

QUANTUM COMPUTING BASED ENSEMBLE CLASSIFICATION

*Minor project report submitted
in partial fulfillment of the requirement for award of the degree of*

**Bachelor of Technology
in
Computer Science & Engineering**

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**VEL TECH RANGARAJAN DR. SAGUNTHALA R&D INSTITUTE OF
SCIENCE & TECHNOLOGY**

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June , 2022

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ABSTRACT

Ensemble learning is the process by which multiple models, such as classifiers or experts, are strategically generated and combined to solve a particular computational intelligence problem. Ensemble learning is primarily used to improve the classification performance. We use the forest.qvm device to simulate one QPU and the qiskit.aer device to simulate another. Each QPU makes an independent prediction, and an ensemble model is formed by choosing the prediction of the most confident QPU. The iris dataset is used in this project, consisting of three classes of iris flower. The TensorFlow quantum package was used to add the outcomes of the quantum circuits to dense layers for efficient classification. A different number of quantum filters were used in the HQCNN model and tested. A different number of quantum filters were used in the HQCNN model design. The performance of the HQCNN models with the different number of quantum filters was compared using validation and testing performance.

Keywords: Quantum Machine learning, Quantum Computing, Ensemble Classification, Iris Flower, Fully connected layer

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LIST OF ACRONYMS AND ABBREVIATIONS

IDE	Integrated Development Environment
OS	Operating system
QCNN	Quantum Convolutional Neural Network
QML	Quantum Machine Learning
QPU	Quantum Processing Unit
QVSM	Quantum Vector Support Machine
SPT	Symmetry Protected Topological

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Chapter 1

INTRODUCTION

1.1 Introduction

Quantum machine learning is a research area that explores the interplay of ideas from quantum computing and machine learning. Quantum machine learning extends the pool of hardware for machine learning by an entirely new type of computing device — the quantum computer. Information processing with quantum computers relies on substantially different laws of physics known as quantum theory. We use the `forest.qvm` device to simulate one QPU and the `qiskit.aer` device to simulate another. Each QPU makes an independent prediction, and an ensemble model is formed by choosing the prediction of the most confident QPU. The iris dataset is used in this consisting of three classes of iris flower. Using a pre-trained model and the PyTorch interface, we'll see that ensembling allows the QPUs to specialize towards different classes.

In the modern viewpoint, quantum computers can be used and trained as like neural networks. We can systematically adapt the physical control parameters, such as an electromagnetic field strength or a laser pulse frequency, to solve a problem. For example, a trained circuit can be used to classify the content of images, and by encoding the image into the physical state of the device and taking measurements.

1.2 Aim of the project

To implement the ensemble learning techniques using quantum computing approach. To enhance the model predictions using ensemble learning on multi class classification

1.3 Project Domain

The project focuses on the Quantum Computing based ensemble classification.

1.4 Scope of the Project

Developing a novel ensemble learning technique using quantum circuits and machine learning algorithms for image classification on quantum data. Develop multiple QPUs for classification applications

Chapter 2

LITERATURE REVIEW

Quantum computing is a recent computing technique inspired by quantum physics to solve computing problems using quantum state properties such as superposition, interference, and entanglement [1]. Artificial neural networks are powerful techniques to solve modern decision-making challenges such as classification, time series forecasting and natural language processing [2]. Also, advanced neural networks like Convolutional Neural Network (CNN) and Recurrent Neural Networks (RNN) need more powerful computational tools than traditional computing systems to handle complex data [3]. The combination of recent artificial.

Neural networks and quantum computing techniques may extend the decision-making capabilities of modern computers [4]. The integrated quantum states and convolutional neural network is named a hybrid quantum convolutional neural network (HQCNN). The quantum-inspired convolutional and pooling layers are the elements of the quantum filter. It performs the convolutional and pooling operations like standard CNNs[5]. Multiple numbers of quantum filters can be connected to the quantum state in the HQCNN model for the feature extraction process. The number of quantum filters for the HQCNN model should be optimized based on the dataset and architecture of the model.

[6] This research combines the quantum states and CNN with the optimized number of quantum filters to handle classification tasks. In this article, we begin with the short introduction and application of a hybrid quantum CNN. Section 2 reviews the recent developments and applications of hybrid quantum neural networks. Section 3 explains the construction of the proposed HQCNN model for the Symmetry-Protected Topological (SPT) phase classification task. Section 4 compares the performance of the proposed HQCNN using the different number of quantum filters on test data. At last, section 5 concludes the outcomes of the research with future suggestions. Quantum computing is used in numerous domains such as neural networks, cryptography and network security to improve performance and processing capabilities. This short literature survey focused on the applications of quantum computing in neural network development on classification tasks. Several neural network ap-

plications are developed using quantum circuits and states. Some of the applications are discussed in this section. The significance of the quantum inspired deep convolutional neural network (QDCNN) on image classification tasks is studied using standard datasets in [7,8]. The authors identified the QDCNN achieves better performance than the traditional CNN models on image classification applications. In [9], the authors proposed a quantum matched-filter technique and deep spiking neural network for segmentation of tumor region in the scanned images. They optimized the quantum matched-filter technique to improve the performance of the task. They achieved an average accuracy of 98.21 percent on test data. The authors in [10], proposed a remote sensed hyperspectral data classification technique using CNN model with quantum genetic technique. They used the quantum genetic technique for creating a sparse feature matrix for achieving improved performance on hyperspectral data classification. A conversational sentiment analysis technique using quantum-inspired CNN and Long short-term memory (LSTM) was proposed by the authors in [11]. The experimental result of the technique shows the importance of quantum-inspired neural network model development. In [12], the authors proposed a facial expressions detection technique using a quantum-inspired search technique. They named the technique is Quantum-inspired binary gravitational search technique to detect seven different emotions by the facial appearance. The authors in [13], proposed a quantuminspired Particle Swarm Optimization (PSO) technique for enhancing CNN models. The quantuminspired PSO optimized CNN model performs better than traditional CNN models. A Quantum Generative Adversarial Network (QGAN) to generate small gray-scale images was proposed by the authors in [14]. The image generation on high dimensional space was completed in parallel using the QGAN model. The next section briefly discussed the SPT phase dataset preparation, hybrid model development and the model training processes.

Chapter 3

PROJECT DESCRIPTION

3.1 Existing System

A novel hybrid quantum convolutional neural network was proposed in this section to classify the binary class data. The TensorFlow quantum framework was used to implement the proposed HQCNN model for classification. The implementation of the proposed HQCNN was performed on a GPU environment. The implementation process consists of three steps. At first, the data collection step collects the STP phase data. In the second step, the quantum cluster was designed for the convolutional and pooling process. Finally, the HQCNN model was developed for the STP phase classification. The upcoming sub-sections were extensively discussed about each step of the implementation process.

