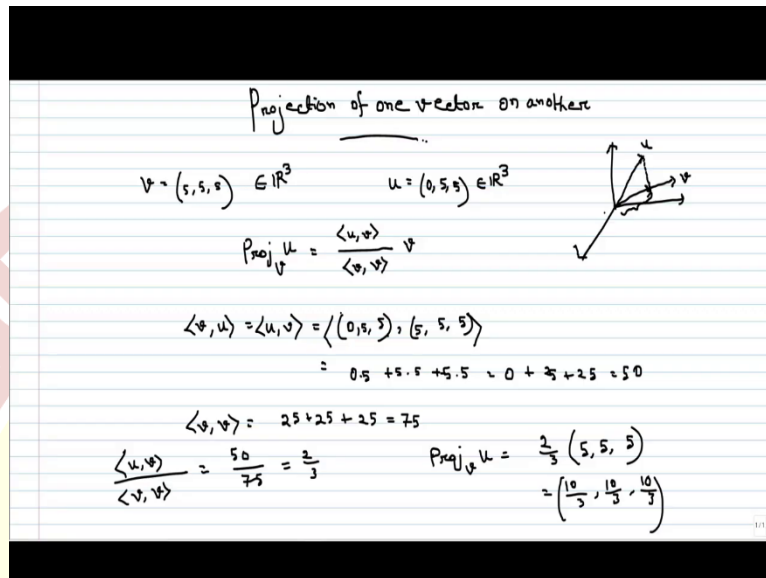


**IIT Madras**  
ONLINE DEGREE

**Mathematics for Data Science 2**  
**Professor. Sarang S. Sane**  
**Department of Mathematics**  
**Indian Institute of Technology, Madras**  
**Week 9 Tutorial 01**

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Projection of one vector on another

$$v = (5, 5, 5) \in \mathbb{R}^3 \quad u = (0, 5, 5) \in \mathbb{R}^3$$

$$\text{Proj}_v u = \frac{\langle u, v \rangle}{\langle v, v \rangle} v$$

$$\langle v, u \rangle = \langle u, v \rangle = \langle (0, 5, 5), (5, 5, 5) \rangle$$

$$= 0 \cdot 5 + 5 \cdot 5 + 5 \cdot 5 = 0 + 25 + 25 = 50$$

$$\langle v, v \rangle = 25 + 25 + 25 = 75$$

$$\frac{\langle u, v \rangle}{\langle v, v \rangle} = \frac{50}{75} = \frac{2}{3} \quad \text{Proj}_v u = \frac{2}{3} (5, 5, 5)$$

$$= \left( \frac{10}{3}, \frac{10}{3}, \frac{10}{3} \right)$$

Hello everyone, so in this video let us try to calculate projection of one vector on another vector. So, let us begin with this example, suppose, I am taking a vector  $v$  which is  $(5, 5, 5)$ . So, this is a vector on  $\mathbb{R}^3$ . Now, suppose there is another vector  $u$  and I am denoting it by  $(0, 5, 5)$ . So, I am taking another vector on  $\mathbb{R}^3$ . And I want to calculate the projection of vector  $u$  on  $v$ .

So, projection of vector  $u$  in the direction of  $v$  this one we have to calculate. So, in the lecture we have seen the formula to calculate it, so, we have to calculate the inner product of  $u$  and  $v$   $\langle u, v \rangle$ , we also have to calculate the inner product of  $v$  and  $v$ . And as we are calculating the projection in the direction of  $v$ , so we have to multiply the vector  $v$  with this scalar.

$$\text{Proj}_v u = \frac{\langle u, v \rangle}{\langle v, v \rangle} v$$

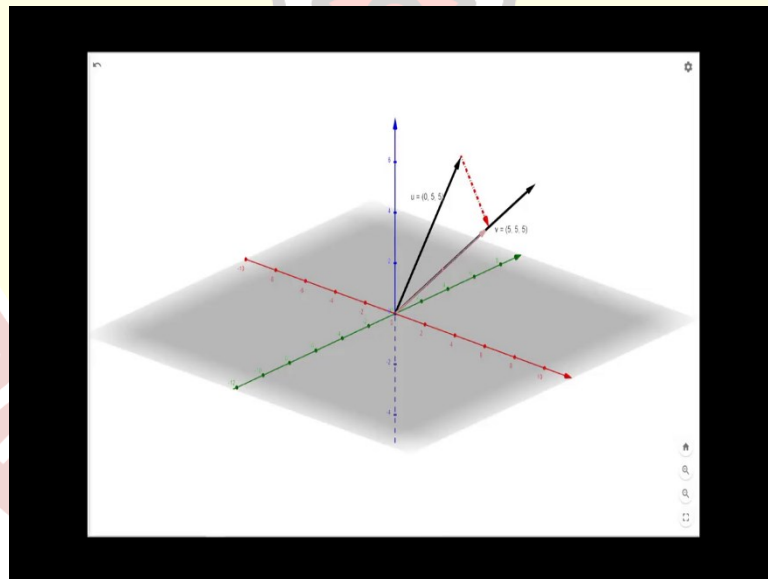
So, as you calculate the inner product of  $u$  and  $v$ , you will get an scalar if we calculate inner product  $v$  and  $v$ , we will get another scalar you have to multiply this scalar with this vector to get the projection. So, let us calculate. So, what is inner product  $u$  and  $v$ ? So, inner product  $u$  and  $v$  which is same as inner product  $v$  and  $u$  obviously, so it is nothing but the dot product.

