

Rahul

- LL

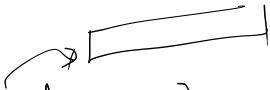
- Arr (pre-sum ...)

- Sort

- | Searching

- Bit man^o

- [Stacks]



- Math gcd primeFactors ?

- recursion ?

- Time Complexity ↗

- (BS) → O(logn)

- (MS) → O(n logn)

Q) Bit manipulation (Prob^n)

$$\text{eg } A = \begin{smallmatrix} 8 & 4 & 2 & 1 \\ 1 & 0 & 1 & 0 \end{smallmatrix} \quad (\text{10})$$

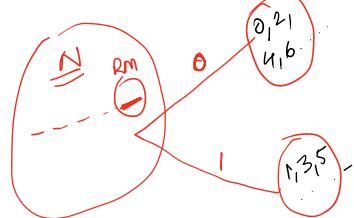
$$A > \begin{smallmatrix} 1 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 \end{smallmatrix} \quad (9)$$

$$\boxed{A \otimes 1} = ?$$

$A \otimes 1 \Rightarrow 0 \Rightarrow$ last bit in A \Rightarrow unset
 $\Rightarrow 1 \Rightarrow$ set.

$$\begin{array}{r} \begin{smallmatrix} 1 & 0 & 1 & 0 \\ 1 & 0 & 1 & 0 \end{smallmatrix} = E + E \Rightarrow (E) \\ \cancel{\text{1}} \cancel{\text{0}} \cancel{\text{1}} \cancel{\text{0}} = 8 + 2 = 10 \end{array}$$

$$\begin{smallmatrix} 1 & 0 & 0 \\ (E) & (0) \end{smallmatrix} \quad [2=1] = E + 0 = 0$$



$$(ii) A \otimes 0 \Rightarrow \underline{0}$$

$$(iii) A \otimes A = \underline{A}$$

$$A(10) \Rightarrow 1010$$

$$\begin{array}{r} \times 0000 \\ \hline 0000 \Rightarrow 0 \end{array}$$

$$(4) A \setminus 0 = \textcircled{A}$$

$$(5) A / A = \textcircled{A}$$

$$(6) A \wedge 0 = \textcircled{A}$$

$$(7) A \wedge A = \textcircled{0}$$

$$A(10) = \underline{1} \underline{0} \underline{1} \underline{0}$$

$$\begin{array}{r} 0 = \cancel{A} \ 0 \ 0 \ 0 \ 0 \\ \hline 1 \ 0 \ 1 \ 0 = \textcircled{A} \end{array}$$

(8) Commutative Property

$$(i) (a \& b) = (b \& a) \checkmark$$

$$2 \& 5 = 5 \& 2$$

~~1 0 1 0~~
~~0 1 0 1~~

$$(ii) (a | b) = (b | a) \checkmark$$

$$(iii) (a \wedge b) = (b \wedge a) \checkmark$$

(9) Associativity

$$\boxed{a \& b \& c} = \boxed{(c \& a) \& b} \times$$

$a \& c \xrightarrow{\quad} \boxed{a \& b \& c}$

$$a | b | c = \boxed{\begin{matrix} b \\ a | b | c \end{matrix}} \checkmark$$

$$\boxed{a \wedge b \wedge c} = \boxed{\begin{matrix} b \wedge c \wedge a \\ b \wedge a \wedge c \\ a \wedge b \wedge c \end{matrix}}$$

$$8 \quad a \wedge b \wedge c \wedge b \wedge a$$

$$\begin{array}{r} \text{if} \quad \frac{a \wedge a \wedge b \wedge b \wedge c}{0 \wedge 0 \wedge 0 \wedge c} \\ \hline \dots \quad \dots \end{array}$$

$$0^n C = \textcircled{C} \times$$

Given an int arr of size $N-1$
 It contains nos. from $1 \dots N$. eg $N=5$
 Find the left out no.
 $\text{arr} = \{1, 2, 3, 4, 5\}$