3.2 Proposed System

To implement the ensemble learning techniques using quantum computing approach. To enhance the model predictions using ensemble learning on multi class classification. Developing a novel ensemble learning technique using quantum circuits and machine learning algorithms for image classification on quantum data. Develop multiple QPUs for classification applications

3.3 Feasibility Study

This phase examines the design's practicality, and business proposals are presented with a comprehensive design plan and some cost estimates. The feasibility study of the proposed system should be conducted during system analysis. This is to ensure that the planned system will not cause the organisation any problems. A basic understanding of the system's major conditions is required for feasibility analysis. The feasibility analysis takes into account three important factors.

3.3.1 Economic Feasibility

This project is carried out to check the economic impact that the system will have on the organization. The amount of funds that the company can pour into their search and development of the system is limited. The expenditures must be justified. Thus, the developed system as well within the budget and this was achieved because most of the technologies used are freely available. Only the customized products had to be purchased.

3.3.2 Technical Feasibility

This project is carried out to check the technical feasibility, that is, the technical requirements of the system. Any system developed must not have a high demand on the available technical resources. This will lead to high demands on the available technical resources. This will lead to high demands being placed on the client. The developed system must have a modest requirement, as only minimal or null changes are required for implementing this system.

3.3.3 Social Feasibility

The aspect of the project is to check the level of acceptance of the system by the user. This includes the process of training the user to use the system efficiently. The user must not feel threatened by the system, instead must accept it as a necessity. The level of acceptance by the users solely depends on the methods that are employed to educate the user about the system and to make him familiar with it. His level of confidence must be raised so that he is also able to make some constructive criticism, which is welcomed, as he is the final user of the system.

3.4 System Specification

3.4.1 Hardware Specification

- PROCESSOR:I3/INTEL PROCESSOR
- RAM:8GB
- HARDDISK:160GB

3.4.2 Software Specification

- OS: WINDOWS 10
- SERVER SCRIPT: PYTHON
- IDE: GOOGLE COLAB FOR RUNNING QUANTUM MACHINE LEARNING CODES

3.4.3 Standards and Policies

Anaconda Prompt

Anaconda prompt is a type of command line interface which explicitly deals with the ML(MachineLearning) modules.And navigator is available in all the Windows,Linux and MacOS.The anaconda prompt has many number of IDE's which make the coding easier. The UI can also be implemented in python.

Standard Used: ISO/IEC 10918-1:1994

Jupyter

It's like an open source web application that allows us to share and create the documents which contains the live code, equations, visualizations and narrative text. It can be used for data cleaning and transformation, numerical simulation, statistical modeling, data visualization, machine learning.

Standard Used: ISO/IEC WD TR 24772-4

Chapter 4

METHODOLOGY

4.1 General Architecture

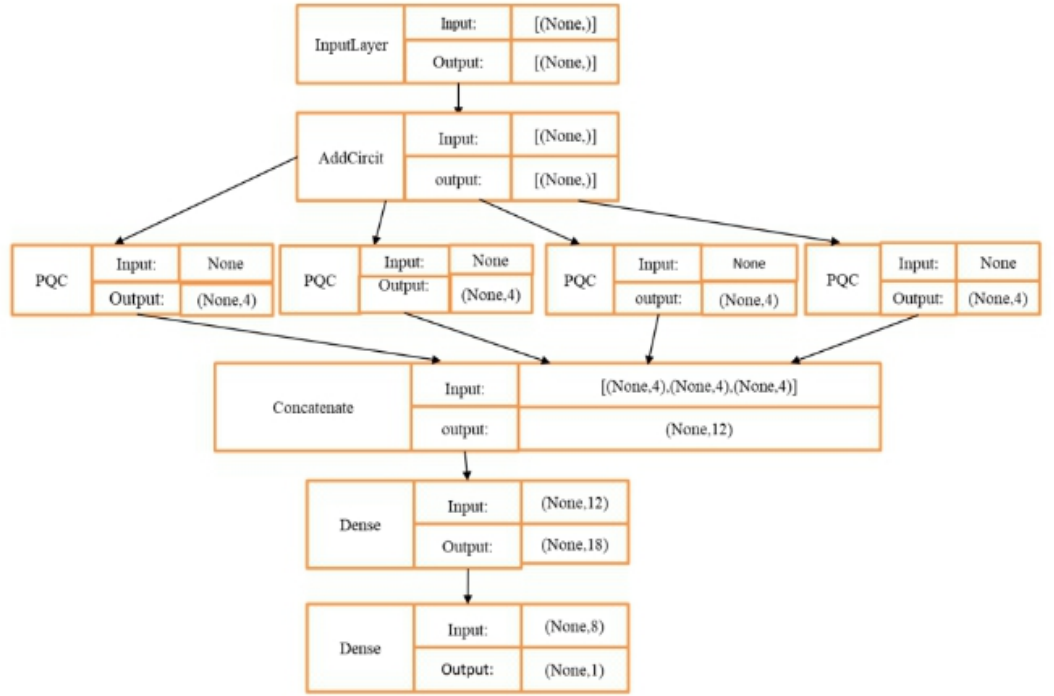


Figure 4.1: General Architecture

The HQCNN model was extended with four parallelconnected quantum filters. The model was named HQCNN4QF. The outputs of the four parallel-connected quantum filters are combined using a concatenation layer. The concatenation layer output was forwarded to the dense layers of the HQCNN-4QF model. Fig. 4.1 shows the layered architecture of the proposed HQCNN-4QF model for SPT phase data classification. The HQCNN-4QF model was trained to 300 epochs on a GPU environment. The accuracy of the HQCNN-4QF model on training and validation data

4.2 Design Phase

4.2.1 Data Flow Diagram

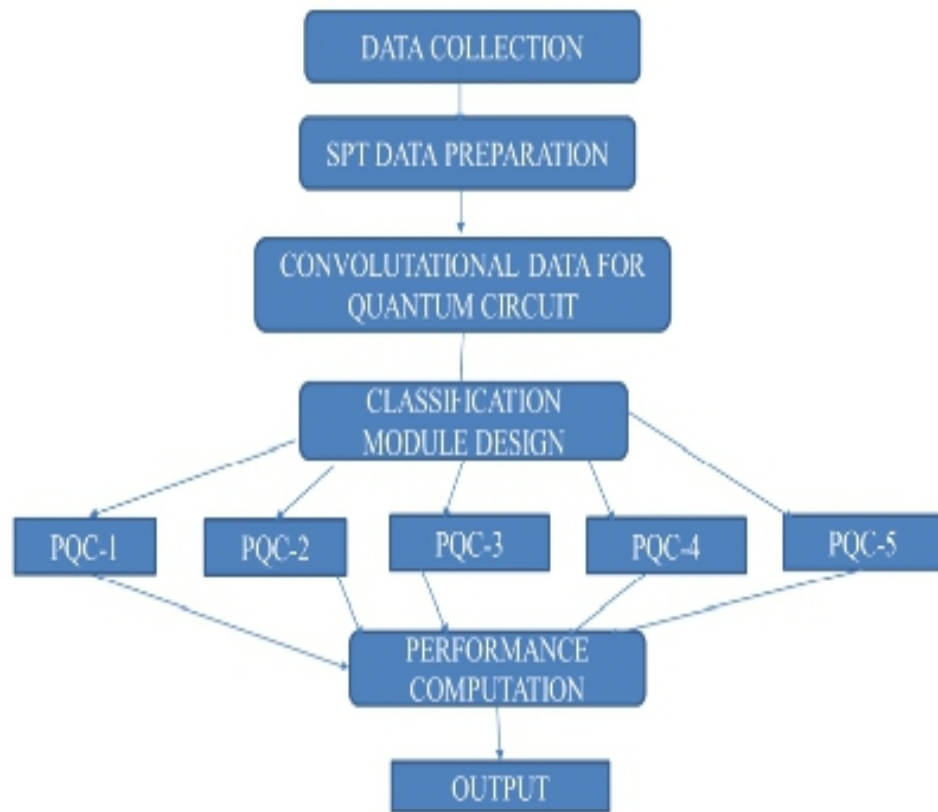


Figure 4.2: Data Flow Diagram

Once the data was collected and the data will go to Pre-processing model for the SPT data preparation. Then the data will pass through linear regressor and random convolutional neural network and the train and testing data will be achieved and the output will represent as graphical representation.

