



chapter 07 calculus problems

```
In [1]: import math
        math.sin(math.pi/2)
```

Out[1]: 1.0

```
In [ ]: import sympy
        sympy.sin(math.pi/2)
```

```
In [3]: from sympy import sin, solve, Symbol
        u = Symbol('u')
        t = Symbol('t')
        g = Symbol('g')
        theta = Symbol('theta')
        solve(u*sin(theta)-g*t,t)
```

Out[3]: [u*sin(theta)/g]

assumptions in symPy

```
In [4]: from sympy import Symbol
        x = Symbol('x', positive = True)
        if (x+5) > 0:
            print('Do something')
        else:
            print('Do something else')
```

Do something

Finding the limit of Functions

```
In [7]: from sympy import Limit, Symbol, S
        x = Symbol('x')
        Limit(1/x,x,S.Infinity)
```

Out[7]: $\lim_{x \rightarrow \infty} \frac{1}{x}$

```
In [8]: l = Limit(1/x,x,S.Infinity)
        l.doit()
```

Out[8]: 0

```
In [9]: Limit(1/x,x,0, dir='+').doit()
```

Out[9]: ∞

```
In [11]: from sympy import Symbol, sin
        Limit(sin(x)/x,x,0).doit()
```

Out[11]: 1

```
In [13]: from sympy import Symbol, Limit, S
        n= Symbol('n')
        Limit((1+1/n)**n,n, S.Infinity).doit()
```

Out[13]: e

Continuous Compound Interest

```
In [14]: from sympy import Symbol, Limit, S
        p = Symbol('p', positive=True)
        r = Symbol('r', positive=True)
        t = Symbol('t', positive=True)
        Limit(p*(1+r/n)**(n*t),n,S.Infinity).doit()
```

Out[14]: pe^{rt}

Instantaneous Rate of Change

```
In [18]: from sympy import Symbol, Limit
        t = Symbol('t')
        st = 5*t**2 + 2*t + 8

        t1 = Symbol('t1')
        delta_t = Symbol('delta_t')

        st1 = st.subs({t:t1})
        st1_delta = st.subs({t:t1+delta_t})
        Limit((st1_delta-st1)/delta_t, delta_t, 0).doit()
```

Out[18]: $10t_1 + 2$

finding derivative of functions

```
In [20]: from sympy import Symbol, Derivative
        t = Symbol('t')
        st = 5*t**2 + 2*t + 8
        Derivative(st,t)
```

Out[20]: $\frac{d}{dt}(5t^2 + 2t + 8)$

```
In [21]: d = Derivative(st,t)
```

```
d.doit()
```

Out[21]: $10t + 2$

```
In [22]: d.doit().subs({t:t1})
```

Out[22]: $10t_1 + 2$

```
In [23]: d.doit().subs({t:1})
```

Out[23]: 12

```
In [24]: from sympy import Derivative, Symbol
x = Symbol('x')
f = (x**3 + x**2 + x)*(x**2+x)
Derivative(f, x).doit()
```

Out[24]: $(2x + 1)(x^3 + x^2 + x) + (x^2 + x)(3x^2 + 2x + 1)$

A Derivative Calculator

```
In [33]: from sympy import Derivative, Symbol, sympify, pprint
from sympy.core.sympify import SympifyError

def derivative(f,var):
    var = Symbol(var)
    d = Derivative(f,var).doit()
    pprint(d)

if __name__ == '__main__':

    f = input('enter a function: ')
    var = input('enter the variable to differentiate with respect to:')
    try:
        f = sympify(f)
    except SympifyError:
        print('invalid input')
    else:
        derivative(f,var)
```

