Rahul Chopra | Bsc.(Hons) Computer Science | 20 21 | 449 | Practical - 3

Plotting third order solution family of Differential Equation.

Question I:

Solve third order Differential Equation y'' - 5y'' + 8y' - 4y = 0 and Plot

its three Solutions.

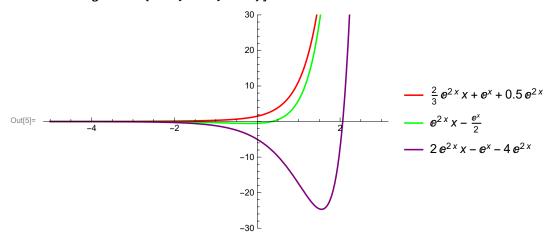
Solution:

```
\label{eq:continuous} \begin{array}{ll} & \text{In[1]:= Sol = DSolve[y'''[x] - 5 y''[x] + 8 y'[x] - 4 y[x] =: 0, y[x], x]} \\ & \text{Out[1]:= } \left\{ \left\{ y[x] \rightarrow \text{e}^x \, \text{C[1]} + \text{e}^{2x} \, \text{C[2]} + \text{e}^{2x} \, \text{x} \, \text{C[3]} \right\} \right\} \\ & \text{In[2]:= Sol1 = y[x] /. Sol[[1]] /. } \left\{ \text{C[1]} \rightarrow \text{1, C[2]} \rightarrow \text{0.5, C[3]} \rightarrow \text{2/3} \right\} \\ & \text{Out[2]:= } \text{e}^x + \text{0.5 } \text{e}^{2x} + \frac{2}{3} \, \text{e}^{2x} \, \text{x} \end{array}
```

$$ln[3]:=$$
 Sol2 = y[x] /. Sol[[1]] /. $\{C[1] \rightarrow -1/2, C[2] \rightarrow 0, C[3] \rightarrow 1\}$
Out[3]= $-\frac{e^{x}}{2} + e^{2x} x$

$$ln[4]:=$$
 Sol3 = y[x] /. Sol[[1]] /. {C[1] \rightarrow -1, C[2] \rightarrow -4, C[3] \rightarrow 2}
Out[4]:= $-e^{x} - 4e^{2x} + 2e^{2x} x$

 $\label{eq:local_local} $$ \inf[s]:= Plot[{Sol1, Sol2, Sol3}, {x, -5, 3}, PlotRange \rightarrow {-30, 30}, \\ PlotStyle \rightarrow {{Red}, {Green}, {Purple}}, \\ PlotLegends \rightarrow {Sol1, Sol2, Sol3}] $$$



Question 2:

Solve third order Differential Equation y" +

$$3y'' - 25y' + 21y = 0$$
 and

Plot its any four Solutions. Solution:

```
ln[6]:= Eqn = y'''[x] + 3 * y''[x] - 25 * y'[x] + 21 * y[x]
         Sol = DSolve [Eqn == 0, y[x], x]
         Sol1 = y[x] /. Sol[1] /. \{C[1] \rightarrow 1, C[2] \rightarrow 0, C[3] \rightarrow 2\}
         Sol2 = y[x] /. Sol[1] /. \{C[1] \rightarrow -1/2, C[2] \rightarrow 0, C[3] \rightarrow 1\}
         Sol3 = y[x] /. Sol[[1]] /. {C[1] \rightarrow -1, C[2] \rightarrow -4, C[3] \rightarrow 2}
         Sol4 = y[x] /. Sol[1] /. \{C[1] \rightarrow -0.5, C[2] \rightarrow -2, C[3] \rightarrow 1\}
         Plot[{Sol1, Sol2, Sol3, Sol4}, {x, -0.5, 0.5},
           PlotStyle → {{Red}, {Green}, {Purple}, {Orange}},
           PlotLegends → {Sol1, Sol2, Sol3, Sol4}]
 Out[6]= 21 y [x] - 25 y' [x] + 3 y'' [x] + y^{(3)} [x]
 \text{Out[7]= } \left\{ \left. \left\{ y \left[\, x \, \right] \right. \right. \right. \to \left. \mathbb{e}^{-7\,x} \, C \left[\, 1\, \right] \right. + \left. \mathbb{e}^{x} \, C \left[\, 2\, \right] \right. + \left. \mathbb{e}^{3\,x} \, C \left[\, 3\, \right] \right. \right\} \right\}
Out[8]= e^{-7x} + 2e^{3x}
Out[9]= -\frac{1}{2} e^{-7x} + e^{3x}
Out[10]= -e^{-7x} - 4e^x + 2e^3x
Out[11]= -0.5 e^{-7x} - 2 e^{x} + e^{3x}
Out[12]=
                 -0.4
                                                                                                           -e^{-7x}-4e^x+2e^{3x}
                                                                                                             -0.5e^{-7x}-2e^{x}+e^{3x}
                                                  -10
```

Question 3:

Solve third order Differential Equation y'' -4y'' - 25y' + 28y = 0 and

Plot its any four Solutions.

In[20]:= Eqn = y'''[x] - 4 * y''[x] - 25 * y'[x] + 28 * y[x] Sol = DSolve[Eqn == 0, y[x], x] Sol1 = y[x] /. Sol[1] /. {C[1]
$$\rightarrow$$
 1, C[2] \rightarrow 0, C[3] \rightarrow 2} Sol2 = y[x] /. Sol[1] /. {C[1] \rightarrow -2, C[2] \rightarrow 10, C[3] \rightarrow 3} Sol3 = y[x] /. Sol[1] /. {C[1] \rightarrow -1, C[2] \rightarrow -4, C[3] \rightarrow 20} Sol4 = y[x] /. Sol[1] /. {C[1] \rightarrow -0.5, C[2] \rightarrow -2, C[3] \rightarrow 1} Plot[{Sol1, Sol2, Sol3, Sol4}, {x, -0.5, 0.5}, PlotStyle \rightarrow {{Red}, {Green}, {Purple}, {Orange}}, PlotLegends \rightarrow {Sol1, Sol2, Sol3, Sol4}]

Out[20]= $28 y[x] - 25 y'[x] - 4 y''[x] + y^{(3)}[x]$

Out[21]= $\left\{ \left\{ y[x] \rightarrow e^{-4x} C[1] + e^{x} C[2] + e^{7x} C[3] \right\} \right\}$

Out[22]= $e^{-4x} + 2 e^{7x}$

Out[23]= $-2 e^{-4x} + 10 e^{x} + 3 e^{7x}$

Out[24]= $-e^{-4x} - 4 e^{x} + 20 e^{7x}$

Out[25]= $-0.5 e^{-4x} - 2 e^{x} + e^{7x}$