4.2.2 Use Case Diagram

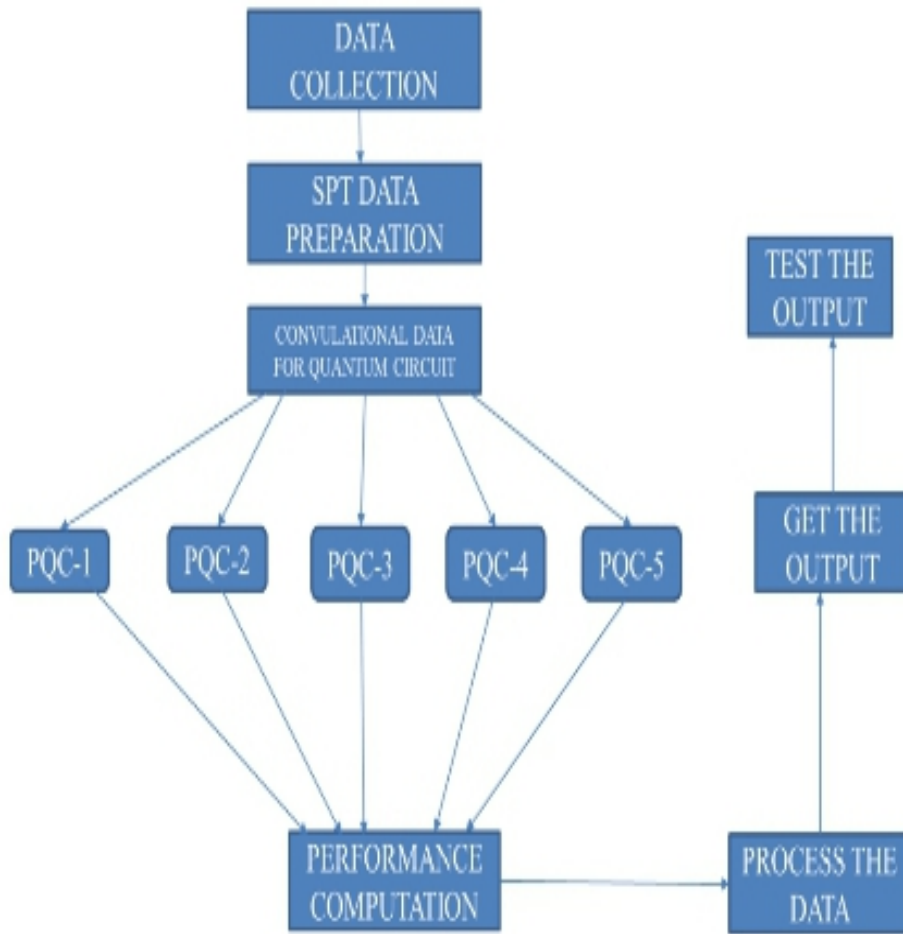


Figure 4.3: Use Case Diagram

All the models like SPT data preparation, Convolutional data for quantum circuit, PQC, Performance computation, process the data and result analysis are to be get the output and to be passed to the test the output.

4.2.3 Sequence Diagram

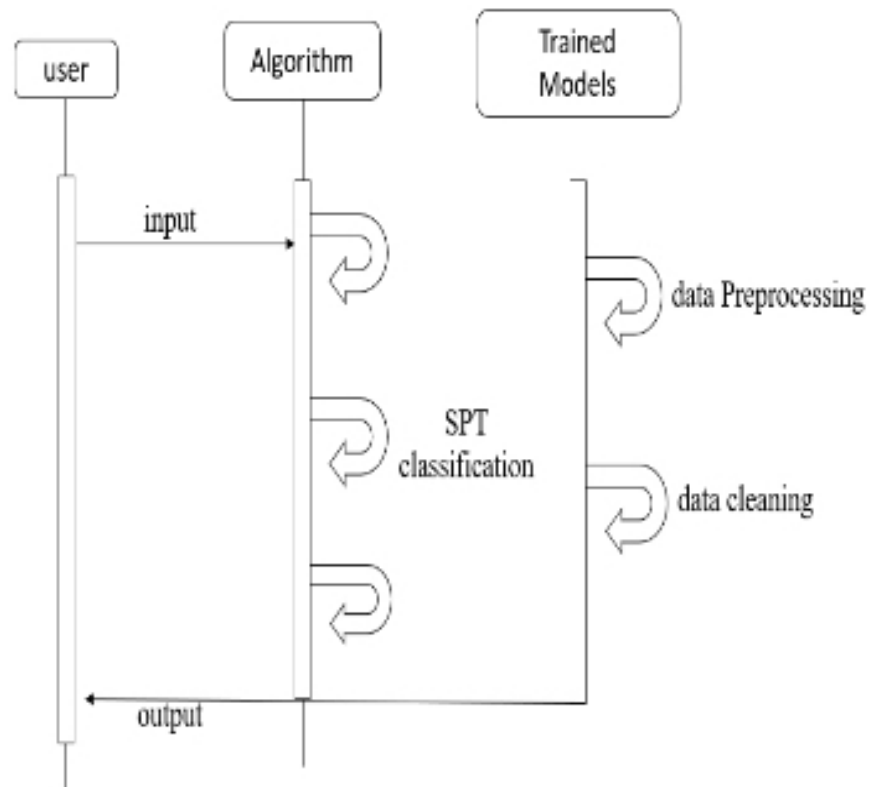


Figure 4.4: Sequence Diagram

The sequence diagram is a Unified Modeling Language diagram that illustrates the sequence of messages between objects in an interaction. The modules like data pre-processing, data cleaning, training, testing, predicting are to be done from user to system and further processing the system need to produce analyze the output and generate an output in graphical representation.

