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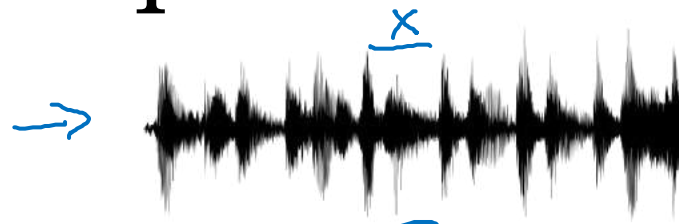
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Recurrent Neural Networks

Why sequence
models?

Examples of sequence data

Speech recognition



y
“The quick brown fox jumped
over the lazy dog.”

Music generation



Sentiment classification

“There is nothing to like
in this movie.”



DNA sequence analysis → AGCCCCTGTGAGGAACTAG



AG**CCCCTGTGAGGAACTAG**

Machine translation

Voulez-vous chanter avec
moi?



Do you want to sing with
me?

Video activity recognition



Running

Name entity recognition → Yesterday, Harry Potter
met Hermione Granger.



Yesterday, **Harry Potter**
met **Hermione Granger**.

Andrew Ng



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Recurrent Neural Networks

Notation

Motivating example

NLP

x: Harry Potter and Hermione Granger invented a new spell.

$\rightarrow x^{(1)} \quad x^{(2)} \quad x^{(3)} \quad \dots \quad x^{(t)} \quad \dots \quad x^{(9)}$

$$T_x = 9$$

$\rightarrow y:$

$y^{(1)} \quad y^{(2)} \quad y^{(3)} \quad \dots \quad y^{(9)}$

$$T_y = 9$$

$x^{(i)(t)}$

$$T_x^{(i)} = 9$$

15

$y^{(i)(t)}$
 \uparrow

$$T_y^{(i)}$$

Representing words

$x^{(t)}$

(x, y)

$x \rightarrow y$

x: Harry Potter and Hermione Granger invented a new spell.

$x^{(1)}$

$x^{(2)}$

$x^{(3)}$

...

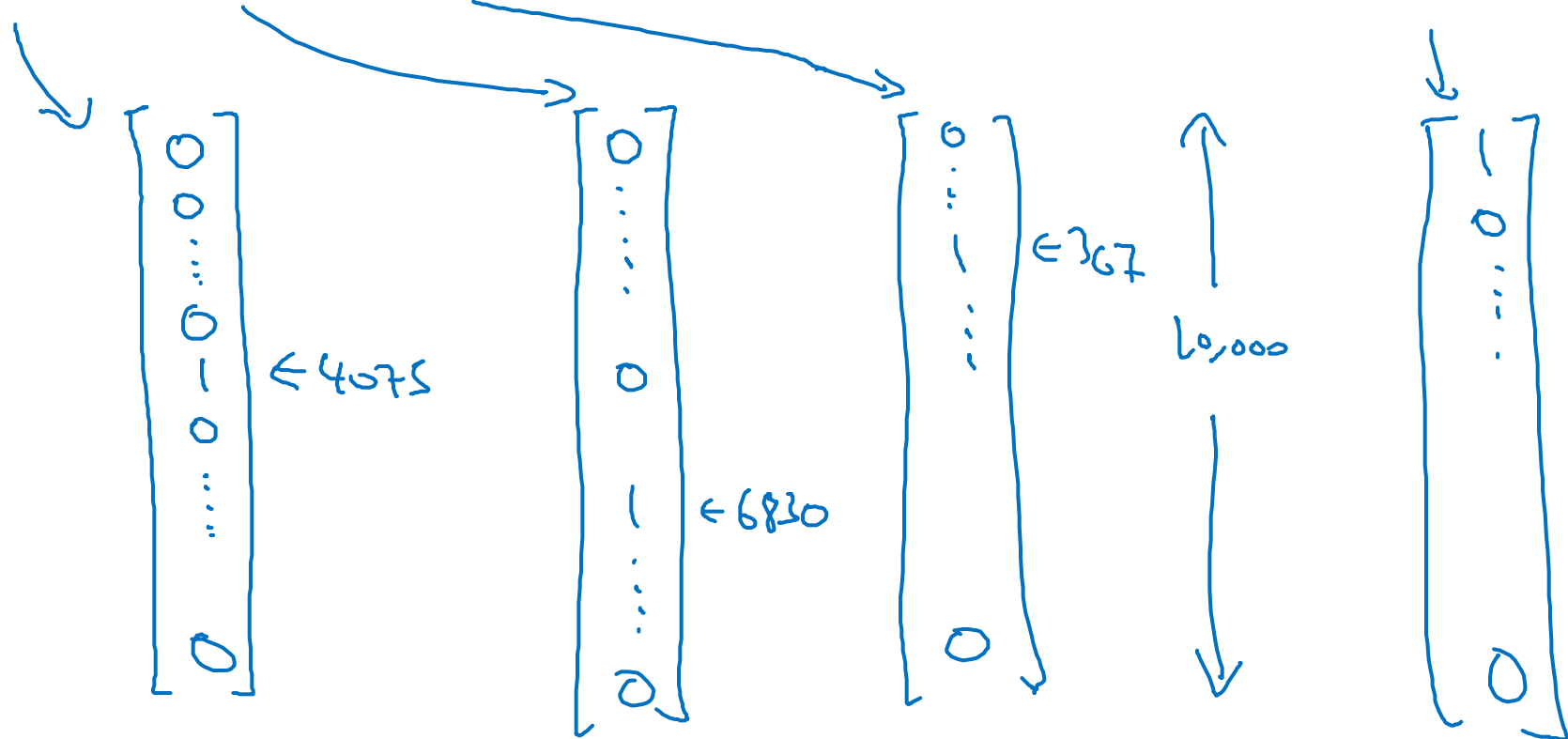
$x^{(7)}$

$x^{(9)}$

Vocabulary

a	1
aaron	2
...	...
and	367
...	...
harry	4075
...	...
potter	6830
...	...
zulu	10,000

<UNK> 10,000



One-hot

Representing words

x: Harry Potter and Hermione Granger invented a new spell.

$$x^{<1>} \quad x^{<2>} \quad x^{<3>} \quad \dots \quad x^{<9>}$$

And = 367

Invented = 4700

$$A = 1$$

New = 5976

Spell = 8376

Harry = 4075

Potter = 6830

Hermione = 4200

Gran... = 4000

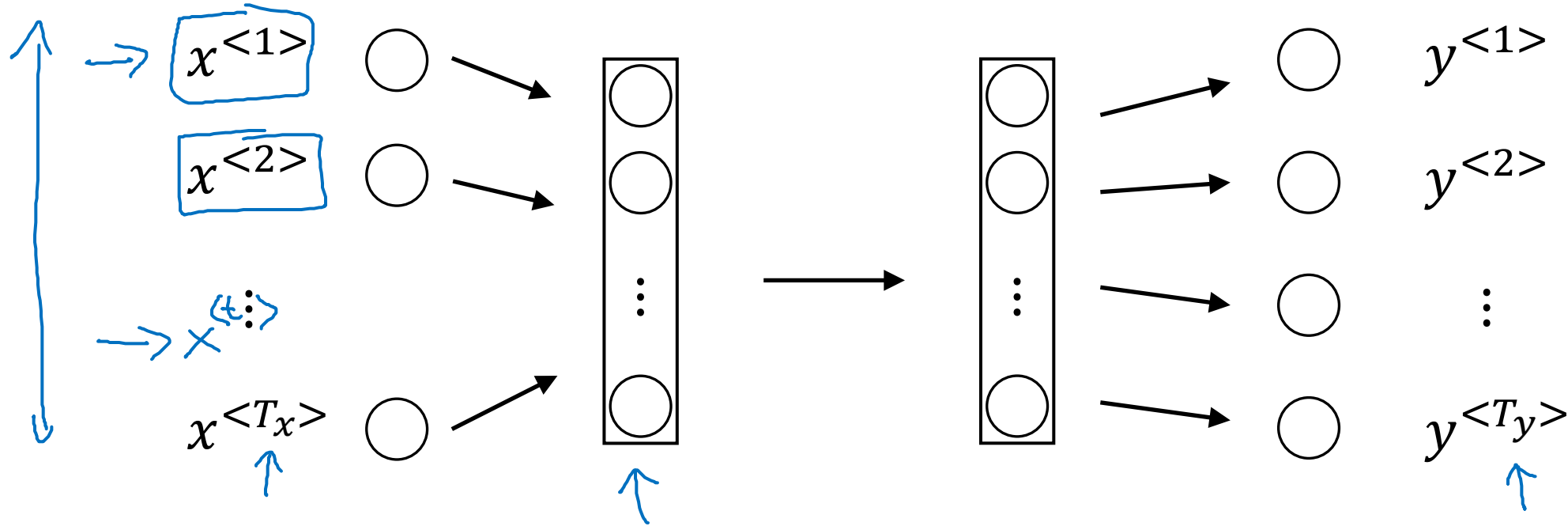


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Recurrent Neural Networks

Recurrent Neural Network Model

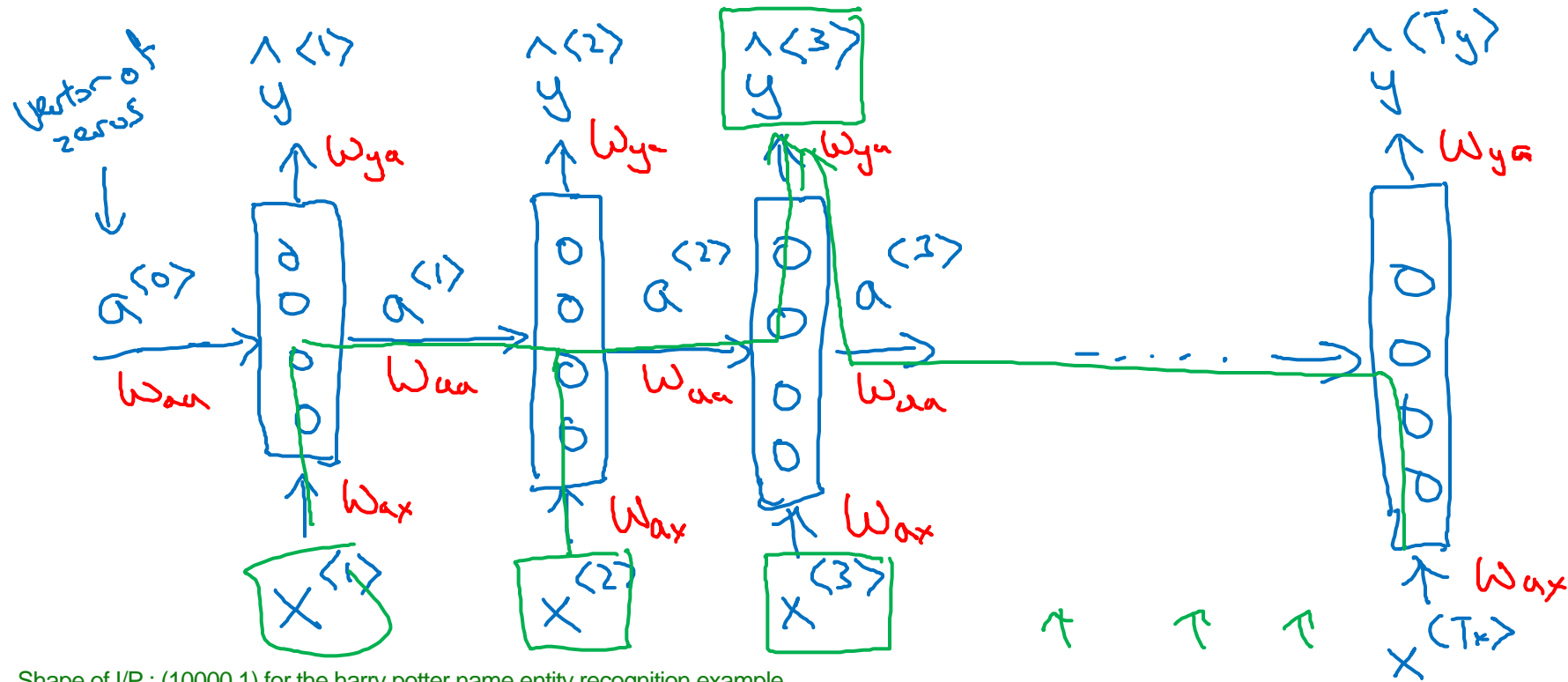
Why not a standard network?