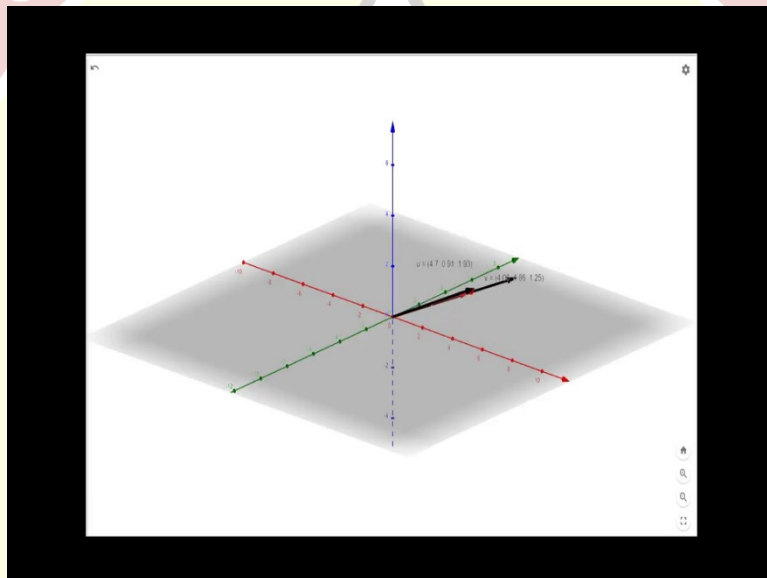
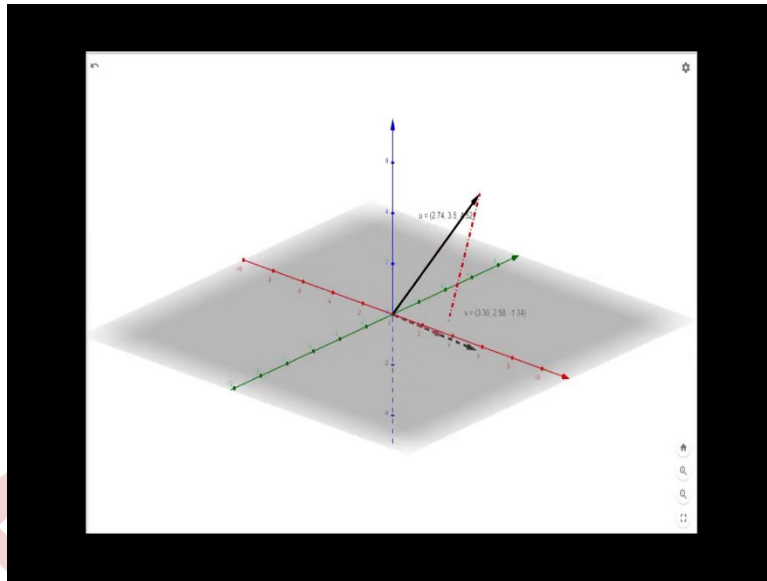
So, we have two vectors here,  $(0, 5, 5)$  and  $(5, 5, 5)$ . So, if we calculate the inner product, if we calculate the dot product, so, we will get  $0 \times 5 + 5 \times 5 + 5 \times 5$ . So, what do we get, we will get  $0 + 25 + 25$ . So, will get 50. Similarly, if you calculate inner product of  $v$  and  $v$ , the same vector, so you will get  $25 + 25 + 25$ , which is 75.

So, the scalar you get here is  $\frac{\langle u, v \rangle}{\langle v, v \rangle}$ . So, this will give you 50 by 75. So, it is nothing but  $2/3$ . Now, in the direction of  $v$ , we have to calculate the projection. So, our projection of  $u$  in the direction of  $v$  is nothing but  $\frac{2}{3} \times v$ . So,  $v$  is  $(5, 5, 5)$ . So, it is  $(10/3, 10/3, 10/3)$ .

So, geometrically what we are doing, we are starting with two vectors, suppose, this is my  $v$  and this is my  $u$ . So, this is why  $u$  vector, this is my  $v$  vector and I am taking projection of  $u$  on this vector. So basically, I am calculating this vector with this much magnitude in the direction of  $v$ . So, this is the geometric representation of this. Now, let us try to visualize this in GeoGebra.

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So, this is  $\mathbb{R}^3$  we can see here, so at first we will take the vector  $v$  which is  $(5, 5, 5)$ . So this is the vector  $v$ . Now, where is the vector  $u$ ? So, here is the vector  $u$  which is  $(0, 5, 5)$ . Now, we have to take the projection of  $u$  on  $v$  as we have calculated it already. So, we can see that this will give us the projection on  $u$  in the direction of  $v$ . So, as you can see, this vector along the rejection of  $v$  is the projection of  $u$  on the direction of  $v$ . So, the dotted line basically gives us a perception how we calculate the projection.

Now, if we change the this  $u$  and  $v$  we can see that this projection will also change. So, now let us try to see this animation where do we change  $u$  and  $v$  all together and we can see the projection is changing. So, in this animation we can see how the change of  $u$  and  $v$  is changing the projection in the direction of  $v$ . So, this animation helps us to visualize this projection. Thank you.