4.2.4 Collaboration diagram

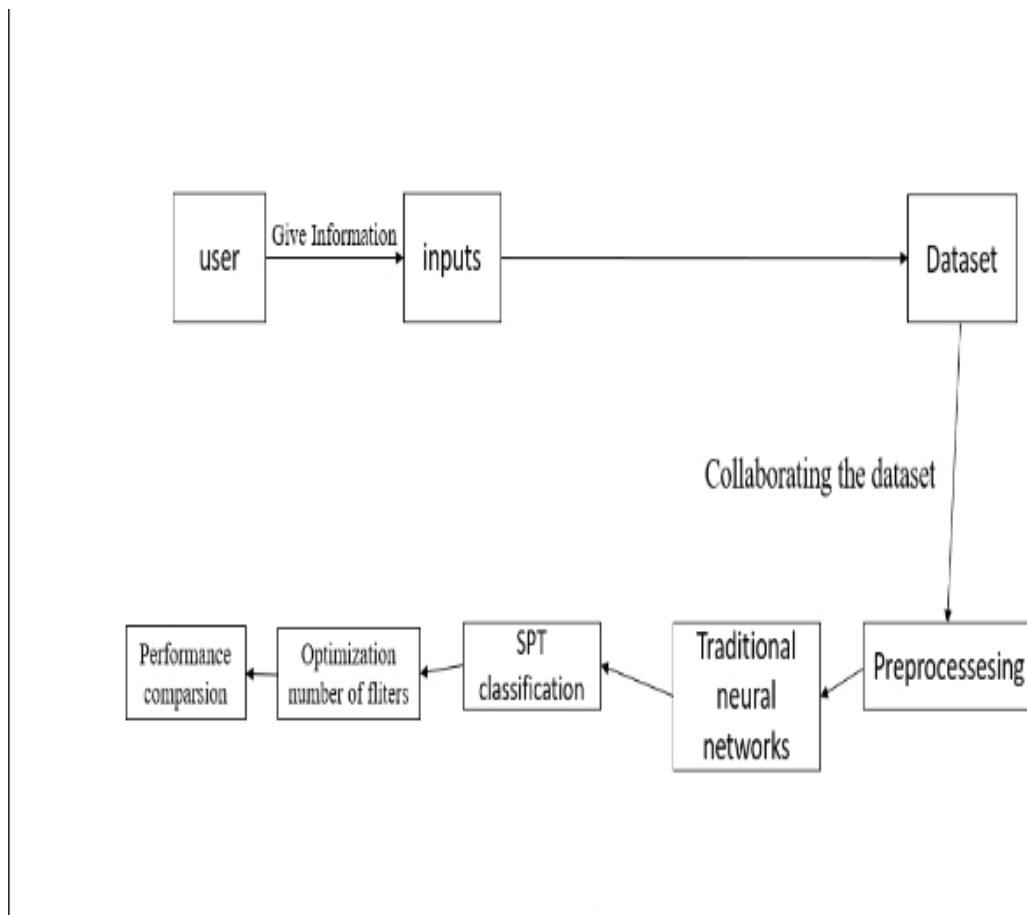


Figure 4.5: Collaboration diagram

The sequence diagram is a Unified Modeling Language diagram that illustrates the sequence of messages between objects in an interaction. The modules like data pre-processing, data cleaning, training, testing, predicting are to be done from user to system and further processing the system need to produce analyze the output and generate an output in graphical representation.

4.3 Algorithm & Pseudo Code

4.3.1 Algorithm

- Step 1: Start the process. Step 2: Setting up tensor flow quantum and circuits.
- Step 3: Generate Data using a Produces n rounds* n qubits datapoints.
- Step 4: Training a Quantum CNN to Detect Excited Cluster States.
- Step 5: Make a model circuit with less quantum pool and conv operations.

Step 6: Design quantum classifier with multiple PQC filters.

Step 7: comparison of proposed HQCNN with various number of filters.

Step 8: Repeat the above process upto the end of the dataset.

Step 9: Output generation process.

Step 10:End.

4.3.2 Pseudo Code

```
1 def create_model_circuit(qubits):
2     model_circuit = cirq.Circuit()
3     symbols = sympy.symbols('qconv0:63')
4     # Cirq uses sympy.Symbols to map learnable variables. TensorFlow Quantum
5     # scans incoming circuits and replaces these with TensorFlow variables.
6     model_circuit += quantum_conv_circuit(qubits, symbols[0:15])
7     model_circuit += quantum_pool_circuit(qubits[:4], qubits[4:],
8                                           symbols[15:21])
9     model_circuit += quantum_conv_circuit(qubits[4:], symbols[21:36])
10    model_circuit += quantum_pool_circuit(qubits[4:6], qubits[6:],
11                                          symbols[36:42])
12    model_circuit += quantum_conv_circuit(qubits[6:], symbols[42:57])
13    model_circuit += quantum_pool_circuit([qubits[6]], [qubits[7]],
14                                          symbols[57:63])
15    return model_circuit
16
17
18 cluster_state_bits = cirq.GridQubit.rect(1, 8)
19 readout_operators = cirq.Z(cluster_state_bits[-1])
20
21 excitation_input = tf.keras.Input(shape=(), dtype=tf.dtypes.string)
22 cluster_state = tfq.layers.AddCircuit()(
23     excitation_input, prepend=cluster_state_circuit(cluster_state_bits))
24
25 quantum_model = tfq.layers.PQC(create_model_circuit(cluster_state_bits),
26                                readout_operators)(cluster_state)
27
28 qcnn_model = tf.keras.Model(inputs=[excitation_input], outputs=[quantum_model])
29
30 tf.keras.utils.plot_model(qcnn_model,
31                            show_shapes=True,
32                            show_layer_names=False,
33                            dpi=70)
```

4.4 Module Description

4.4.1 Design Quantum SVM Model

Quantum computing is a computing paradigm based on the laws of quantum mechanics, enabling a breakthrough in computing power. By carefully exploiting quantum effects such as interference or entanglement, quantum computers aim to efficiently solve particularly difficult problems that would be unsolvable for classical machines, with quantum advantages such as exponential acceleration. On the other hand, Quantum Machine Learning (QML) brings somewhat different research elements from the intersection with classical Machine Learning (ML) while using the computational advantage of quantum computing. There are many aspects and algorithms of QML, such as solving systems of linear equations, principal component analysis (QPCA) and support vector machines. In this article, we focus specifically on the Support Vector Machine (QSVM) model. Similar to support vector machines, the Quantum SVM algorithm (QSVM) is applied to classification problems that require a mapping of functions implicitly specified by a kernel (i.e., a function that is the inner product in the space of the functions being mapped represents). In particular, some previous papers analyze cases where the kernel computation is not classically efficient since it would scale exponentially with the size of the problem (i.e., large number of functions). In addition to speeding up kernel computation, other potential benefits of QSVM could include improved analysis performance (e.g., higher model accuracy), speedup of model training, and data protection.

4.4.2 Design Quantum Neural Network

Machine learning (ML), particularly applied to deep neural networks through the backpropagation algorithm, has enabled a wide range of revolutionary applications, ranging from social to scientific^{1,2}. Achievements include the, which now provides daily handwriting and speech recognition for applications at the frontier of scientific research²⁻⁴. Despite rapid theoretical and practical advances, ML training algorithms are computationally intensive, and now that Moore's law is failing, we must look to a future with a slower progress rate⁵. However, exciting new possibilities are opening up due to the impending advent of quantum computing devices that directly exploit the laws of quantum mechanics to circumvent the technological and thermodynamic limitations of classical computing.