enter a function: $2x^2 + 3x + 1$

enter the variable to differentiate with respect to: x

$4x + 3$

higher-order Derivatives and Finding the Maxima and Minima

```
In [36]: from sympy import Symbol, solve, Derivative
x = Symbol('x')
f = x**5 - 30*x**3 + 50*x
f = x**5 - 30 * x**3 + 50 * x
d1 = Derivative(f,x).doit()
```

```
critical_points = solve(d1)
critical_points
```

```
Out[36]: [-sqrt(9 - sqrt(71)),
          sqrt(9 - sqrt(71)),
          -sqrt(sqrt(71) + 9),
          sqrt(sqrt(71) + 9)]
```

```
In [37]: A = critical_points[2]
         B = critical_points[0]
         C = critical_points[1]
         D = critical_points[3]
```

```
In [38]: d2 = Derivative(f,x,2).doit()
```

```
In [39]: d2.subs({x:B}).evalf()
```

```
Out[39]: 127.661060789073
```

```
In [40]: d2.subs({x:C}).evalf()
```

```
Out[40]: -127.661060789073
```

```
In [41]: d2.subs({x:A}).evalf()
```

```
Out[41]: -703.493179468151
```

```
In [42]: d2.subs({x:D}).evalf()
```

```
Out[42]: 703.493179468151
```

```
In [44]: x = min = -5
         x_max = 5
         f.subs({x:A}).evalf()
```

```
Out[44]: -30.0x3 + 50.0x + x4.17446401028639
```


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```
def grad_ascent(x0,f1x,x):
    epsilon = 1e-6
    step_size = 1e-4
    x_old = x0
    x_new = x_old + step_size*f1x.subs({x:x_old}).evalf()
    while abs(x_old - x_new) > epsilon:
        x_old = x_new
```

```

x_new = x_old + step_size*f1x.subs({x:x_old}).evalf()
return x_new

def find_max_theta(R, theta):
    # Calculate the first derivative
    R1theta = Derivative(R, theta).doit()
    theta0 = 1e-3
    theta_max = grad_ascent(theta0, R1theta, theta)
    return theta_max

if __name__ == '__main__':
    g = 9.8
    #assume initial velocity
    u = 25
    #expression for range
    theta = Symbol('theta')
    R = u**2*sin(2*theta)/g

    theta_max = find_max_theta(R, theta)
    print('theta :{0}'.format(math.degrees(theta_max)))
    print('maxium Range:{0}:'.format(R.subs({theta:theta_max})))

```

theta :1.5186448207743275
 maxium Range:3.37920154330593:

A Generic Program for Gradient Ascent

In [55]:

```

from sympy import Derivative , Symbol, sympify

def grad_ascent(x0,f1x,x):
    step_size = 1e-3
    x_old = x0
    x_new = x_old + step_size*f1x.subs({x:x_old}).evalf()

    return x_new

if __name__ == '__main__':
    f = input('enter a function in one variable:')
    var = input('enter the variable to differentiate with respect to:')
    var0 = float(input('enter the inital value of the variable :'))
    try:
        f = sympify(f)
    except SympifyError:
        print('invalid function entered')

    else:
        var = Symbol(var)
        d = Derivative(f,var).doit()
        var_max = grad_ascent(var0,d,var)
        print('{0}:{1}'.format(var.name,var_max))
        print('maxium value:{0}'.format(f.subs({var:var_max})))

```

enter a function in one variable:25*25*sin(2*theta)/9.8
 enter the variable to differentiate with respect to:theta
 enter the inital value of the variable :0.001
 theta:0.128550765306207

```
In [56]: from sympy import Derivative , Symbol, sympify

def grad_ascent(x0,f1x,x):
    step_size = 1e-3
    x_old = x0
    x_new = x_old + step_size*f1x.subs({x:x_old}).evalf()

    return x_new

if __name__ == '__main__':
    f = input('enter a function in one variable:')
    var = input('enter the variable to differentiate with respect to:')
    var0 = float(input('enter the initial value of the variable :'))
    try:
        f = sympify(f)
    except SympifyError:
        print('invalid function entered')

    else:
        var = Symbol(var)
        d = Derivative(f,var).doit()
        var_max = grad_ascent(var0,d,var)
        print('{0}:{1}'.format(var.name,var_max))
        print('maximum value:{0}'.format(f.subs({var:var_max})))
```

```
enter a function in one variable:cos(y) +k
enter the variable to differentiate with respect to:y
enter the initial value of the variable :0.01
y:0.00999000016666583
maximum value:k + 0.999950100363336
```

A Word of Warning About the Initial Value

```
In [57]: from sympy import Derivative , Symbol, sympify

def grad_ascent(x0,f1x,x):
    step_size = 1e-3
    x_old = x0
    x_new = x_old + step_size*f1x.subs({x:x_old}).evalf()

    return x_new

if __name__ == '__main__':
    f = input('enter a function in one variable:')
    var = input('enter the variable to differentiate with respect to:')
    var0 = float(input('enter the initial value of the variable :'))
    try:
        f = sympify(f)
    except SympifyError:
        print('invalid function entered')

    else:
        var = Symbol(var)
        d = Derivative(f,var).doit()
        var_max = grad_ascent(var0,d,var)
        print('{0}:{1}'.format(var.name,var_max))
```