Problems:

- - Inputs, outputs can be different lengths in different examples.
- - Doesn't share features learned across different positions of text.

Recurrent Neural Networks



Shape of I/P : (10000,1) for the harry potter name entity recognition example

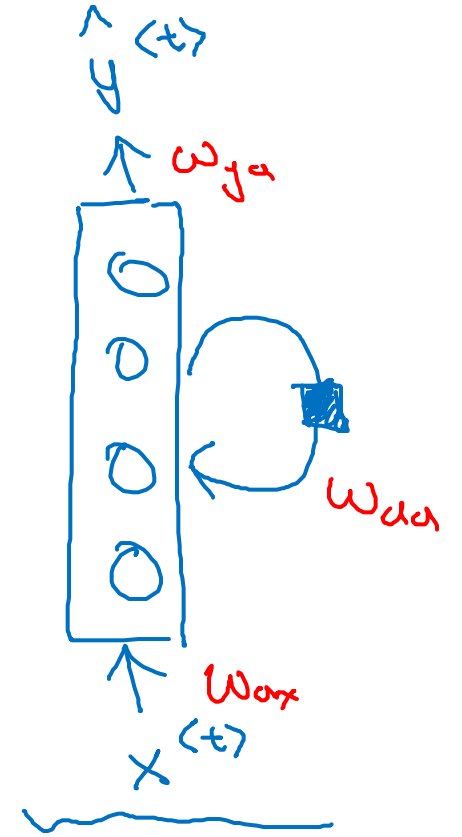
Shape of O/P : (1) [expected o/p = 0 or 1]

[Suppose 1 hidden layer with 128 neurons]

Shape of W_{ax} - (128, 10000)

Shape of W_{aa} - (128,128) Since weight is (number of neurons in current layer, number of inputs)

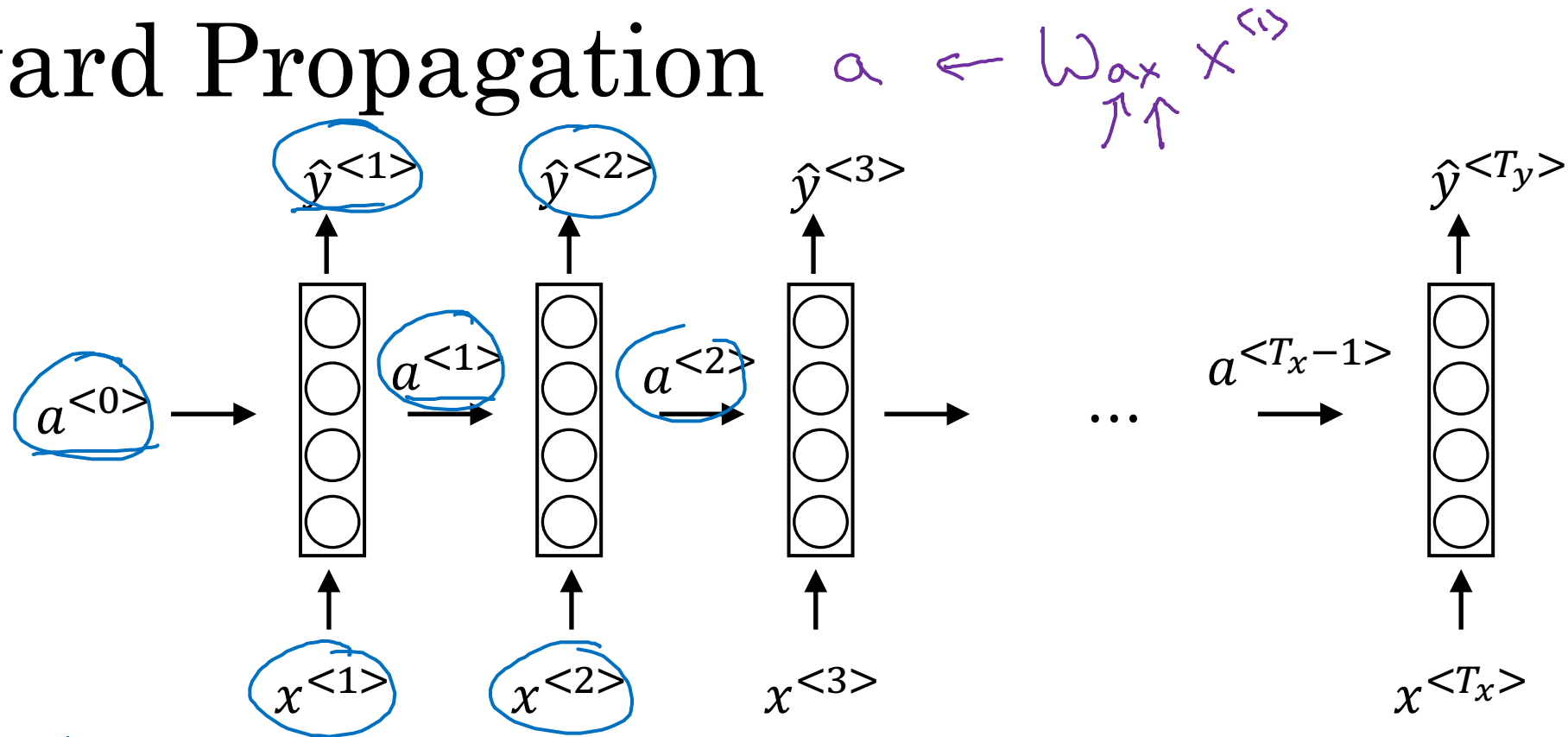
Bidirectional RNN (BRNN)



He said, "Teddy Roosevelt was a great President."

He said, "Teddy bears are on sale!"

Forward Propagation



$$a^{<0>} = \vec{0}$$

$$\underline{a}^{<1>} = g_1(W_{aa} a^{<0>} + \underline{W_{ax}} x^{<1>} + b_a) \leftarrow \underline{\tanh / \text{Relu}}$$

$$\underline{\hat{y}}^{<1>} = g_2(\underline{W_{ya}} a^{<1>} + b_y) \leftarrow \text{Sigmoid}$$

$$\boxed{\begin{aligned} a^{<t>} &= g(W_{aa} a^{<t-1>} + W_{ax} x^{<t>} + b_a) \\ \hat{y}^{<t>} &= g(W_{ya} a^{<t>} + b_y) \end{aligned}}$$

Simplified RNN notation

$$a^{<t>} = g(\underbrace{W_{aa} a^{<t-1>}}_{\substack{\uparrow \\ (100, 100)}} + \underbrace{W_{ax} x^{<t>}}_{\substack{\uparrow \\ (100, 10,000)}} + b_a)$$

$$\hat{y}^{<t>} = g(W_{ya} a^{<t>} + b_y)$$

$$\hat{y}^{<t>} = g(W_y a^{<t>} + b_y)$$

$$a^{<t>} = g(W_a [a^{<t-1>}, x^{<t>}] + b_a)$$

$$\begin{matrix} \uparrow 100 \\ \left[W_{aa} \mid W_{ax} \right] \\ \leftarrow 100 \quad \leftarrow 10,000 \end{matrix} = W_a \quad (100, 10,000)$$

$$[a^{<t-1>}, x^{<t>}] = \begin{bmatrix} a^{<t-1>} \\ x^{<t>} \end{bmatrix} \quad \begin{matrix} \updownarrow 100 \\ \updownarrow 10,000 \\ \updownarrow 10,100 \end{matrix}$$

$$\begin{bmatrix} W_{aa} & W_{ax} \end{bmatrix} \begin{bmatrix} a^{<t-1>} \\ x^{<t>} \end{bmatrix} = \underline{W_{aa} a^{<t-1>} + W_{ax} x^{<t>}}$$