4.5 Steps to execute/run/implement the project

4.5.1 Connections and Importing

- Establish the connection between System with COLAB IDE for executing the modules.
- After establishing the connection import all the required data from dataset.

4.5.2 Graphical representation of data

- Now do all the required operations like generating graphical representations for the data.
- Generate the output as testcases for training and testing modules by using QCNN Analysis. Describe steps with title and mention steps in bullet points

4.5.3 Predicting the Training and Testing dataset Output

- Test all the training and testing modules for future enhancement and generate individual output for every testcase.

Chapter 5

IMPLEMENTATION AND TESTING

5.1 Input and Output

5.1.1 Input Design

At first, a novel HQCNN model with one quantum filter was proposed for the STP phase data classification. This model combines a quantum filter with the traditional artificial neural network. After the quantum filter operation, the qubits are transferred to the fully connected neural network. The fully connected neural network contains two dense layers. The second dense layer was used to classify the data to respective labels. The layered architecture of the proposed HQCNN1QF was illustrated in fig.5.1. The training and validation set of the dataset was used to train the model. The HQCNN-1QF model was trained to 300 epochs on a GPU environment.

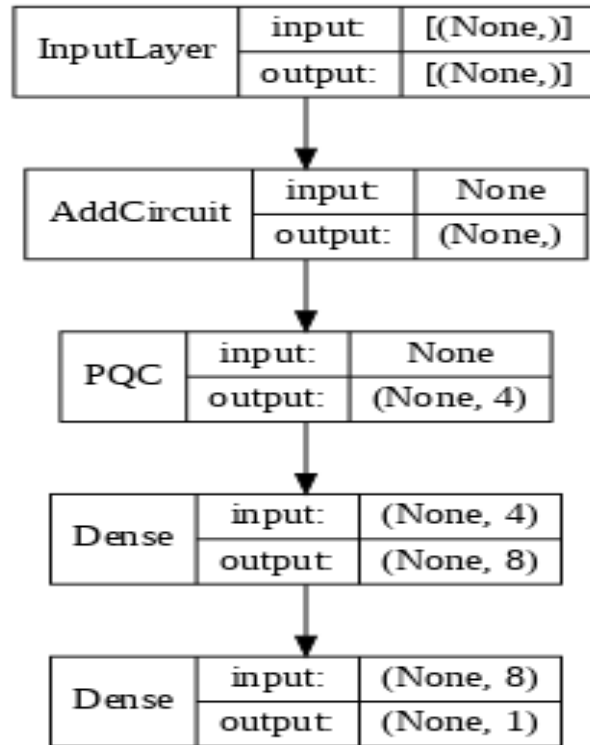


Figure 5.1: The layered architecture of the HQCNN-1QF model

5.1.2 Output Design

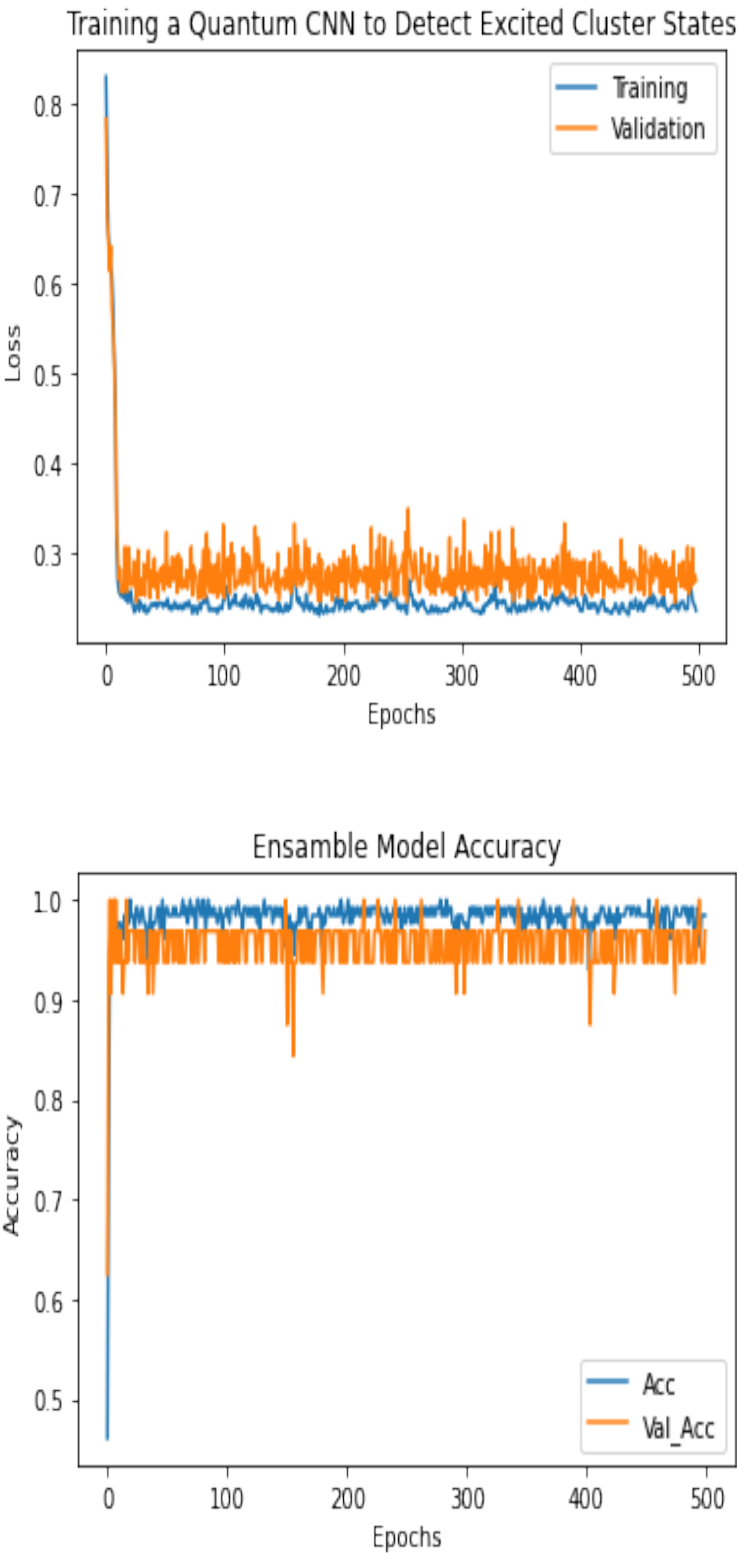


Figure 5.2: The layered architecture of the HQCNN-1QF model

5.2 Testing

Testing is that the method of evaluating a system is that the intent to seek out whether or not it satisfies the desired needs or not. The purpose of testing is to urge errors. Testing is that the strategy of making an endeavor to urge every conceivable fault or weakness in a very work product. It is the strategy of effort software with the intent of guaranteeing that the code meets its requirements associate degree user expectations and doesn't fail in an unacceptable manner.

