



Module 16

Partha Pratim
Das

Week Recap

Objectives &
Outline

Relational
Algebra

Select

Project

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Rename

Division

Module Summary

Database Management Systems

Module 16: Formal Relational Query Languages/1

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Module Summary

- SQL Examples have been practiced for basic query structures
- Nested Subquery in SQL
- Data Modification
- SQL expressions for Join and Views
- Transactions
- Integrity Constraints
- More data types in SQL
- Authorization in SQL
- Functions and Procedures in SQL
- Triggers



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Module Summary

- To understand formal query language through relational algebra



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Module Summary

- Relational Algebra



Formal Relational Query Language

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Module Summary

- Relational Algebra
 - Procedural and Algebra based
- Tuple Relational Calculus
 - Non-Procedural and Predicate Calculus based
- Domain Relational Calculus
 - Non-Procedural and Predicate Calculus based



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Module Summary

Relational Algebra



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Module Summary

- Created by Edgar F Codd at IBM in 1970
- Procedural language
- Six basic operators
 - select: σ
 - project: Π
 - union: \cup
 - set difference: $-$
 - Cartesian product: \times
 - rename: ρ
- The operators take one or two relations as inputs and produce a new relation as a result

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Module Summary

- Notation: $\sigma_p(r)$
- p is called the **selection predicate**
- Defined as:

$$\sigma_p(r) = \{t | t \in r \text{ and } p(t)\}$$

where p is a formula in propositional calculus consisting of **terms** connected by : \wedge (**and**), \vee (**or**), \neg (**not**)

Each **terms** is one of:

$$< \text{attribute} > \text{ op } < \text{attribute} > \text{ or } < \text{constant} >$$

where op is one of: $=, \neq, >, \geq, <, \leq$

- Example of selection:

$$\sigma_{\text{dept_name} = 'Physics'}(\text{instructor})$$

A	B	C	D
α	α	1	7
α	β	5	7
β	β	12	3
β	β	23	10

A	B	C	D
α	α	1	7
β	β	23	10

$$\sigma_{A=B \wedge D > 5}(r)$$



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Module Summary

- Notation: $\Pi_{A_1, A_2, \dots, A_k}(r)$
where A_1, A_2 are attribute names and r is a relation
- The result is defined as the relation of k columns obtained by erasing the columns that are not listed
- Duplicate rows removed from result, since relations are sets
- Example: To eliminate the *dept_name* attribute of *instructor*

$$\Pi_{ID, name, salary}(instructor)$$

A	B	C
α	10	1
α	20	1
β	30	1
β	40	2

A	C
α	1
α	1
β	1
β	2

=

A	C
α	1
β	1
β	2



Union Operation

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Module Summary

- Notation: $r \cup s$
- Defined as: $r \cup s = \{t \mid t \in r \text{ or } t \in s\}$
- For $r \cup s$ to be valid.
 - a) r, s must have the *same arity* (same number of attributes)
 - b) The attribute domains must be *compatible* (example: 2nd column of r deals with the same type of values as does the 2nd column of s)
 - c) Example: to find all courses taught in the Fall 2009 semester, or in the Spring 2010 semester, or in both

A	B
α	1
α	2
β	1

r

A	B
α	2
β	3

s

A	B
α	1
α	2
β	1
β	3

$r \cup s$

$$\Pi_{course_id}(\sigma_{semester="Fall" \wedge year=2009}(section)) \cup \Pi_{course_id}(\sigma_{semester="Spring" \wedge year=2010}(section))$$



Difference Operation

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Module Summary

- Notation $r - s$
- Defined as: $r - s = \{t | t \in r \text{ and } t \notin s\}$
- Set differences must be taken between **compatible** relations
 - r and s must have the **same** arity
 - attribute domains of r and s must be compatible
- Example: to find all courses taught in the Fall 2009 semester, but not in the Spring 2010 semester

$$\Pi_{course_id}(\sigma_{semester="Fall" \wedge year=2009}(section)) -$$

$$\Pi_{course_id}(\sigma_{semester="Spring" \wedge year=2010}(section))$$

A	B
α	1
α	2
β	1

r

A	B
α	2
β	3

s

A	B
α	1
β	1

$r - s$



Intersection Operation

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Module Summary

- Notation: $r \cap s$
- Defined as:

$$r \cap s = \{t \mid t \in r \text{ and } t \in s\}$$

- Assume:
 - r, s have the *same arity*
 - attributes of r and s are compatible
- Note: $r \cap s = r - (r - s)$