$\text{TC} = O(n)$
 $\text{SC} = O(1)$

$\text{Ans} \Rightarrow 0 \nmid \textcircled{3}$

$m=2 \Rightarrow \text{Sort.} \rightarrow \textcircled{1}$
 $\boxed{1, 2, 0, 5}$
 $\begin{matrix} 0 & 1 & 2 & 3 \\ \textcircled{1} & \textcircled{2} & \textcircled{3} & \textcircled{5} \end{matrix}$
 $\text{TC} \sim O(n \log n) + O(n) \sim O(n \log n)$
 $\text{SC} = O(1)$

$m=3 \Rightarrow$
 $\sum_{i=1}^n i - \sum_{i=1}^{N-1} \text{arr}[i] = \textcircled{2}$
 $\text{for } i=0 \dots (n-2)$
 $\text{sum} = \text{arr}[i]$
 $\text{TotalSum} = \left[\frac{n(n+1)}{2} \right]$
 $\text{TC} = O(n)$
 $\text{SC} = O(1)$

Left shift ($<<$)

$a=22$
 $(a<<1) \Rightarrow 22 * 2^1 \Rightarrow 22 * 2^0$
 $(a<<2) \Rightarrow 22 * 2^2 \Rightarrow 22 * 2^1$
 $(a<<3) \Rightarrow 22 * 2^3 \Rightarrow 22 * 2^2$

$a << i = a * 2^i$

$|a=1| \Rightarrow |1 << i = 1 * 2^i|$

$\overbrace{\quad \quad \quad}^{\rightarrow} \perp \perp = +$

$$A \Rightarrow 0010 \quad | \quad 101$$

$$\begin{array}{r} 0000 \\ \times 0100 \\ \hline 0010 \quad | \quad 101 \end{array} \Rightarrow 45(A)$$

$$A \Rightarrow 0010 \quad | \quad 1101$$

$$\begin{array}{r} 0001 \\ \times 0000 \\ \hline 0010 \quad | \quad 1101 \end{array} \Rightarrow 61(45+16)$$

$$\begin{array}{r} 1 \ll 4 \\ = 2^4 \\ = 16 \end{array}$$

$\boxed{N \mid (1 \ll i)}$ \Rightarrow if i^{th} bit is already set
 \Rightarrow if i^{th} bit is unset.

$$A \Rightarrow 0010 \quad | \quad 101$$

$$\wedge \quad 0000 \quad | \quad 0100$$

$$\hline 0010 \quad | \quad 1001 \Rightarrow 41$$

$$A \Rightarrow 0010 \quad | \quad 1101$$

$$\wedge \quad 0001 \quad | \quad 0000$$

$$\hline 0010 \quad | \quad 1101 \Rightarrow 61$$

$\boxed{N \wedge (1 \ll i)}$ \Rightarrow if i^{th} bit is set
 \Rightarrow if i^{th} bit is unset.

$$A \Rightarrow 0010 \quad | \quad 1101$$

$$\& \quad 0000 \quad | \quad 0100$$

$$\hline 0000 \quad | \quad 0100 = 4$$

$$A \Rightarrow 0010 \quad | \quad 1101$$

$$\& \quad 0001 \quad | \quad 0000$$

$$\hline 0000 \quad | \quad 0000 = 0$$

$\boxed{N \& (1 \ll i)}$ \Rightarrow if i^{th} bit is set
 \Rightarrow if i^{th} bit is unset.

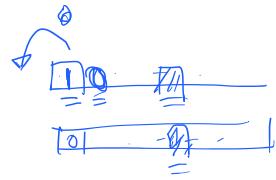
Given an int 'n'
 i) set i^{th} bit of "n"
 . b1

$$N = N \mid (1 \ll i)$$

(ii) Toggle i^{th} bit. ($0 \rightarrow 1, 1 \rightarrow 0$)

$$N = N \wedge (1 \ll i)$$

$$\underline{N \ll i}$$



(iii) Check if i^{th} bit is set or not.

$$\underline{\underline{m}} \quad \underline{\underline{\text{if } (N \& (1 \ll i)) == 1 \ll i}}$$

\Rightarrow set

else

\Rightarrow unset.

$$\underline{\underline{0110}} \quad \underline{\underline{N \ll i}}$$

$$\underline{\underline{\text{if } (N \mid (1 \ll i)) == N}}$$

\Rightarrow set

else

\Rightarrow unset.