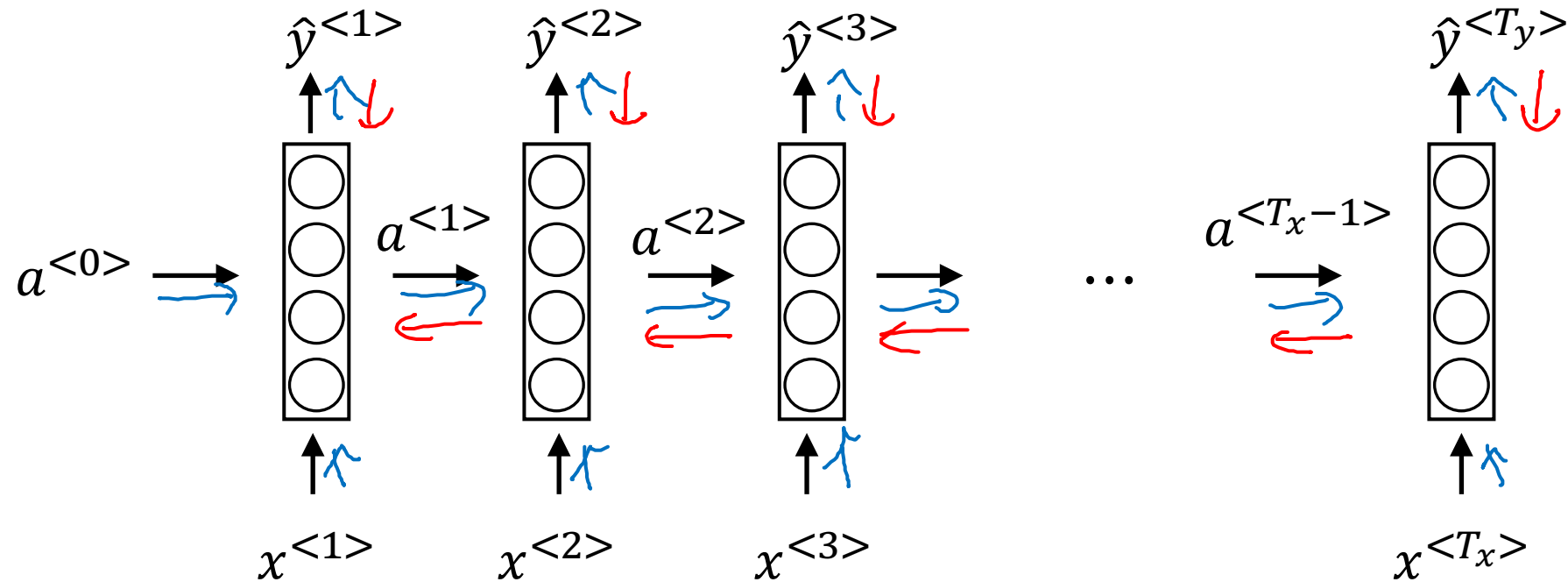


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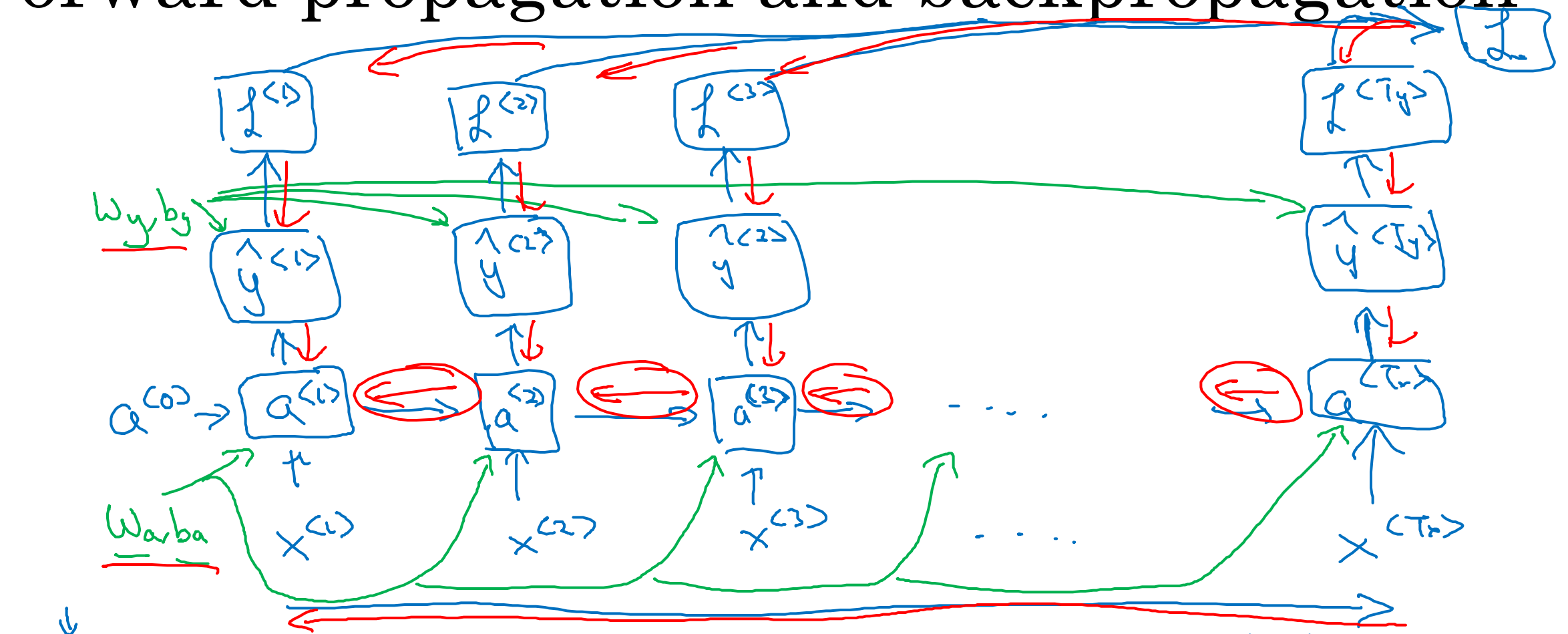
Recurrent Neural Networks

Backpropagation
through time

Forward propagation and backpropagation



Forward propagation and backpropagation



$$\mathcal{L}^{(t)}(\hat{y}^{(t)}, y^{(t)}) = -y^{(t)} \log \hat{y}^{(t)} - (1 - y^{(t)}) \log (1 - \hat{y}^{(t)})$$

$$\mathcal{L}(\hat{y}, y) = \sum_{t=1}^{T_y} \mathcal{L}^{(t)}(\hat{y}^{(t)}, y^{(t)})$$

Backpropagation through time



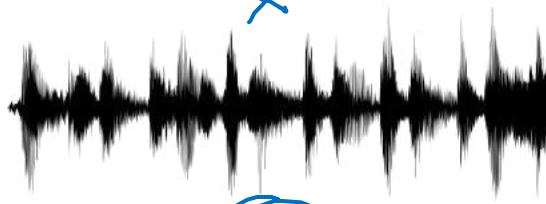
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Recurrent Neural Networks

Different types of RNNs

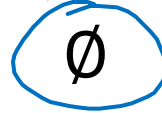
Examples of sequence data

Speech recognition



T_x T_y y
“The quick brown fox jumped over the lazy dog.”

Music generation



Sentiment classification

“There is nothing to like in this movie.”



DNA sequence analysis

AGCCCCTGTGAGGAACTAG



AG**CCCCTGTGAGGAACT**AG

Machine translation

Voulez-vous chanter avec moi?



Do you want to sing with me?

Video activity recognition



Running

Name entity recognition

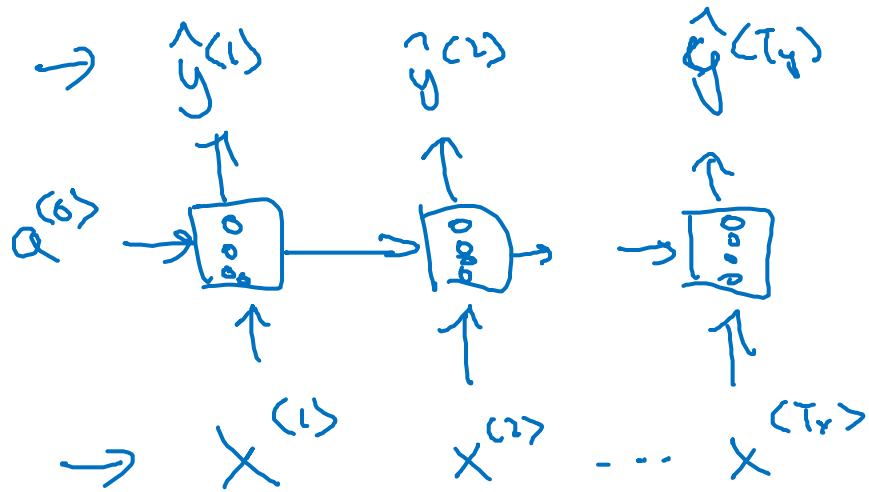
Yesterday, Harry Potter met Hermione Granger.



Yesterday, **Harry Potter** met **Hermione Granger**.

