# ECE 637: Lab 8

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## Section 3.1 Report

1. Original and thresholded image:





(a) Original image

(b) Thresholded image

2. Computed RMSE and fidelity values:

Listing 1: RMSE and fidelity for section 3.1

1 house\_threshold 2 RMSE: 87.393 Fidelity: 75.661

3. For python code for fidelity function refer to Listing 8 at page 4

For python code refer to Listing 7 at page 4 and Listing 12 at page 8.

### Section 4.2 Report

• The three Bayer index matrices of sizes 2x2, 4x4, and 8x8:

Listing 2: Bayer index matrices

```
1 Bayer index matrix: size 2x2
   \begin{bmatrix} 1 & 2 \end{bmatrix}
   [3 0]]
3
4 Bayer index matrix: size 4x4
         9
             6 10]
   [ 5
    13
          1 14
     7 11
                 8
    [15]
          3 12
                 0]]
   Bayer index matrix: size 8x8
10
   [[21 37 25 41 22 38
11
          5 57
                    54
                        6
                          58
12
    29
         45
            17
                33 30
                       46
                          18
                               34
                   62 \ 14 \ 50
13
    61
         13 \ 49
                 1
                43 \ 20 \ 36 \ 24
14
    [23]
         39 27
                               40]
15
    55
          7 59
                11 \ 52
                        456
                                8
16
    [31 47 19 35 28 44 16
                               32
    [63 15 51
                 3 60 12 48
17
                                0]]
```

• The three halftoned images:



• RMSE and Fidelity for each of the three halftoned images:

Listing 3: RMSE and fidelity for 2x2

```
1 house_dither2
2 RMSE: 97.669 Fidelity: 49.313
```

#### Listing 4: RMSE and fidelity for 4x4

```
1 house_dither4
2 RMSE:101.007 Fidelity:16.847
```

Listing 5: RMSE and fidelity for 8x8

```
1 house_dither8
2 RMSE:100.915 Fidelity:15.855
```

For python refer to Listing 9 at page 5, Listing 10 at page 7 and Listing 12 at page 8.

# Section 5 Report

- For python code refer to Listing 11 at page 7
- The error diffusion result:



Figure 3: Error diffusion result

• RMSE and fidelity results:

Listing 6: RMSE and fidelity

```
1 house_error_diff
2 RMSE: 98.847 Fidelity: 14.761
```

• Table of RMSE and fidelity

$\operatorname{Method}$	RMSE	Fidelity
Simple thresholding	87.393	75.661
Order dithering 2x2	97.669	49.313
Order dithering 4x4	101.007	16.847
Order dithering 8x8	100.915	15.855
Error diffusion	98.847	14.761

**TODO**comment

## Appendix

Got to git repo for complete code.

Listing 7: Python code for section 3

```
#!/usr/bin/env python3
1
2
   \# -*- coding: utf-8 -*-
3
   @author: rahul
4
   ECE637 DIP-1: lab 8 Halftoning
5
   section 3
6
7
8
9
   import numpy as np
10
   from PIL import Image
11
   import os, sys
12
   import matplotlib.pyplot as plt
13
   from matplotlib import cm
14
   from utils import RMSE, Fidelity
15
16
   def get base(filename):
17
18
        base = os.path.basename(filename).split('.')[0]
        return base
19
20
21
   def main(input img, Threshold):
22
        #compute binary image using threshold
23
        out img = (255*(input img>Threshold).astype(np.int)).astype(np.uint8)
^{24}
        #compute rmse
25
        rmse = RMSE(input img, out img)
        fidelity = Fidelity (input img, out img)
26
27
        return out img, rmse, fidelity
28
29
    if __name__=="__main__":
30
        input img name = sys.argv[1]
        output\_img\_name \ = \ get\_base(input\_img\_name) + \ ' \ threshold'
31
32
        Threshold = 127.0
33
        im = Image.open(input img name)
34
        input img = np.array(im)
35
36
        out img, rmse, fidelity = main(input img, Threshold)
37
38
39
        #print info
        print(output img name)
40
        print("RMSE:%0.3f \t Fidelity:%0.3f"%(rmse, fidelity))
41
42
43
        #save plots and images
        gray = cm.get cmap('gray',256)
44
        plt . figure (frameon=False)
45
        plt.imshow(out_img, cmap=gray, interpolation='none')
46
        plt . axis ( ' off ')
47
48
        plt.savefig(output img name+'.pdf', bbox inches='tight', pad inches=0)
49
50
        out im = Image.fromarray(out img)
51
        out_im.save(output_img_name+'.tif')
```