5.3 Types of Testing

5.3.1 Unit testing

Unit Testing is done for every model in the project. So, the models are data importing, data processing, data executing with the help of linear regressor, data analysis using PQC, analysing part with graphical notation. It was achieved by testing each module and need to check for correctness of model components.

Input

```
1 from collections import Counter
2
3 import matplotlib.pyplot as plt
4 import numpy as np
5 import pennylane as qml
6 import sklearn.datasets
7 import sklearn.decomposition
8 import torch
9 from matplotlib.lines import Line2D
10 from matplotlib.patches import Patch
```

5.3.2 Integration testing

Input

```
1 def plot_points(x_train, y_train, x_test, y_test):
2     c_train = []
3     c_test = []
4
5     for y in y_train:
```

```

6         c_train.append(colours[y])
7
8     for y in y_test:
9         c_test.append(colours[y])
10
11     plt.scatter(x_train[:, 0], x_train[:, 1], c=c_train)
12     plt.scatter(x_test[:, 0], x_test[:, 1], c=c_test, marker="x")
13
14     plt.xlabel("Feature 1", fontsize=16)
15     plt.ylabel("Feature 2", fontsize=16)
16
17     ax = plt.gca()
18     ax.set_aspect(1)
19
20     c_transparent = "#00000000"
21
22     custom_lines = [
23         Patch(facecolor=colours[0], edgecolor=c_transparent, label="Class 0"),
24         Patch(facecolor=colours[1], edgecolor=c_transparent, label="Class 1"),
25         Patch(facecolor=colours[2], edgecolor=c_transparent, label="Class 2"),
26         Line2D([0], [0], marker="o", color=c_transparent, label="Train",
27                markerfacecolor="black", markersize=10),
28         Line2D([0], [0], marker="x", color=c_transparent, label="Test",
29                markerfacecolor="black", markersize=10),
30     ]
31
32     ax.legend(handles=custom_lines, bbox_to_anchor=(1.0, 0.75))
33
34
35 plot_points(x_train, y_train, x_test, y_test)
36 plt.show()

```

Chapter 6

RESULTS AND DISCUSSIONS

6.1 Efficiency of the Proposed System

The quantum filters of the proposed HQCNN model were extended to three and it is named HQCNN-3QF in this section. The quantum filters are extracting features from the output of the AddCircuit layer. And combined using concatenate layer in the model. Each quantum filter produced 4 qubits of extracted information from the data. The layered architecture of the HQCNN-3QF was illustrated.

6.2 Comparison of Existing and Proposed System

SL.No	EXISTING SYSTEM	PROPOSED SYSTEM
1	It not based on quantum theory.	It is based on quantum theory.
2	Sends digital signals using bits.	Sends data through the use of particles or photons.
3	Operates is not extreme cold environments.	Operates in extreme cold environments.
4	Encryption is not based on quantum properties.	Encryption is based on quantum properties.

Table 6.1: Comparison of Existing and Proposed System

6.3 Sample Code

```
1 from collections import Counter
2 import matplotlib.pyplot as plt
3 import numpy as np
4 import pennylane as qml
5 import sklearn.datasets
6 import sklearn.decomposition
7 import torch
8 from matplotlib.lines import Line2D
9 from matplotlib.patches import Patch
10 n_features = 2
11 n_classes = 3
12 n_samples = 150
```



```

13
14 data = sklearn.datasets.load_iris()
15 x = data["data"]
16 y = data["target"]
17 np.random.seed(1967)
18 x, y = zip(*np.random.permutation(list(zip(x, y))))
19
20 pca = sklearn.decomposition.PCA(n_components=n_features)
21 pca.fit(x)
22 x = pca.transform(x)
23 x_min = np.min(x, axis=0)
24 x_max = np.max(x, axis=0)
25
26 x = 2 * np.pi * (x - x_min) / (x_max - x_min) - np.pi*split = 125
27
28 x_train = x[:split]
29 x_test = x[split:]
30 y_train = y[:split]
31 y_test = y[split:]
32
33
34 colours = ["#ec6f86", "#4573e7", "#ad61ed"]
35
36
37 def plot_points(x_train, y_train, x_test, y_test):
38     c_train = []
39     c_test = []
40
41     for y in y_train:
42         c_train.append(colours[y])
43
44     for y in y_test:
45         c_test.append(colours[y])
46
47     plt.scatter(x_train[:, 0], x_train[:, 1], c=c_train)
48     plt.scatter(x_test[:, 0], x_test[:, 1], c=c_test, marker="x")
49
50     plt.xlabel("Feature 1", fontsize=16)
51     plt.ylabel("Feature 2", fontsize=16)
52
53     ax = plt.gca()
54     ax.set_aspect(1)
55
56     c_transparent = "#00000000"
57
58     custom_lines = [
59         Patch(facecolor=colours[0], edgecolor=c_transparent, label="Class 0"),
60         Patch(facecolor=colours[1], edgecolor=c_transparent, label="Class 1"),
61         Patch(facecolor=colours[2], edgecolor=c_transparent, label="Class 2"),
62         Line2D([0], [0], marker="o", color=c_transparent, label="Train",

```

```

63         markerfacecolor="black", markersize=10),
64         Line2D([0], [0], marker="x", color=c_transparent, label="Test",
65               markerfacecolor="black", markersize=10),
66     ]
67
68     ax.legend(handles=custom_lines, bbox_to_anchor=(1.0, 0.75))
69
70
71 plot_points(x_train, y_train, x_test, y_test)
72 plt.show()