Examples of RNN architectures

$$T_x = T_y$$

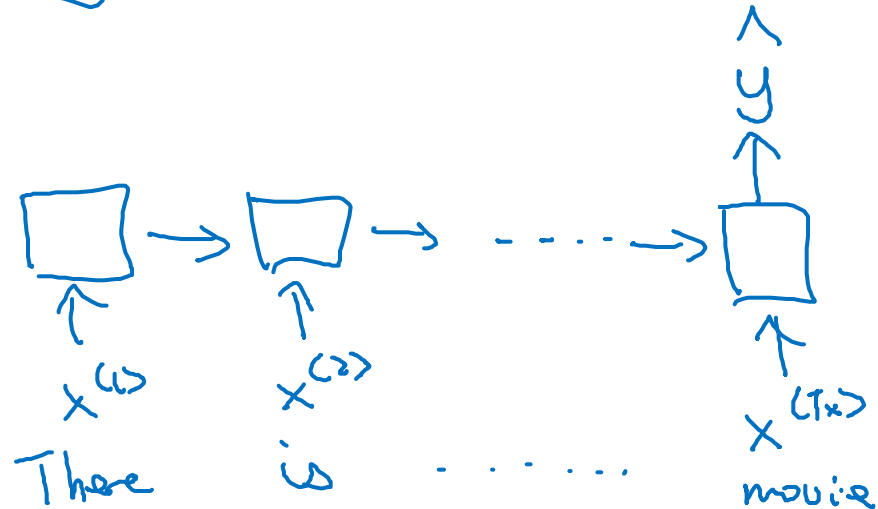


Many-to-many

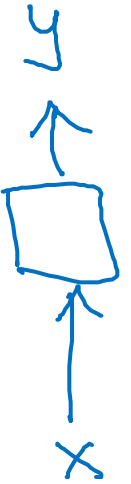
Sentiment classification-

$x = \text{text}$

$y = 0/1 \quad 1 \dots 5$

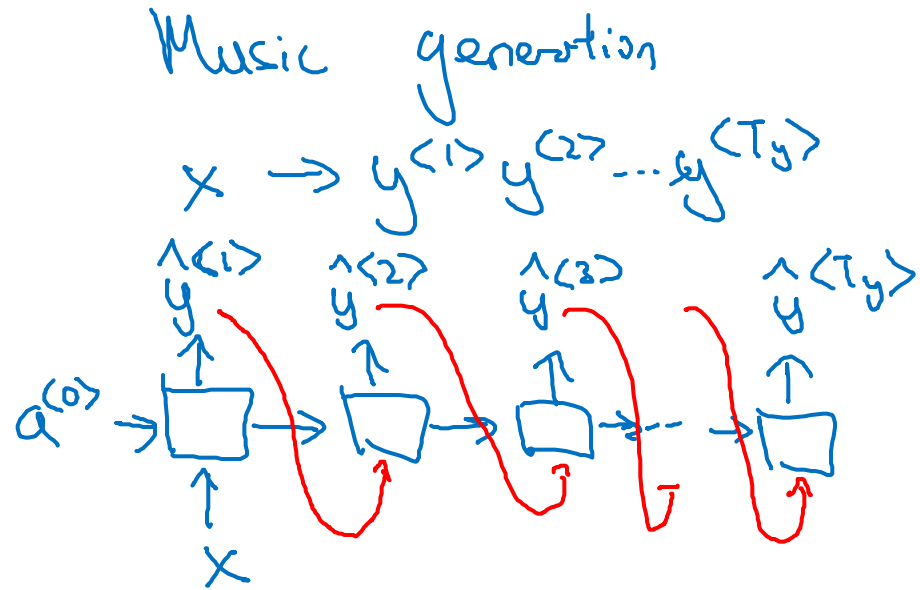


Many-to-one



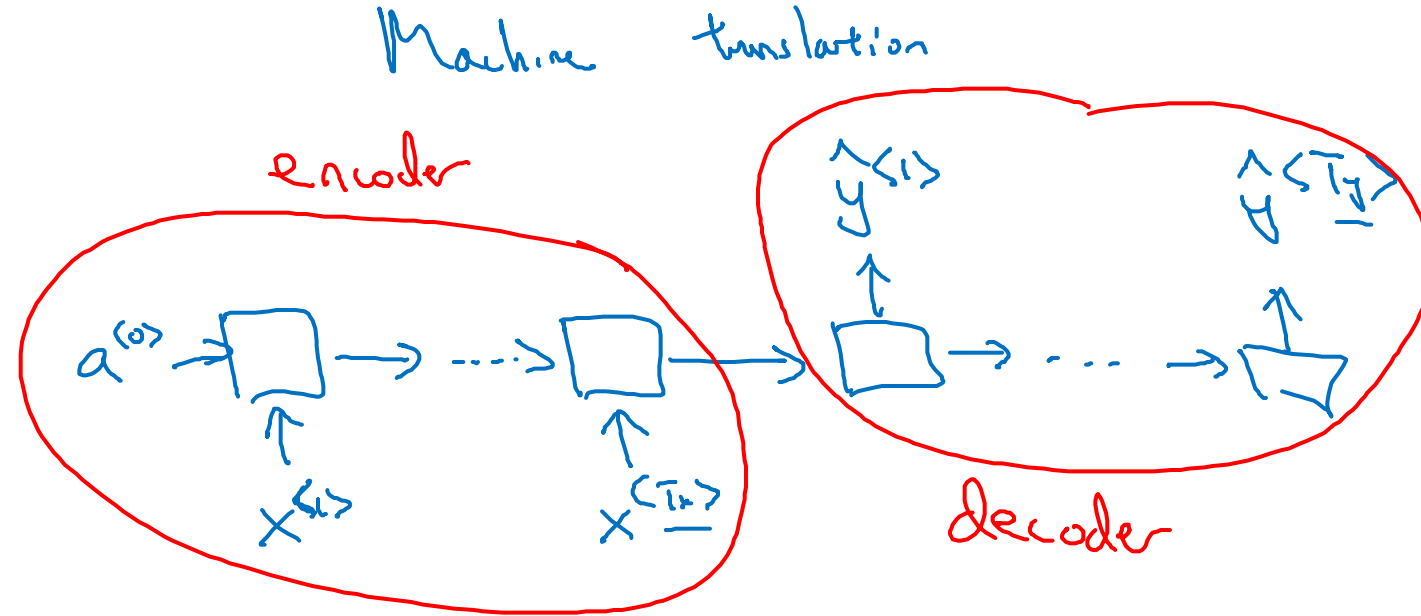
One-to-one

Examples of RNN architectures



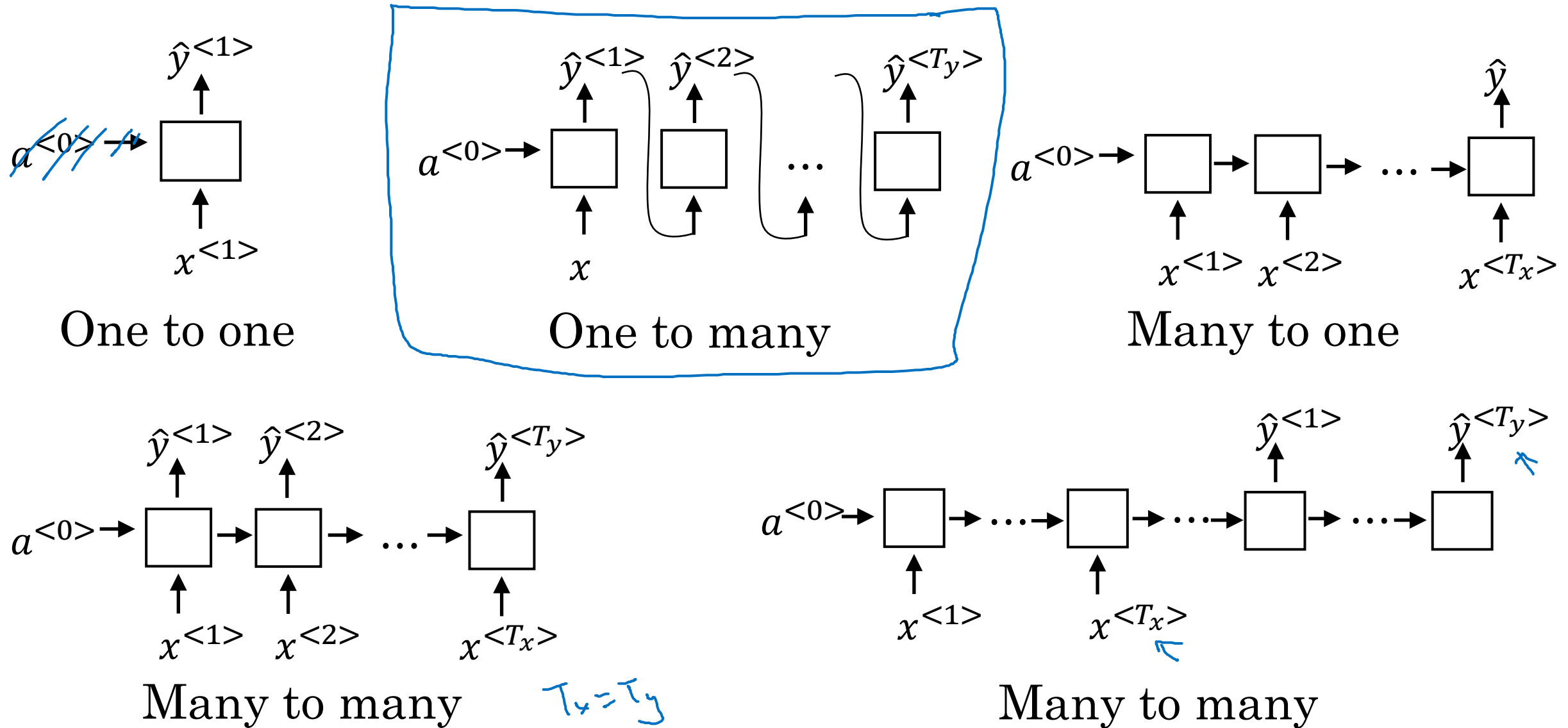
One-to-many

$$x = \phi$$



Many-to-many

Summary of RNN types





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Recurrent Neural Networks

Language model and
sequence generation

What is language modelling?

Speech recognition

The apple and pair salad.

→ The apple and pear salad.

$$P(\text{The apple and pair salad}) = 3.2 \times 10^{-13}$$

$$P(\text{The apple and pear salad}) = 5.7 \times 10^{-10}$$

$$P(\text{Sentence}) = ?$$

$$P(y^{(1)}, y^{(2)}, \dots, y^{(T)})$$

Language modelling with an RNN

Training set: large corpus of english text.

Tokenize

Cats average 15 hours of sleep a day. \downarrow $\langle \text{EOS} \rangle$

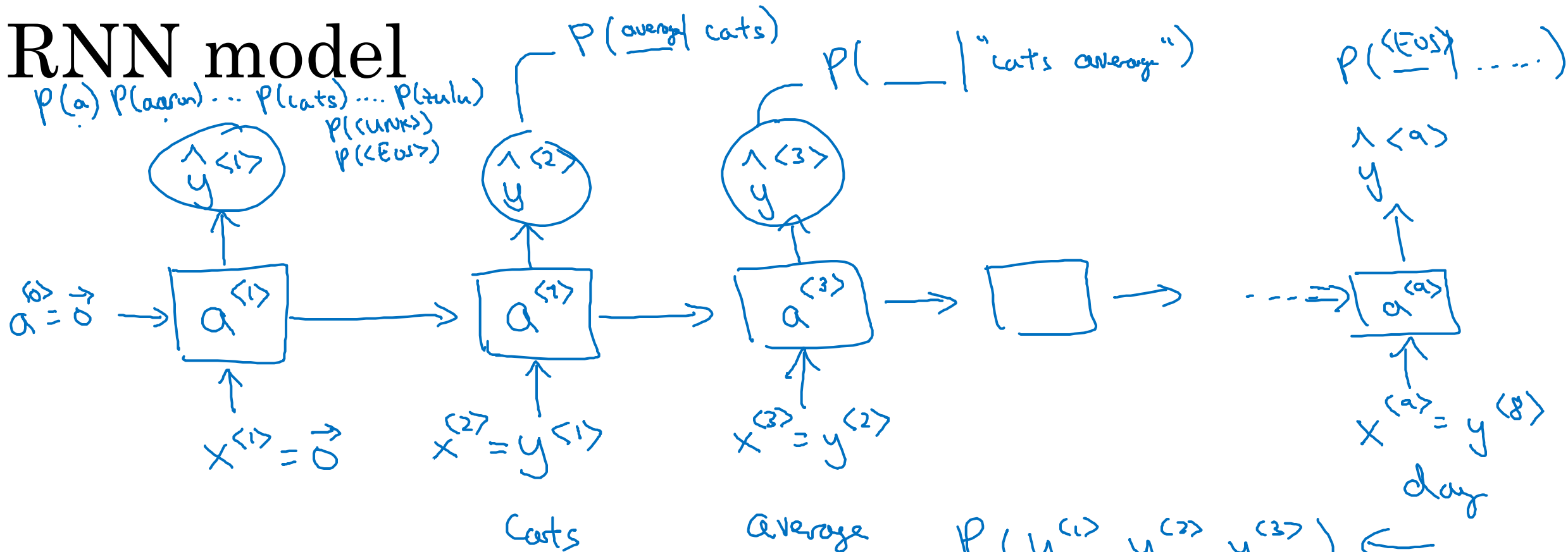
$y^{(1)}$ $y^{(2)}$ $y^{(3)}$... $y^{(8)}$ $y^{(9)}$
 $x^{(t)} = y^{(t-1)}$