~~extra space~~
~~extra time~~

Given an int arr, except 1 ele. all other ele. having triplet.

Find the unique no.

$$\underline{\underline{\text{eg}}} \quad [2, 3, 3, 1, 1, 3, 1] \quad \underline{\underline{O/P}} \Rightarrow (2) \checkmark$$

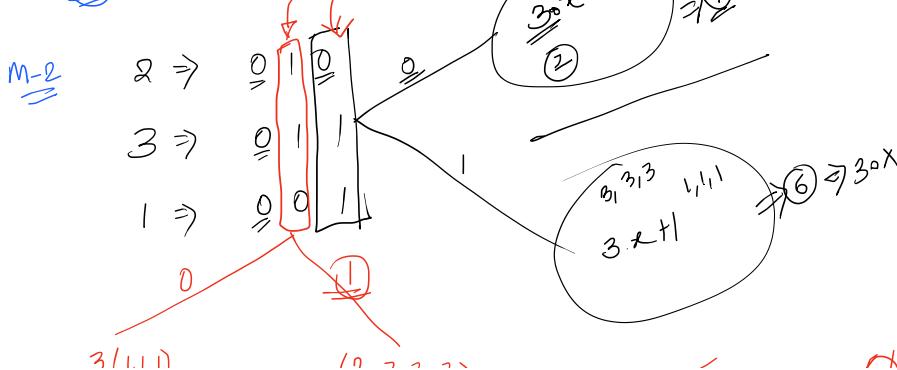
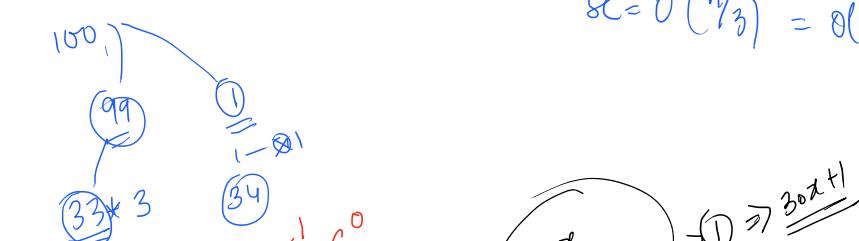
$$\underline{\underline{m-1}} \quad \left[\begin{matrix} 2-1 \\ 3-\cancel{*}3 \\ 1-\cancel{*}3 \end{matrix} \right] \quad \downarrow \quad \underline{\underline{(2) \times}}$$

$$\underline{\underline{\text{TC}}} = \underline{\underline{O(N)}} + \underline{\underline{O(N/3)}} \Rightarrow \underline{\underline{O(N)}}$$

build
Hmap

Traverse
Hmap

$$\underline{\underline{SC}} = O\left(\frac{n}{3}\right) = O(n)$$



$$\begin{array}{rcl} 0 & \cancel{\times} & 0 \Rightarrow (2) \checkmark \\ \cancel{0=7} & \cancel{0=3} & C_0 + 1 \\ \cancel{C_1=4} & & C_1 = 6 \end{array}$$

$\sim \text{C++11}$

$(\alpha, \beta, \gamma, \delta)$

$\left[\dots \frac{\alpha}{\beta} \right]$

$\alpha m = 0$

for $i \leftarrow 0 \dots \beta - 1$ { 32 }

$c_0 = 0$ /

$c_{-1} = 0$ /

for ($j = 0; j < n; j++$) {

if ($a[i][j] \& (1 \ll i) == 0$)

$c_0 +=$

else

$c_{-1} +=$

}

if ($c_0 \% 3 == 0$) {

$\alpha m = (\alpha m + (1 \ll i))$

}

- notion

- (GHT) ↗

$\underline{\underline{O(N)}}$

$O(\underline{\underline{32}} \cdot N)$

$T_C \approx \underline{\underline{O(N)}}$

$S_C = \underline{\underline{O(1)}}$