Listing 8: Python code for RMSE and Fidelity

```
#!/usr/bin/env python3
1
2
   \# -*- coding: utf-8 -*-
3
   @author: rahul
   ECE637 DIP-1: lab 8 Halftoning
5
 6
    utility file for image metrics
7
8
9
   import numpy as np
10
   from scipy.signal import convolve2d
11
12
   {\color{red} \mathbf{def} \ \ Un\_gamma\_correct (img \,, \ gamma):}
13
        lin = 255.*((img/255.)**gamma)
14
        return lin.astype(np.uint8)
15
   def Scale to equal brightness (img):
16
17
        return Un_gamma_correct(img, 1./3.)
18
19
   def LPF(img, sigma=np.sqrt(2), size=7):
20
        "pass image through low-pass filter"
21
        #make the filter
        h = np.zeros((size, size))
22
23
        for r in range(size):
24
            for c in range (size):
25
                i = r - (size//2)
26
                j = c - (size//2)
27
                h[r,c] = np. exp(-1.0*(i**2+j**2)/(2*sigma**2))
28
        h /= np.sum(h) #normalize
        #convolve filter
29
30
        out img = convolve2d(img, h)
31
        \#rescale to 0-255
32
        out img -= out img.min()
33
        out img *= (255./out img.max())
34
        return out img.astype(np.uint8)
35
36
   def RMSE(original img, binary image):
37
        "compute rmse error betweeen two images"
        h,w = original img.shape
38
        rmse = (1./(h*w))*np.sum((original img.astype(np.float32) - binary image.astype(
39
            np.float32))**2)
40
        return np.sqrt(rmse)
41
   def Fidelity (original img, binary img):
42
43
        "Compute image fidelity metric"
44
        gamma = 2.2
        # un-gamma correct the images
45
46
        original lin = Un gamma correct (original img, gamma)
47
        binary lin = Un gamma correct (binary img, gamma)
48
        # LPF
49
        original lin lpf = LPF(original lin)
50
        binary lin lpf = LPF(binary lin)
51
        # scale to equal brightness (cube-root)
52
        f_tilde = Scale_to_equal_brightness(original_lin_lpf)
53
        b_tilde = Scale_to_equal_brightness(binary_lin_lpf)
54
        #rmse
        fidelity = RMSE(f tilde, b tilde)
55
        return fidelity
56
```

Listing 9: Python code for section 4

```
1
    #!/usr/bin/env python3
 2
    \# -*- coding: utf-8 -*-
 3
 4
    @author: rahul
    ECE637 DIP-1: lab 8 Halftoning
 5
 6
    section 4
 7
 8
 9
   import numpy as np
   from PIL import Image
10
11
    import os, sys
12
    import matplotlib.pyplot as plt
13
    from matplotlib import cm
14
15
    from utils import RMSE, Fidelity
16
17
    def get_base(filename):
18
        base = os.path.basename(filename).split('.')[0]
19
        return base
20
21
    def Dither mat(N):
22
        if N==2:
23
             return np.array([[1,2],[3,0]])
^{24}
        else:
             return np.block ([[4*Dither_mat(N//2) + 1, 4*Dither_mat(N//2) + 2]
25
26
                               [4*Dither_mat(N//2) + 3, 4*Dither_mat(N//2)]
                                                                                    11)
27
28
    def Threshold_mat(dither_mat):
29
        N, \underline{=}dither\underline{mat}.shape
        T = np.zeros((N,N))
30
        for i in range (N):
31
32
             for j in range(N):
33
                 T[i, j] = 255.0*((dither_mat[i, j] + 0.5)/N**2)
34
        return T
35
    def main(input_img, dither_size, gamma):
36
37
        h, w = input_img.shape
        linear\_img = 255.*(input\_img/255.)**gamma
38
39
        dither_mat = Dither_mat(dither_size)
40
        threshold_mat = Threshold_mat(dither_mat)
41
42
        out_img = np.zeros((h,w))
43
        for i in range(h):
44
             for j in range(w):
45
                 r = i\%dither\_size; c = j\%dither\_size
46
                 if linear_img[i,j] > threshold_mat[r,c]:
47
                     out_img[i,j] = 255
48
                 else:
49
                     \operatorname{out}_{img}[i,j] = 0
50
        return out_img.astype(np.uint8)
51
         name == main :
52
        input_img_name = sys.argv[1]
53
54
        dither size = np.int(sys.argv[2])
55
        output img name = get base(input img name)+ 'dither'+str(dither size)
56
        gamma = 2.2
57
        print (output_img_name)
58
```

```
59
       im = Image.open(input img name)
60
       input img = np.array(im)
61
62
       out img= main(input img, dither size, gamma)
       #compute rmse
63
64
       rmse = RMSE(input img, out img)
65
       fidelity = Fidelity (input img, out img)
66
       #print info
       print("RMSE:%0.3f \t Fidelity:%0.3f"%(rmse, fidelity))
67
68
69
       #save plots and images
70
       71
       \verb|plt.figure|(frameon=False|)
72
       plt.imshow(out_img, cmap=gray, interpolation='none')
       plt . axis ( ' off ' )
73
       plt.savefig(output img name+'.pdf', bbox inches='tight', pad inches=0)
74
75
76
       out im = Image.fromarray(out img)
77
       out im.save(output img name+'.tif')
```