The Egyptian ~~Mau~~ is a breed of cat. $\langle \text{EOS} \rangle$

$\langle \text{UNK} \rangle$

10,000

RNN model



→ Cats average 15 hours of sleep a day. <EOS>

$$\mathcal{L}(\hat{y}^{<t>}, y^{<t>}) = - \sum_i y_i^{<t>} \log \hat{y}_i^{<t>}$$

$$\mathcal{L} = \sum_t \mathcal{L}^{<t>}(\hat{y}^{<t>}, y^{<t>})$$

$$p(y^{(1)}, y^{(2)}, y^{(3)}) \leftarrow$$

$$= \frac{p(y^{(1)}) p(y^{(2)} | y^{(1)})}{p(y^{(3)} | y^{(1)}, y^{(2)})}$$

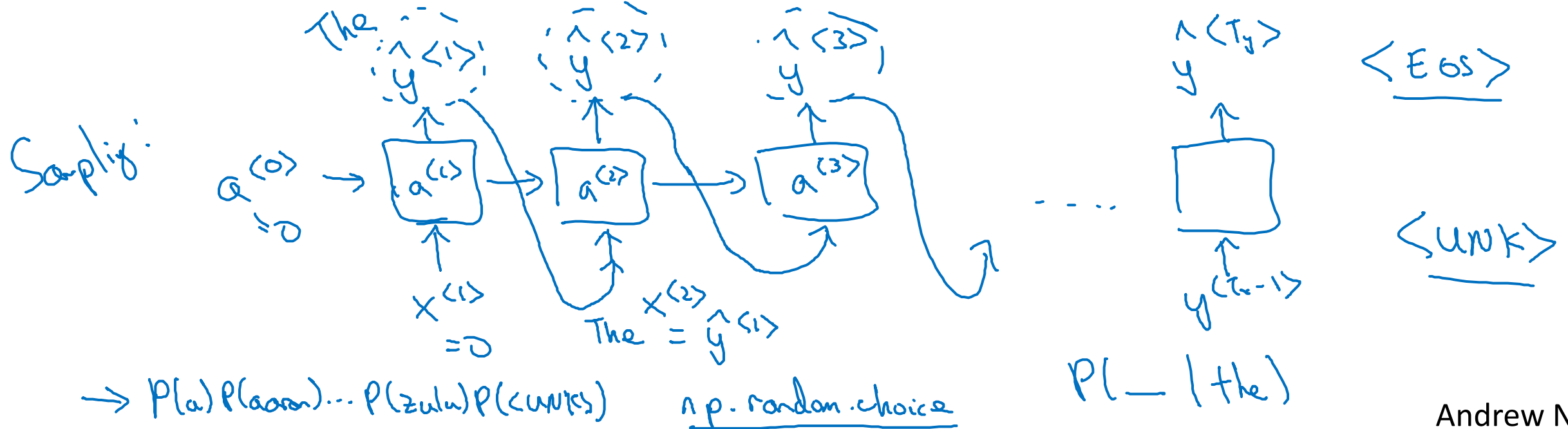
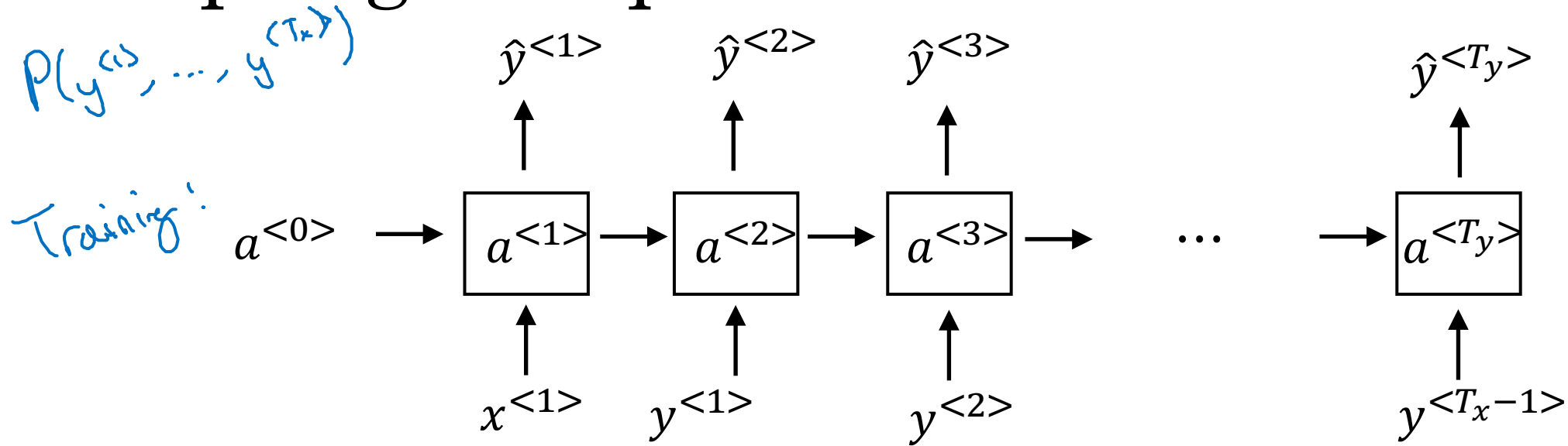


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Recurrent Neural Networks

Sampling novel
sequences

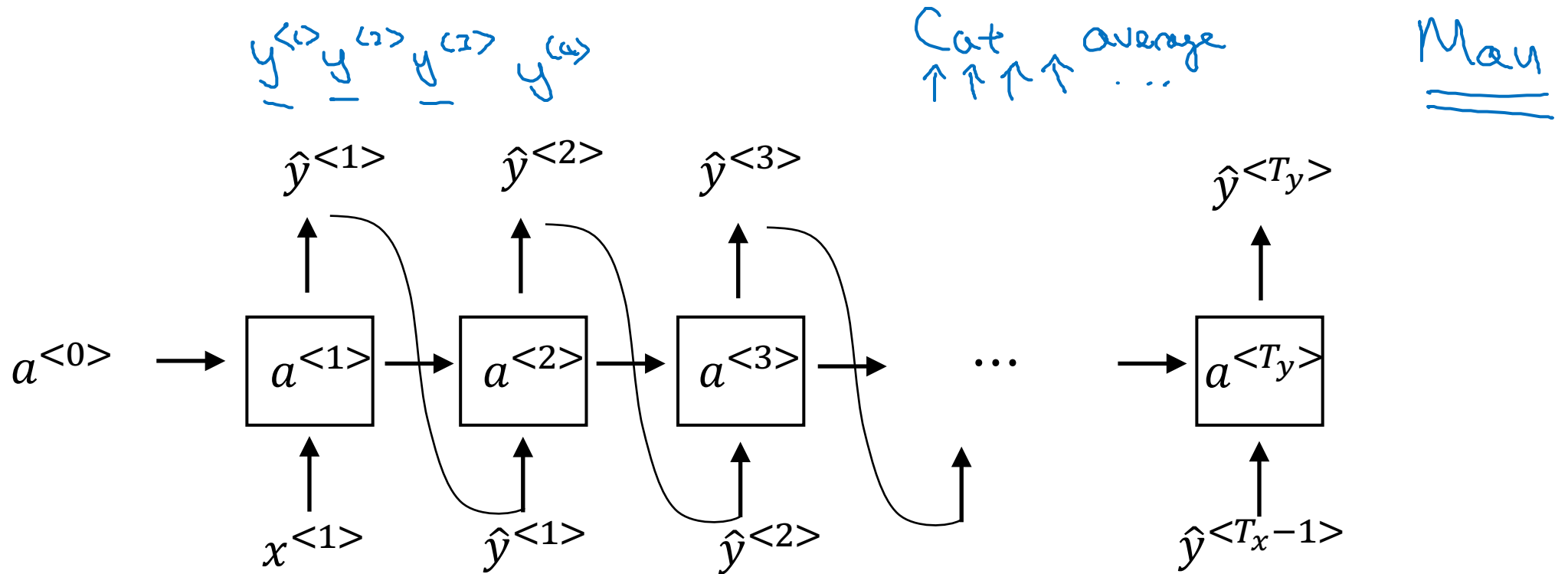
Sampling a sequence from a trained RNN



Character-level language model

→ Vocabulary = [a, aaron, ..., zulu, <UNK>] ←

→ Vocabulary = [a, b, c, ..., z, \backslash , ., , , ; , 0, ..., 9, A, ..., Z]




Sequence generation

News

President enrique peña nieto, announced
sench's sulk former coming football langston
paring.

"I was not at all surprised," said hich langston.

"Concussion epidemic", to be examined. 

The gray football the told some and this has on
the uefa icon, should money as.

Shakespeare

The mortal moon hath her eclipse in love.

And subject of this thou art another this fold.

When besser be my love to me see sabl's.

For whose are ruse of mine eyes heaves.