A	B
α	1
α	2
β	1

r

A	B
α	2
β	3

s

A	B
α	2

$r \cap s$



Cartesian-Product Operation

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Module Summary

- Notation $r \times s$
- Defined as:

$$r \times s = \{t \mid t \in r \text{ and } q \in s\}$$

- Assume that attributes of $r(R)$ and $s(S)$ are disjoint.
(That is, $R \cap S = \phi$)
- If attributes of $r(R)$ and $s(S)$ are not disjoint, then
renaming must be used

A	B
α	1
β	2

 r

C	D	E
α	10	a
β	10	a
β	20	b
γ	10	b

 s

A	B	C	D	E
α	1	α	10	a
α	1	β	10	a
α	1	β	20	b
α	1	γ	10	b
β	2	α	10	a
β	2	β	10	a
β	2	β	20	b
β	2	γ	10	b

 $r \times s$



Rename Operation

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Module Summary

- Allows us to name, and therefore to refer to, the results of relational-algebra expressions.
- Allows us to refer to a relation by more than one name.
- Example:

$$\rho_X(E)$$

returns the expression E under the name X

- If a relational-algebra expression E has arity n , then

$$\rho_X(A_1, A_2, \dots, A_n)(E)$$

returns the result of expression E under the name X , and with the attributes renamed to

$$A_1, A_2, \dots, A_n$$

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Module Summary

- The division operation is applied to two relations
- $R(Z) \div S(X)$, where X subset Z . Let $Y = Z - X$ (and hence $Z = X \cup Y$); that is, let Y be the set of attributes of R that are not attributes of S
- The result of DIVISION is a relation $T(Y)$ that includes a tuple t if tuples t_R appear in R with $t_R[Y] = t$, and with
 - $t_R[X] = t_s$ for every tuple t_s in S .
- For a tuple t to appear in the result T of the DIVISION, the values in t must appear in R in combination with every tuple in S
- Division is a derived operation and can be expressed in terms of other operations
- $r \div s \equiv \Pi_{R-S}(r) - \Pi_{R-S}(r)((\Pi_{R-S}(r) \times s) - \Pi_{R-S,S}(r))$



Division Examples

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Module Summary

• R

Lecturer	Module
Brown	Compilers
Brown	Databases
Green	Prolog
Green	Databases
Lewis	Prolog
Smith	Databases

S

Subject
Prolog

R | S

Lecturer
Green Lewis



Division Examples (2)

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Module Summary

• R

Lecturer	Module
Brown	Compilers
Brown	Databases
Green	Prolog
Green	Databases
Lewis	Prolog
Smith	Databases

S

Subject
Databases
Prolog

R | S

Lecturer
Green



Division Examples (3)

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Module Summary

A

<i>sno</i>	<i>pno</i>
s1	p1
s1	p2
s1	p3
s1	p4
s2	p1
s2	p2
s3	p2
s4	p2
s4	p4

B1

<i>pno</i>
p2

B2

<i>pno</i>
p2
p4

B3

<i>pno</i>
p1
p2
p4

A/B1

<i>sno</i>
s1
s2
s3
s4

A/B2

<i>sno</i>
s1
s4

A/B3

<i>sno</i>
s1



Division Example (4)

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Module Summary

- Relations r, s :

A	B
α	1
α	2
α	3
β	1
γ	1
δ	1
δ	3
δ	4
ϵ	6
ϵ	1
β	2

r

B
1
2

s

A
α
β

- $r \div s$:

*e.g. A is customer name
B is branch-name
1 and 2 here show two specific branch-names
(Find customers who have an account in all
branches of the bank)*



Division Example (5)

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Module Summary

- Relations r, s :

A	B	C	D	E
α	a	α	a	1
α	a	γ	a	1
α	a	γ	b	1
β	a	γ	a	1
β	a	γ	b	3
γ	a	γ	a	1
γ	a	γ	b	1
γ	a	β	b	1

r

A	B	C
α	a	γ
γ	a	γ

- $r \div s$:

D	E
a	1
b	1

s

e.g. Students who have taken both "a" and "b" courses, with instructor "1"

(Find students who have taken all courses given by instructor 1)



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Module Summary

- Discussed relational algebra with examples

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