#### Listing 10: Python code for printing bayer matrices

```
#!/usr/bin/env python3
1
2
   \# -*- coding: utf-8 -*-
3
   Created on Thu Apr 8 17:15:10 2021
4
5
   @author: rahul
 6
7
   from order dithering import Dither mat
8
9
10
   for i in [2,4,8]:
        d = Dither_mat(i);
11
        print('Bayer index matrix: size %dx%d'%(i,i))
12
13
        print (d)
```

#### Listing 11: Python code for section 5

```
1
   #!/usr/bin/env python3
 2
   \# -*- coding: utf-8 -*-
 3
   @author: rahul
 4
   ECE637 DIP-1: lab 8 Halftoning
 5
   section 5
 6
 7
 8
 9
   import numpy as np
10
   from PIL import Image
   import os, sys
11
12
    import matplotlib.pyplot as plt
   from matplotlib import cm
13
14
   from utils import RMSE, Fidelity
15
16
17
    def get_base(filename):
18
        base = os.path.basename(filename).split('.')[0]
19
        return base
20
   def main(input img, gamma, Threshold):
```

```
22
        h, w = input_img.shape
23
         linear img = 255.*(input img/255.)**gamma
24
         out img = np.zeros((h,w))
25
        H = np.array([7., 3., 5., 1.])/16.
26
        K = \ [0 \ , \ 1 \ , \ 1 \ , \ 1]
27
        L \ = \ \begin{bmatrix} 1 \ , & -1, & 0 \ , & 1 \end{bmatrix}
28
         for i in range(h):
              for j in range(w):
29
                  old_pxl = linear_img[i,j]
30
                  q = 255. if old pxl>Threshold else 0.
31
                  out\_img\left[\,i\;,\;\;j\,\right]\;=\;q
32
                  e = old_pxl - q
33
                  for h \times \overline{l}, k, l \times \overline{in} \times \overline{zip}(H, K, L):
34
35
                       r = i+k; c = j+l
36
                       if r < h and r > = 0 and c < w and c > = 0:
37
                            linear img[r,c] += e*h kl
         return out img.astype(np.uint8)
38
39
    if __name__=="__main ":
40
41
        input img name = sys.argv[1]
        output img name = get base(input img name)+ ' error diff'
42
43
        gamma = 2.2
         Threshold = 127.
44
         print(output img name)
45
46
47
         im = Image.open(input img name)
48
         input img = np.array(im)
49
50
        out img= main(input img, gamma, Threshold)
51
        #compute rmse
         rmse = RMSE(input img, out img)
52
         fidelity = Fidelity (input img, out img)
53
54
        #print info
         print("RMSE:%0.3f \t Fidelity:%0.3f"%(rmse, fidelity))
55
56
57
        #save plots and images
         gray = cm.get cmap('gray',256)
58
         plt.figure(frameon=False)
59
60
         plt.imshow(out img, cmap=gray, interpolation='none')
61
         plt.axis('off')
62
         plt.savefig(output img name+'.pdf', bbox inches='tight', pad inches=0)
63
64
        out im = Image.fromarray(out img)
65
         out im.save(output img name+'.tif')
```

Listing 12: Bash code for running python code

```
#!/bin/bash
1
2
    img dir = ... / ...
3
4
5
    #section 3
    python simple_thresholding.py "$img_dir"/house.tif | tee sec3.log
6
7
    mv ./*.tif ./output/sec3/
8
    mv \cdot / *.pdf \cdot /output/sec3/
9
    mv \cdot /*.log \cdot /output/sec3/
10
    echo 'section 3 done'
11
12 \mid \#section \mid 4
```

```
python print_dither.py | tee dither_mats.log
13
   for ((size = 2; size < = 8; size *= 2))
14
15
   do
   python order_dithering.py "$img_dir"/house.tif $size | tee dither_"$size".log
16
17
   done
18
   mv ./*.tif output/sec4/
   mv ./*.pdf output/sec4/
19
   mv ./*.log output/sec4/echo 'section 4 done'
20
21
22
23
   #section 5
   python error_diffusion.py "$img_dir"/house.tif | tee sec5.log
^{24}
25
   | mv ./*.pdf output/sec5/
26 mv /* tif output/sec5/
27 mv ./*.log output/sec5
28 echo 'section 5 done'
```