```

Output

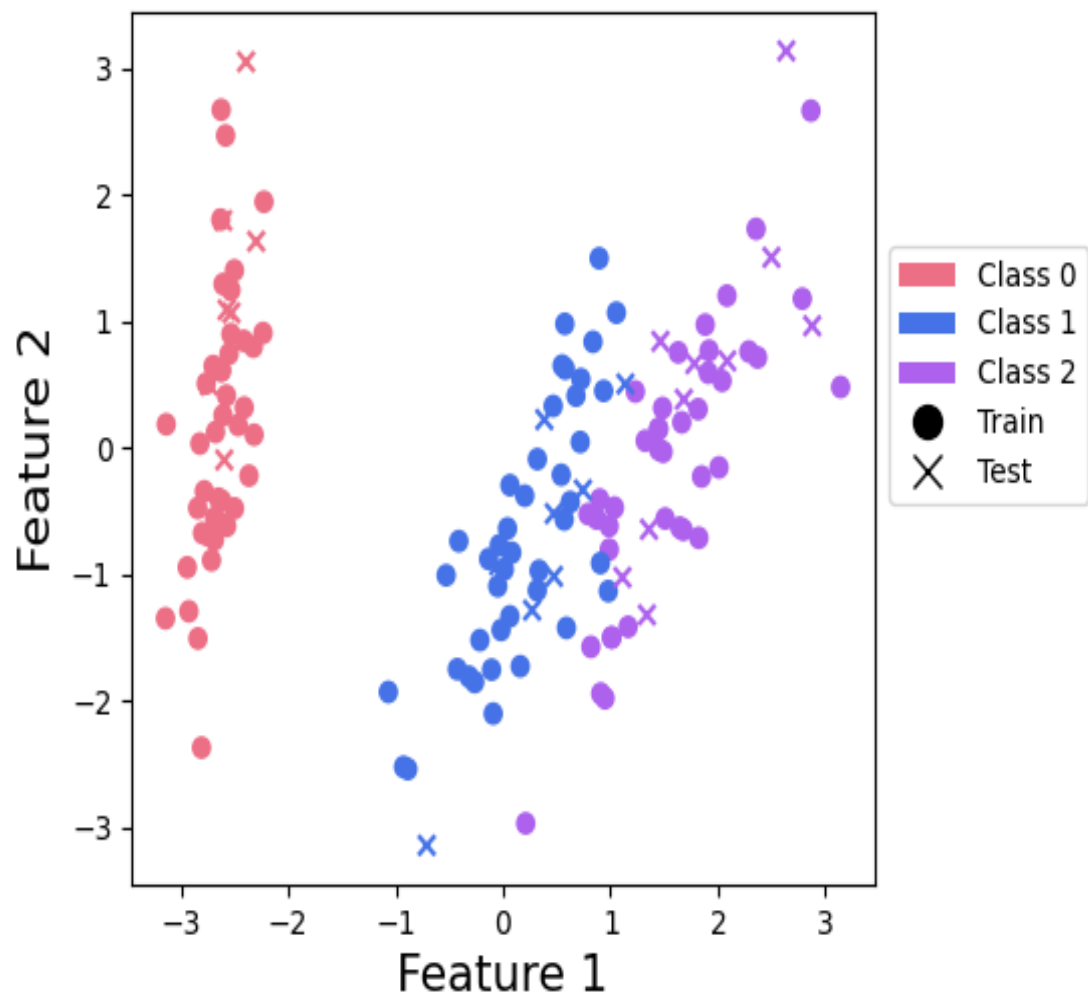


Figure 6.1: Ensemble classification with Forest and Qiskit devices

Chapter 7

CONCLUSION AND FUTURE ENHANCEMENTS

7.1 Conclusion

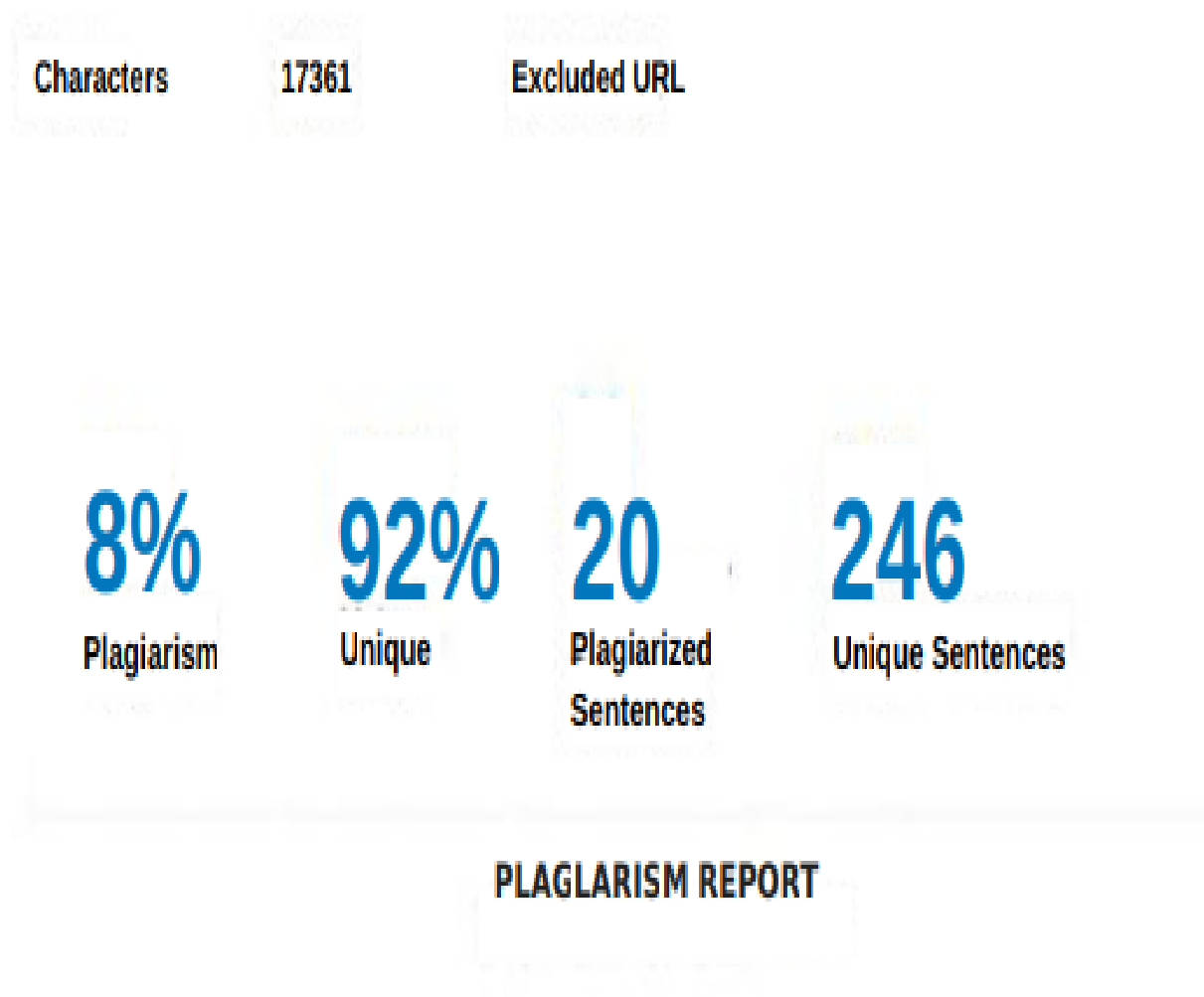
A Deep Convolutional Neural Network is a part of deep neural networks commonly used to classify multimedia data such as images and audios. The CNN requires high computation power to get trained on sample data for classification tasks. In addition, the high computational power requirement consumes more energy. A quantum computing technique provides high computing power with low energy consumption; it is the best alternative to traditional computing techniques to perform complex tasks. The proposed HQCNN combines a quantum filter with the traditional fully connected network for speeding up the training process. The quantum filter consists of QConv and QPool layers for feature extraction from data. The fully connected neural network was introduced after the quantum filter process. The number of quantum filters was optimized using their validation performance. In the future, the research will focus on the optimization of the number of filters and layers in the traditional neural network part of the HQCNN model. Also, the HQCNN model will extend to some other classification datasets

7.2 Future Enhancements

To Develop a quantum data using Projected Quantum Kernel features from image dataset. To Design a novel hybrid classification technique using quantum circuits and convolutional neural network for image classification. To Analysis the performance of the hybrid QCNN network and classical CNN networks on image classification. Developing a novel hybrid classification technique using quantum circuits and convolutional neural network for image classification on quantum data. Identify the importance of the quantum filter numbers on classification model design.