```
print(' {0}:{1}'.format(var.name, var_max))
print('maximum value:{0}'.format(f.subs({var:var_max})))
```

enter a function in one variable: $x^5 - 30x^3 + 50x$
 enter the variable to differentiate with respect to: x
 enter the initial value of the variable :-2
 $x: -2.230000000000000$
 maximum value:166.039702265700

In [58]:

```
from sympy import Derivative, Symbol, sympify

def grad_ascent(x0, f1x, x):
    step_size = 1e-3
    x_old = x0
    x_new = x_old + step_size*f1x.subs({x:x_old}).evalf()

    return x_new

if __name__ == '__main__':
    f = input('enter a function in one variable:')
    var = input('enter the variable to differentiate with respect to:')
    var0 = float(input('enter the initial value of the variable :'))
    try:
        f = sympify(f)
    except SympifyError:
        print('invalid function entered')

    else:
        var = Symbol(var)
        d = Derivative(f, var).doit()
        var_max = grad_ascent(var0, d, var)
        print(' {0}:{1}'.format(var.name, var_max))
        print('maximum value:{0}'.format(f.subs({var:var_max})))
```

enter a function in one variable: $x^5 - 30x^3 + 50x$
 enter the variable to differentiate with respect to: x
 enter the initial value of the variable :0.5
 $x: 0.527812500000000$
 maximum value:22.0203528721678

The Role of the Step Size and Epsilon

In [61]:

```
from sympy import Derivative, Symbol, sympify, solve, SympifyError

def grad_ascent(x0, f1x, x):
    # Check if f1x=0 has a solution
    if not solve(f1x):
        print('cannot continue, solution for {0}=0 does not exist'.format(f1x))
        return
    epsilon = 1e-6
    step_size = 1e-4
    x_old = x0
    x_new = x_old + step_size*f1x.subs({x: x_old}).evalf()
    while abs(x_old - x_new) > epsilon:
        x_old = x_new
        x_new = x_old + step_size*f1x.subs({x: x_old}).evalf() # Fixed here
    return x_new
```

```

if __name__ == '__main__':
    f = input('enter a function in one variable:')
    var = input('enter the variable to differentiate with respect to: ')
    var0 = float(input('enter the initial value of the variable: '))
    try:
        f = sympify(f)
    except SympifyError:
        print('invalid function entered')
    else:
        var = Symbol(var)
        d = Derivative(f, var).doit()
        var_max = grad_ascent(var0, d, var)
        if var_max:
            print('{0}: {1}'.format(var.name, var_max))
            print('maximum value: {0}'.format(f.subs({var: var_max})))

```

enter a function in one variable:log(x)
 enter the variable to differentiate with respect to: x
 enter the initial value of the variable: 0.1
 cannot continue, solution for 1/x=0 does not exist

Finding the integrals of Functions

In [64]:

```

from sympy import Integral, symbols
x = Symbol('x')
k = Symbol('k')
Integral(k*x,x)

```

Out[64]: $\int kx \, dx$

In [65]:

```

Integral(k*x,x).doit()

```

Out[65]: $\frac{kx^2}{2}$

In [66]:

```

Integral(k*x,(x,0,2)).doit()

```

Out[66]: $2k$

In [67]:

```

from sympy import Integral, Symbol
x = Symbol('x')
Integral(x,(x,2,4)).doit()

```

Out[67]: 6

Probability Density Functions

In [68]:

```

from sympy import Symbol, exp, sqrt, pi, integrals
x = Symbol('x')
p = exp(-(x-10)**2/2)/sqrt(2*pi)
Integral(p,(x,11,12)).doit().evalf()

```



```
Integral(p,(x,-10,10)).doit().evalf()
```

Out[68]: 0.135905121983278

```
In [69]: from sympy import Symbol, exp, sqrt, pi, Integral, S
x = Symbol('x')
p = exp(-(x-10)**2/2)/sqrt(2*pi)
Integral(p,(x,S.NegativeInfinity,S.Infinity)).doit().evalf()
```

Out[69]: 1.0

chapter ends.