0.76	0 ✗	0	0	1	1
$x_5$	1	0.71	0 ✗	0	0	0	1

$$\uparrow (FPR | TPR) \quad \uparrow (FPR) \quad \uparrow (FPR, TPR) \quad \uparrow$$

Step 2 → False threshold say  $\sigma = 0.95$   $\rightarrow 1$   
 else  $\rightarrow 0$

$$FPR = \frac{FP}{P}$$

$$TPR = \frac{TP}{1 - P}$$

0	1
0	3

$$N=11, P=4$$

$$FPR \quad \uparrow$$

$$TPR \quad \uparrow$$

F-PR

sugges Her

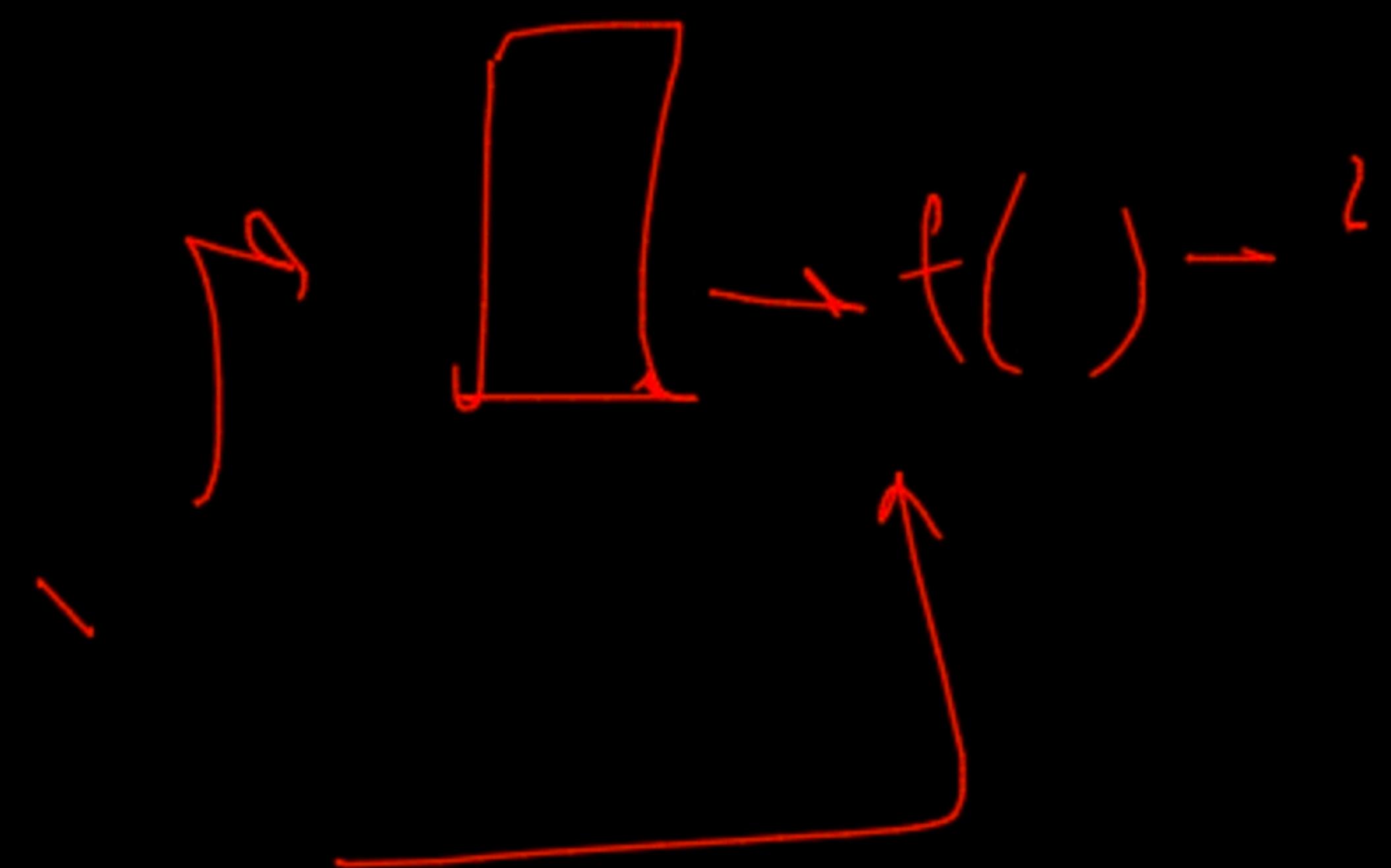
Paul

1 PR

AKL, Pre, Recall, CM, ROC & AUC

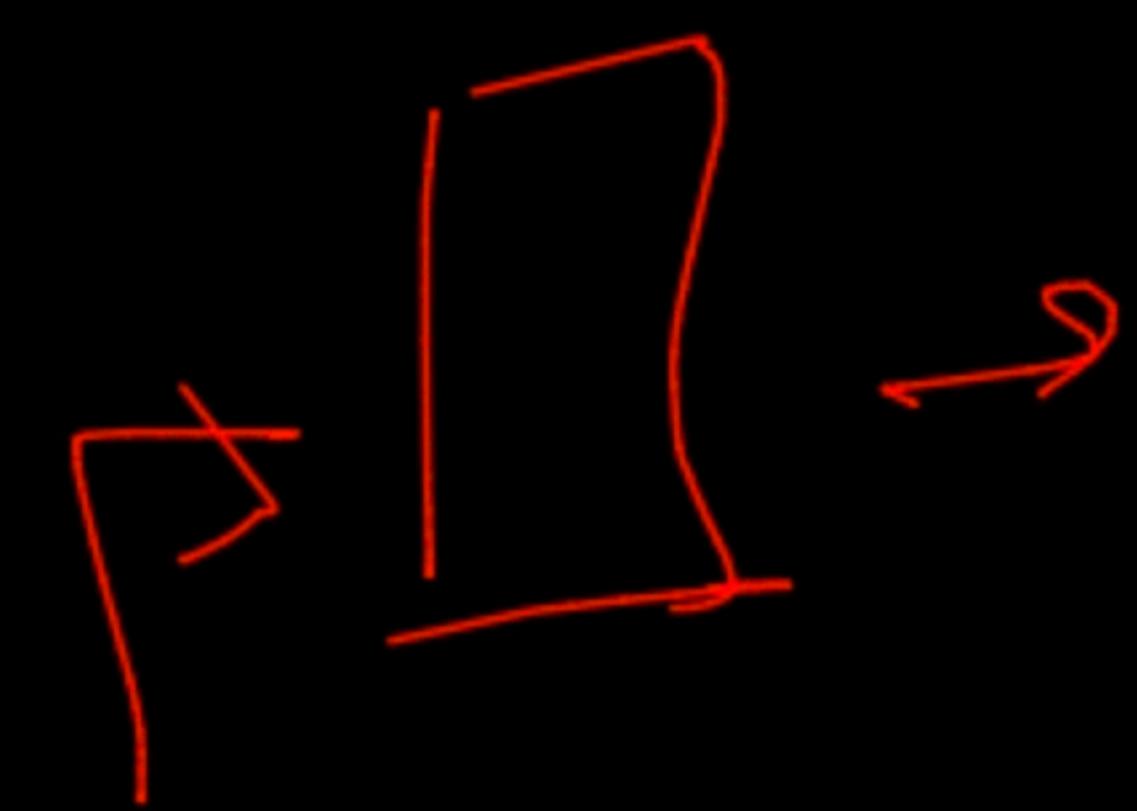