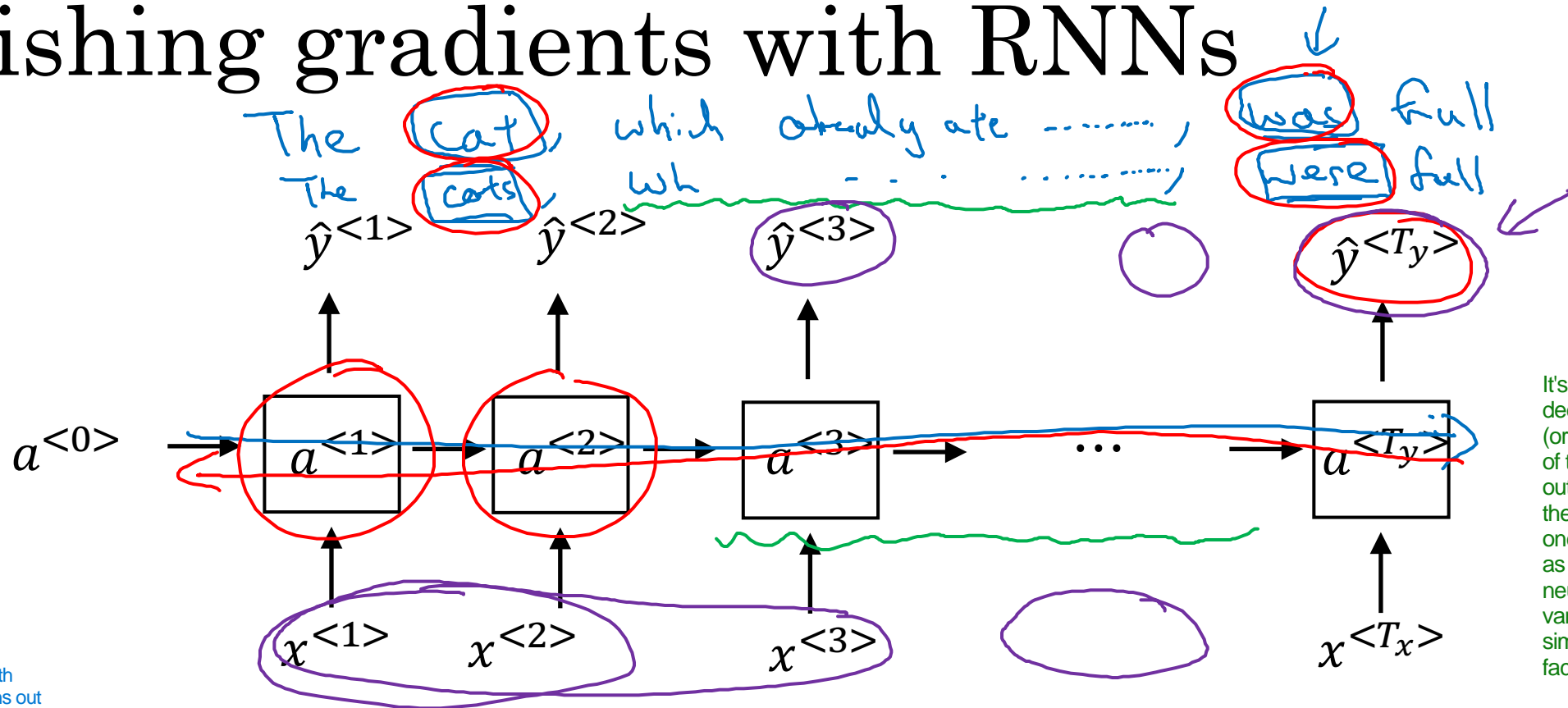


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Recurrent Neural Networks

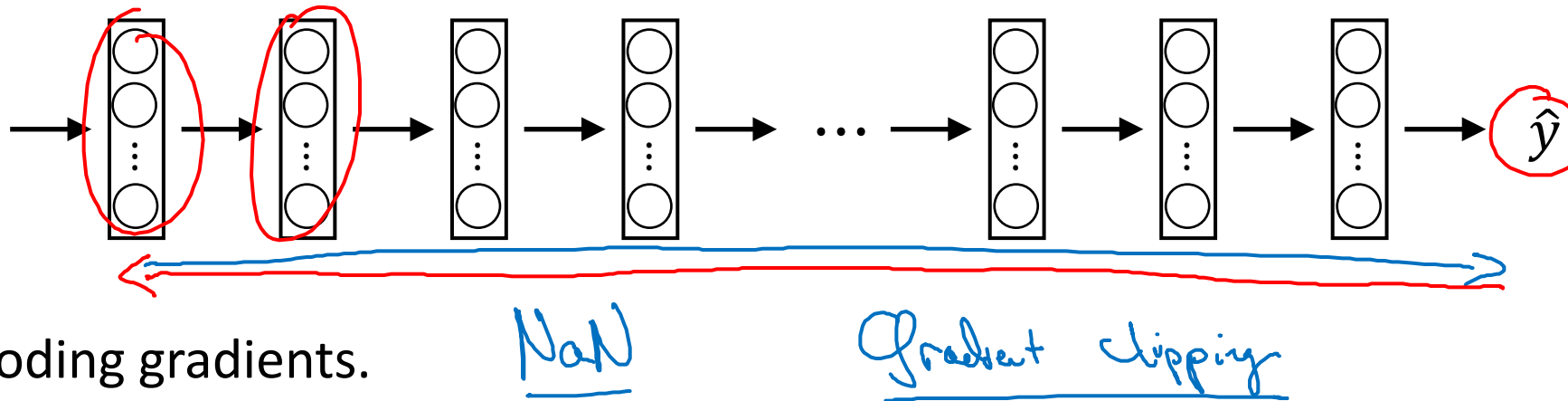
Vanishing gradients with RNNs

Vanishing gradients with RNNs



It's difficult for the outputs of the deeper layers to remember the (or get affected) by the outcome of the shallower layer as the output is greatly influenced by the layers near it rather than the ones that are far from it, hence as we saw with very deep neural networks, the problem of vanishing/exploding gradient, simple RNN architecture also faces similar problem.

Although it is easy to deal with exploding gradients as it turns out that exploding gradients are easier to spot because the parameter has just blow up. You might often see NaNs, not a numbers, meaning results of a numerical overflow in your neural network computation. If you do see exploding gradients, one solution to that is apply gradients clipping. All that means is, look at your gradient vectors, and if it is bigger than some threshold, re-scale some of your gradient vectors so that it's not too big, so that is clipped according to some maximum value



Exploding gradients.

NaN

Gradient clipping

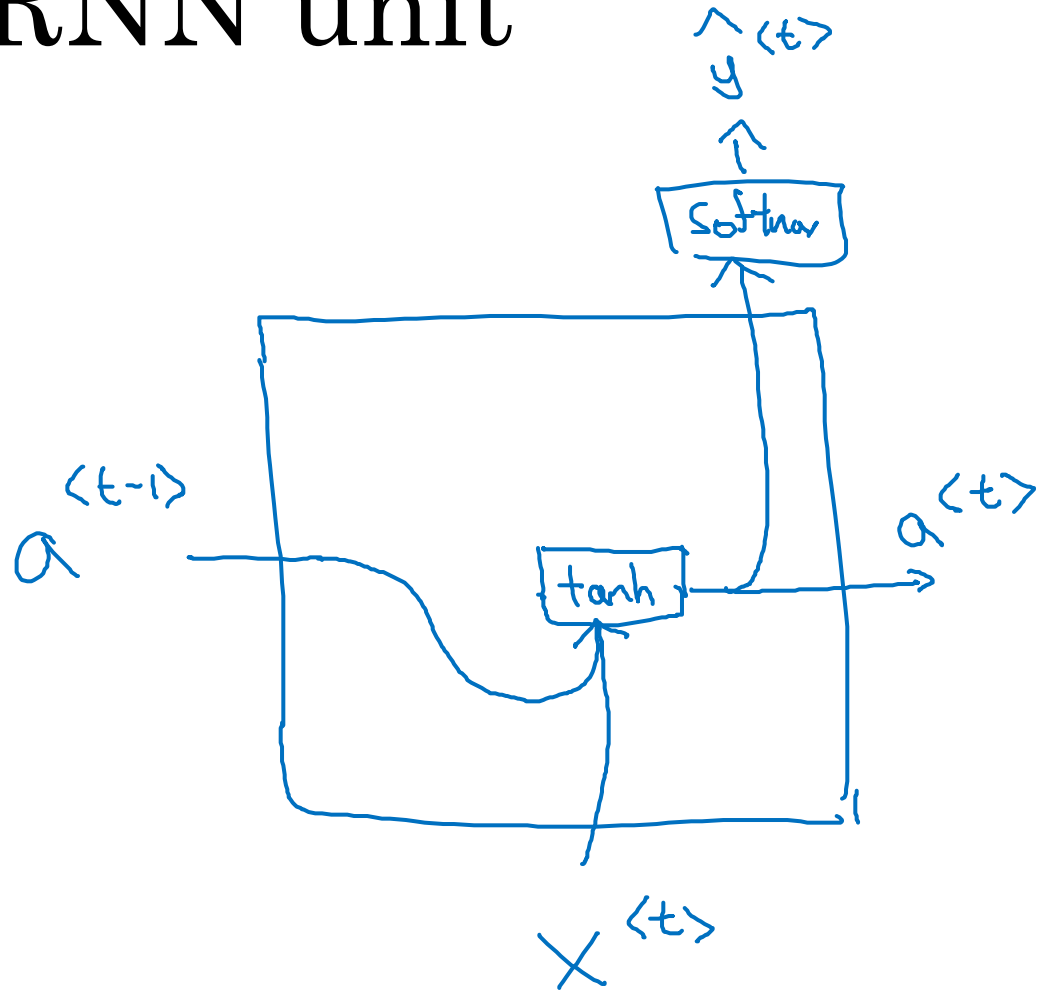


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Recurrent Neural Networks

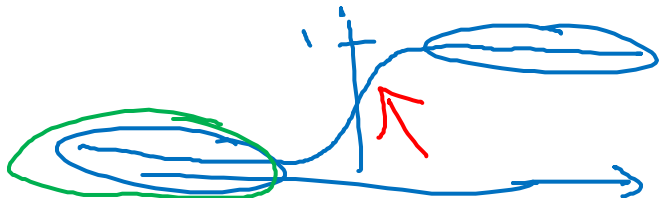
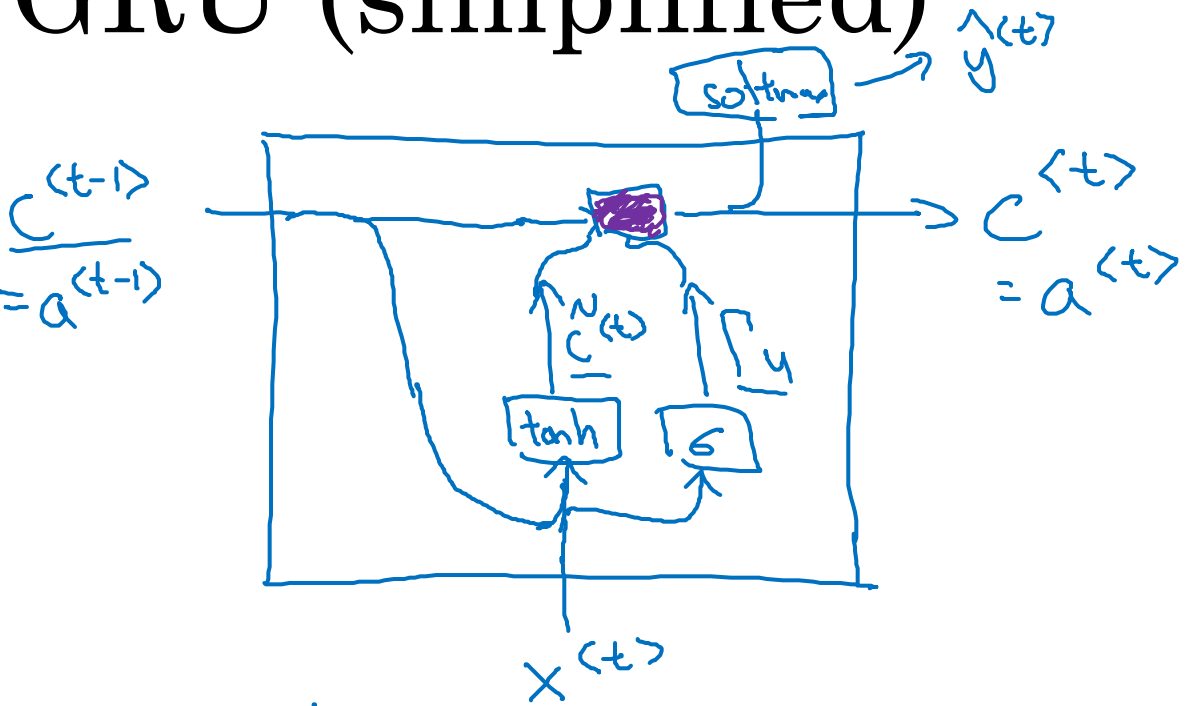
Gated Recurrent Unit (GRU)

RNN unit



$$\underline{a^{<t>}} = \overset{\substack{\text{tanh} \\ \downarrow}}{g}(\underbrace{W_a[a^{<t-1>}, x^{<t>}]}_{\uparrow} + b_a)$$

GRU (simplified)



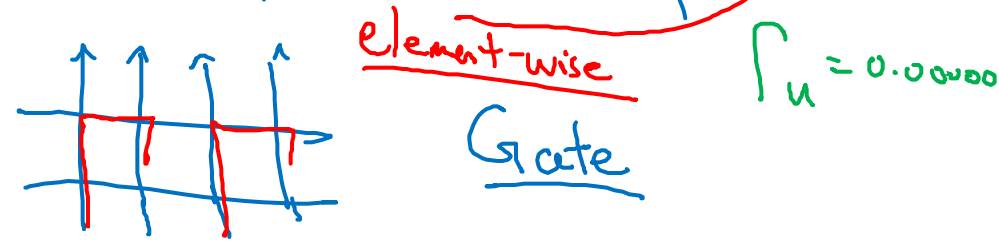
C = memory cell

$\rightarrow \underline{C}^{(t)} = \underline{a}^{(t)}$

$\rightarrow \tilde{C}^{(t)} = \tanh(W_c [C^{(t-1)}, x^{(t)}] + b_c)$

$\rightarrow \Gamma_u = \sigma(W_u [C^{(t-1)}, x^{(t)}] + b_u)$

$\rightarrow \underline{C}^{(t)} = \Gamma_u * \tilde{C}^{(t)} + (1 - \Gamma_u) * \underline{C}^{(t-1)}$



$\Gamma_u = 1$
 $\underline{C}^{(t)} = 1$
 $\Gamma_u = 0 \quad \Gamma_u = 0 \quad \Gamma_u = 0 \quad \dots$
The cat, which already ate ..., was full.

[Cho et al., 2014. On the properties of neural machine translation: Encoder-decoder approaches]

[Chung et al., 2014. Empirical Evaluation of Gated Recurrent Neural Networks on Sequence Modeling]

Full GRU

$$\tilde{c}^{<t>} = \tanh(W_c [\tilde{c}^{<t-1>}, x^{<t>}] + b_c)$$

$$\Gamma_u = \sigma(W_u [c^{<t-1>}, x^{<t>}] + b_u)$$

$$\Gamma_r = \sigma(W_r [c^{<t-1>}, x^{<t>}] + b_r)$$

$$c^{<t>} = \Gamma_u * \tilde{c}^{<t>} + (1 - \Gamma_u) * c^{<t-1>}$$

LSTM

The cat, which ate already, was full.



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Recurrent Neural Networks

LSTM (long short
term memory) unit

GRU and LSTM

GRU

$$\underline{\tilde{c}^{<t>}} = \tanh(W_c[\underline{\Gamma_r} * \underline{c^{<t-1>}}, x^{<t>}] + b_c)$$

$$\underline{\Gamma_u} = \sigma(W_u[\underline{c^{<t-1>}}, x^{<t>}] + b_u)$$

$$\underline{\Gamma_r} = \sigma(W_r[\underline{c^{<t-1>}}, x^{<t>}] + b_r)$$

$$\underline{c^{<t>}} = \underline{\Gamma_u} * \underline{\tilde{c}^{<t>}} + \underline{(1 - \Gamma_u)} * \underline{c^{<t-1>}}$$

$\underline{a^{<t>}} = \underline{c^{<t>}}$

\uparrow
 Γ_f

LSTM

$$\underline{\tilde{c}^{<t>}} = \tanh(W_c[a^{<t-1>}, x^{<t>}] + b_c)$$

(update) $\Gamma_u = \sigma(W_u[a^{<t-1>}, x^{<t>}] + b_u)$

(forget) $\Gamma_f = \sigma(W_f[a^{<t-1>}, x^{<t>}] + b_f)$

(output) $\Gamma_o = \sigma(W_o[a^{<t-1>}, x^{<t>}] + b_o)$

$$\underline{c^{<t>}} = \underline{\Gamma_u} * \underline{\tilde{c}^{<t>}} + \underline{\Gamma_f} * \underline{c^{<t-1>}}$$

$$\underline{a^{<t>}} = \underline{\Gamma_o} * \underline{c^{<t>}}$$

LSTM units

GRU

$$\tilde{c}^{<t>} = \tanh(W_c[\Gamma_r * c^{<t-1>}, x^{<t>}] + b_c)$$

$$\Gamma_u = \sigma(W_u[c^{<t-1>}, x^{<t>}] + b_u)$$

$$\Gamma_r = \sigma(W_r[c^{<t-1>}, x^{<t>}] + b_r)$$

$$c^{<t>} = \Gamma_u * \tilde{c}^{<t>} + (1 - \Gamma_u) * c^{<t-1>}$$

$$a^{<t>} = c^{<t>}$$

LSTM

$$\tilde{c}^{<t>} = \tanh(W_c[a^{<t-1>}, x^{<t>}] + b_c)$$

$$\Gamma_u = \sigma(W_u[a^{<t-1>}, x^{<t>}] + b_u)$$

$$\Gamma_f = \sigma(W_f[a^{<t-1>}, x^{<t>}] + b_f)$$

$$\Gamma_o = \sigma(W_o[a^{<t-1>}, x^{<t>}] + b_o)$$

$$c^{<t>} = \Gamma_u * \tilde{c}^{<t>} + \Gamma_f * c^{<t-1>}$$

$$a^{<t>} = \Gamma_o * c^{<t>}$$

LSTM in pictures

$$\tilde{c}^{<t>} = \tanh(W_c[a^{<t-1>}, x^{<t>}] + b_c)$$

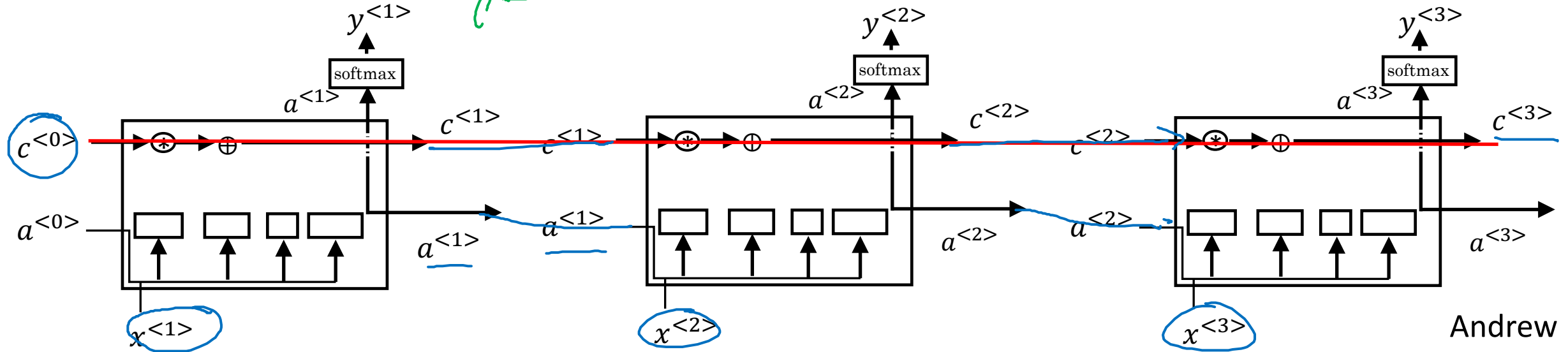
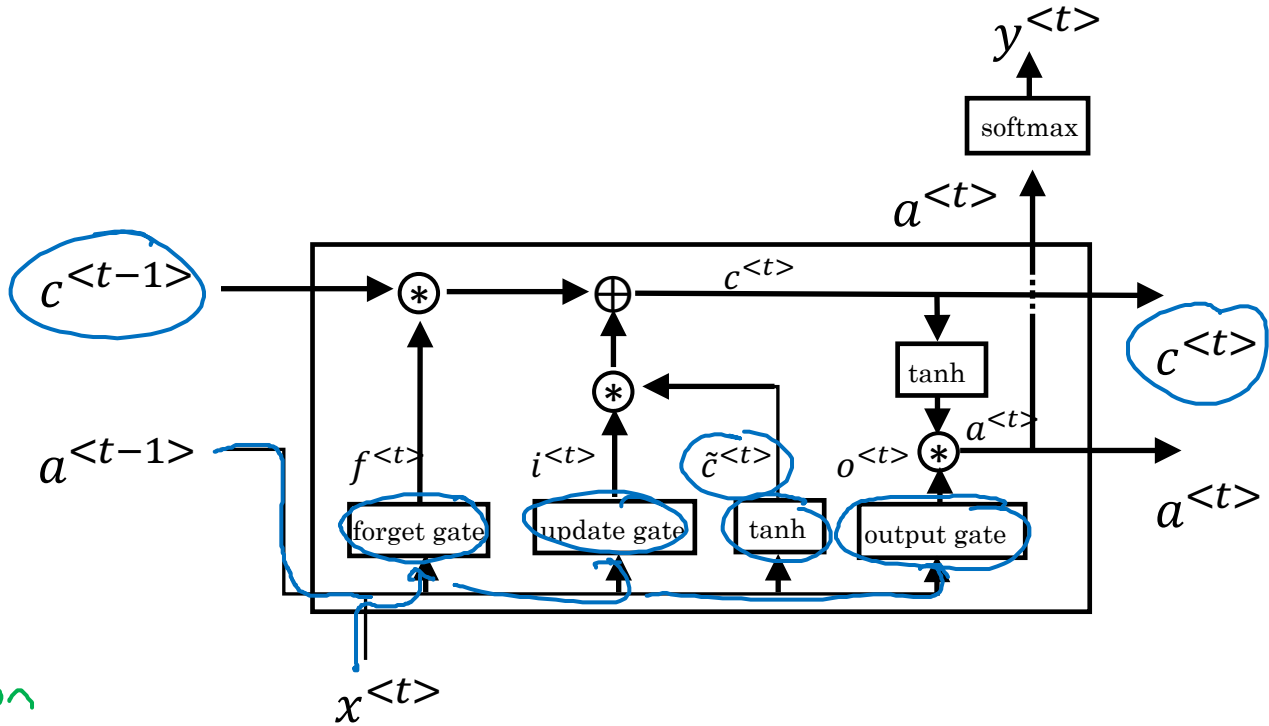
$$\rightarrow \Gamma_u = \sigma(W_u[\underbrace{a^{<t-1>}, x^{<t>}}_{\text{input}}, b_u])$$