n-class

Binary class



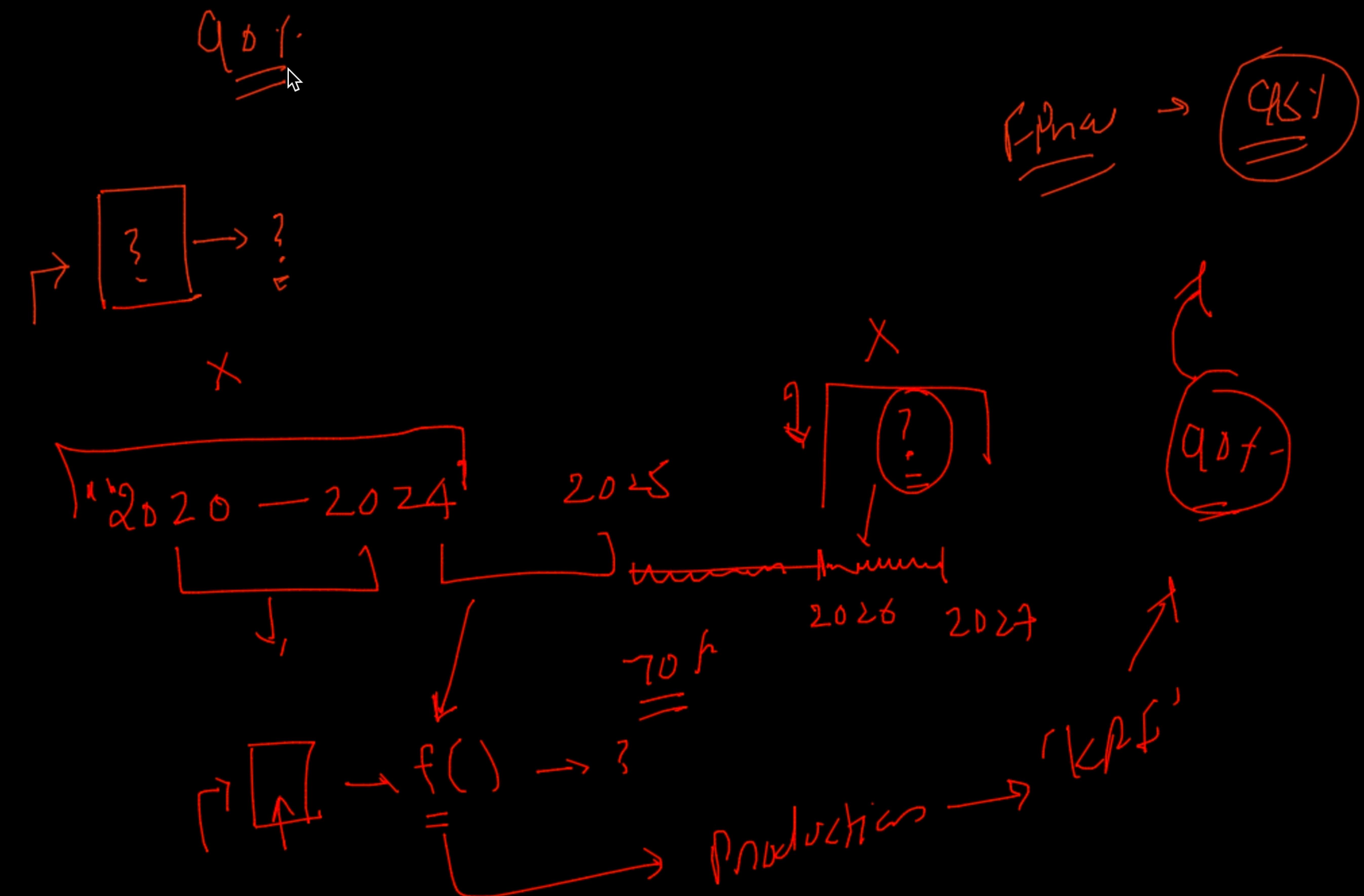
$(x, y)$

$\{0, 1, 2, \dots, n\}$



KP

ALL, 1, 1, 1



Log-loss

Use Prob-slope

Medical domain

Acc

$[0 - 1]$

Conf

Log-loss

$f(x)$

$(y - f(x))$

Random model

Binary classification

$0.5 > 0.1$

'less'

$\downarrow$

$$\begin{array}{c}
 \text{X} \quad \text{Y} \quad \gamma \quad \text{Log-loss} \\
 \checkmark \quad x_1 \quad 1 \quad 0.9 \rightarrow -\log(0.9) * 1 \rightarrow 0.045 \\
 \checkmark \quad x_2 \quad 1 \quad 0.6 \rightarrow -\log(0.6) * 1 \rightarrow 0.22 \leftarrow \text{No!} \\
 \checkmark \quad x_3 \quad 0 \quad 0.1 \rightarrow -\log(0.9) * 1 \rightarrow 0.045 \quad (\text{less}) \\
 \checkmark \quad x_4 \quad 0 \quad 0.4 \quad n \quad -\log(0.6) \rightarrow 0.22 \uparrow
 \end{array}$$

$$\text{Log-loss} = -\frac{1}{n} \sum_{i=1}^n \underbrace{[\log(p_i) * y_i + (1-y_i) * \log(1-p_i)]}_{(1-1)}$$

$$\log-loss = 0.54$$

$\downarrow \log \uparrow$