$$\rightarrow \Gamma_f = \sigma(W_f[\underline{a^{<t-1>}, x^{<t>}}] + b_f)$$

$$\rightarrow \Gamma_o = \sigma(W_o[\underline{a^{<t-1>}, x^{<t>}}]) + b_o)$$

$$c^{<t>} = \Gamma_u * \tilde{c}^{<t>} + \Gamma_f * c^{<t-1>}$$

$$a^{<t>} = \Gamma_o * c^{<t>}$$





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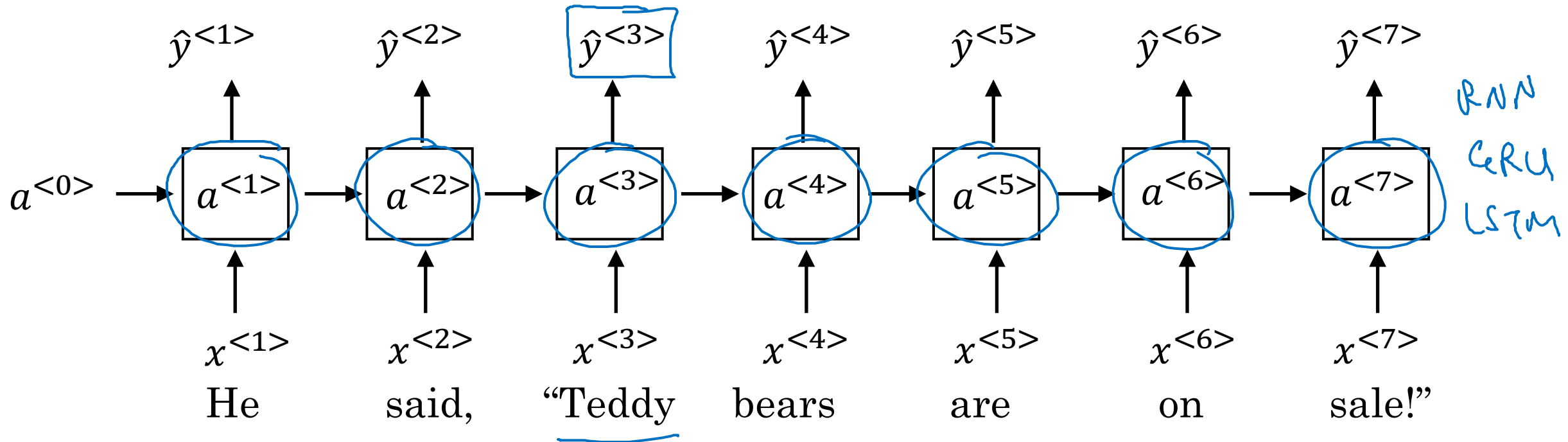
Recurrent Neural Networks

Bidirectional RNN

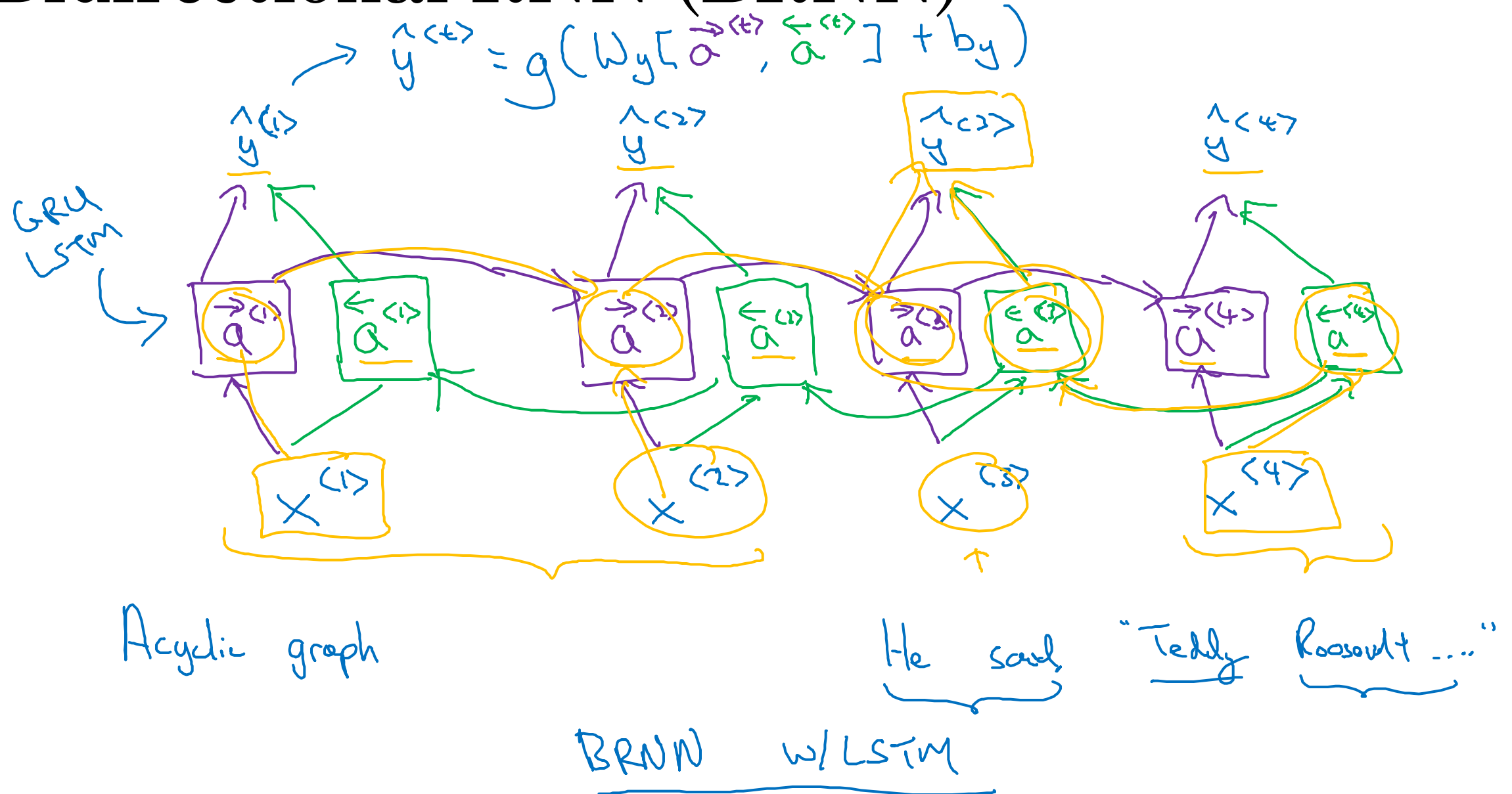
Getting information from the future

He said, “Teddy bears are on sale!”

He said, “Teddy Roosevelt was a great President!”



Bidirectional RNN (BRNN)



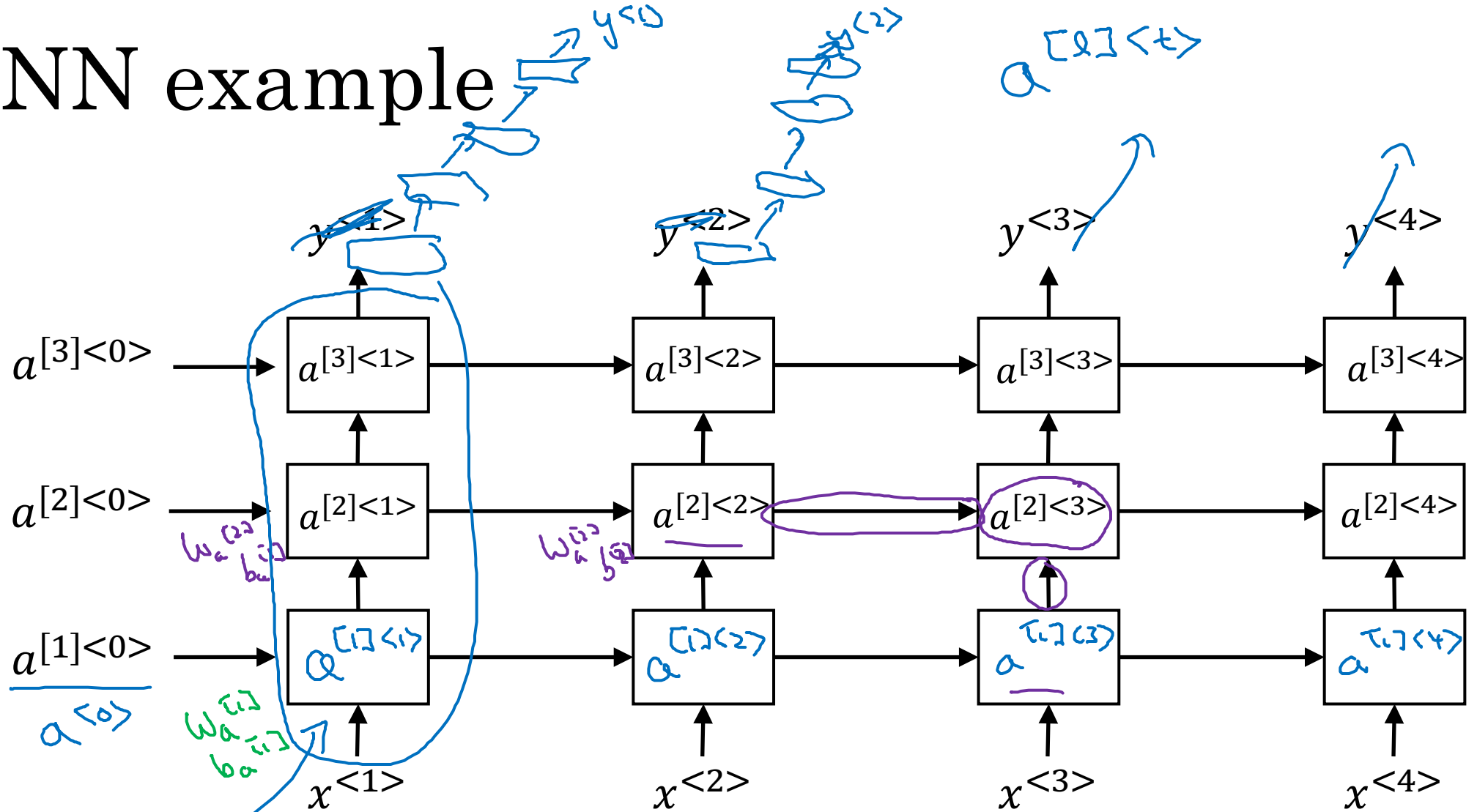
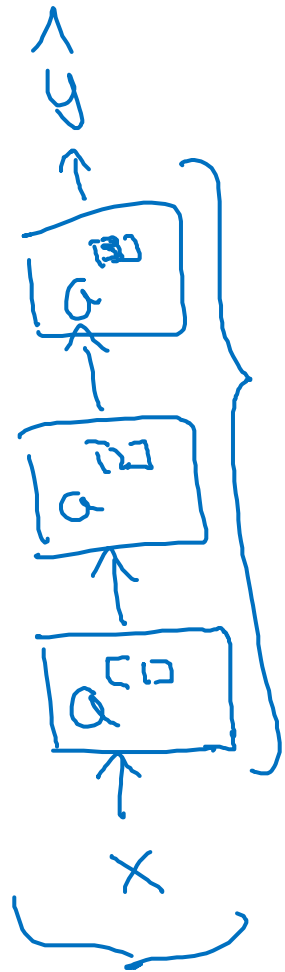


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Recurrent Neural Networks

Deep RNNs

Deep RNN example



$$a^{[2] \langle 3 \rangle} = g (w_a^{[2]} [a^{[1] \langle 2 \rangle}, a^{[1] \langle 3 \rangle}] + b_a^{[1]})$$

RNN
GRU
LSTM

BROWN