Chapter 8

PLAGIARISM REPORT



Chapter 9

SOURCE CODE & POSTER PRESENTATION

9.1 Source Code

```
1 !pip install tensorflow==2.7.0
2 Looking in indexes: https://pypi.org/simple, https://us-python.pkg.dev/colab-wheels/public/simple/
3 Collecting tensorflow==2.7.0
4   Downloading https://us-python.pkg.dev/colab-wheels/public/tensorflow/tensorflow-2.7.0%2
      Bzzzcolab20220506150900-cp37-cp37m-linux_x86_64.whl
5     \ 665.5 MB 8.2 MB/s
6 Successfully installed gast-0.4.0 keras-2.7.0 tensorflow-2.7.0+zzzcolab20220506150900 tensorflow-
  estimator-2.7.0
7 !pip install tensorflow-quantum
8   Successfully uninstalled google-api-core-1.31.6
9 ERROR: pip's dependency resolver does not currently take into account all the packages that are
  installed. This behaviour is the source of the following dependency conflicts.
10 pydata-google-auth 1.4.0 requires google-auth<3.0dev,>=1.25.0; python_version >= "3.6", but you have
  google-auth 1.18.0 which is incompatible.
11 google-cloud-bigquery-storage 1.1.1 requires google-api-core[grpc
    ]!=2.0.*,!=2.1.*,!=2.2.*,!=2.3.0,<3.0.0dev,>=1.31.5, but you have google-api-core 1.21.0 which
    is incompatible.
12 Successfully installed backports.cached-property-1.0.1 cirq-core-0.14.1 cirq-google-0.14.1 duet
  -0.2.6 google-api-core-1.21.0 google-auth-1.18.0 googleapis-common-protos-1.52.0 sympy-1.8
  tensorflow-quantum-0.6.1 typing-extensions-3.10.0
13 import importlib, pkg_resources
14 importlib.reload(pkg_resources)
15 <module 'pkg_resources' from '/usr/local/lib/python3.7/dist-packages/pkg_resources/__init__.py'>
16 import tensorflow as tf
17 import tensorflow_quantum as tfq
18
19 import cirq
20 import sympy
21 import numpy as np
22
23 %matplotlib inline
24 import matplotlib.pyplot as plt
25 from cirq.contrib.svg import SVGCircuit
26 qubit = cirq.GridQubit(0, 0)
27
```

```

28 circuit1 = cirq.Circuit(cirq.X(qubit))
29 circuit2 = cirq.Circuit(cirq.H(qubit))
30
31 input_circuit_tensor = tfq.convert_to_tensor([circuit1, circuit2])
32
33 y_circuit = cirq.Circuit(cirq.Y(qubit))
34
35 y_appender = tfq.layers.AddCircuit()
36
37 output_circuit_tensor = y_appender(input_circuit_tensor, append=y_circuit)
38 print(tfq.from_tensor(input_circuit_tensor))
39 [cirq.Circuit([
40     cirq.Moment(
41         cirq.X(cirq.GridQubit(0, 0)),
42     ),
43 ])
44 cirq.Circuit([
45     cirq.Moment(
46         cirq.H(cirq.GridQubit(0, 0)),
47     ),
48 ])]
49
50 print(tfq.from_tensor(output_circuit_tensor))
51 [cirq.Circuit([
52     cirq.Moment(
53         cirq.X(cirq.GridQubit(0, 0)),
54     ),
55     cirq.Moment(
56         cirq.Y(cirq.GridQubit(0, 0)),
57     ),
58 ])
59 cirq.Circuit([
60     cirq.Moment(
61         cirq.H(cirq.GridQubit(0, 0)),
62     ),
63     cirq.Moment(
64         cirq.Y(cirq.GridQubit(0, 0)),
65     ),
66 ])]
67 def generate_data(qubits):
68     n_rounds = 20 # Produces n_rounds * n_qubits datapoints.
69     excitations = []
70     labels = []
71     for n in range(n_rounds):
72         for bit in qubits:
73             rng = np.random.uniform(-np.pi, np.pi)
74             excitations.append(cirq.Circuit(cirq.rx(rng)(bit)))
75             labels.append(1 if (-np.pi / 2) <= rng <= (np.pi / 2) else -1)
76
77     split_ind = int(len(excitations) * 0.8)

```

```

78     train_excitations = excitations[:split_ind]
79     test_excitations = excitations[split_ind:]
80
81     train_labels = labels[:split_ind]
82     test_labels = labels[split_ind:]
83
84     return tfq.convert_to_tensor(train_excitations), np.array(train_labels), \
85           tfq.convert_to_tensor(test_excitations), np.array(test_labels)
86     sample_points, sample_labels, _, _ = generate_data(cirq.GridQubit.rect(1, 4))
87 print('Input:', tfq.from_tensor(sample_points)[0], 'Output:', sample_labels[0])
88 print('Input:', tfq.from_tensor(sample_points)[1], 'Output:', sample_labels[1])
89 Input: (0, 0):      X      ^-0.124      Output: 1
90 Input: (0, 1):      X      ^0.394      Output: 1
91 def cluster_state_circuit(bits):
92     circuit = cirq.Circuit()
93     circuit.append(cirq.H.on_each(bits))
94     for this_bit, next_bit in zip(bits, bits[1:] + [bits[0]]):
95         circuit.append(cirq.CZ(this_bit, next_bit))
96     return circuit
97 SVGCircuit(cluster_state_circuit(cirq.GridQubit.rect(1, 4)))
98 def one_qubit_unitary(bit, symbols):
99     return cirq.Circuit(
100         cirq.X(bit)**symbols[0],
101         cirq.Y(bit)**symbols[1],
102         cirq.Z(bit)**symbols[2])
103
104
105 def two_qubit_unitary(bits, symbols):
106     circuit = cirq.Circuit()
107     circuit += one_qubit_unitary(bits[0], symbols[0:3])
108     circuit += one_qubit_unitary(bits[1], symbols[3:6])
109     circuit += [cirq.ZZ(*bits)**symbols[6]]
110     circuit += [cirq.YY(*bits)**symbols[7]]
111     circuit += [cirq.XX(*bits)**symbols[8]]
112     circuit += one_qubit_unitary(bits[0], symbols[9:12])
113     circuit += one_qubit_unitary(bits[1], symbols[12:])
114     return circuit
115
116
117 def two_qubit_pool(source_qubit, sink_qubit, symbols):
118     pool_circuit = cirq.Circuit()
119     sink_basis_selector = one_qubit_unitary(sink_qubit, symbols[0:3])
120     source_basis_selector = one_qubit_unitary(source_qubit, symbols[3:6])
121     pool_circuit.append(sink_basis_selector)
122     pool_circuit.append(source_basis_selector)
123     pool_circuit.append(cirq.CNOT(control=source_qubit, target=sink_qubit))
124     pool_circuit.append(sink_basis_selector**-1)
125     return pool_circuit
126 SVGCircuit(one_qubit_unitary(cirq.GridQubit(0, 0), sympy.symbols('x0:3')))
127 SVGCircuit(two_qubit_unitary(cirq.GridQubit.rect(1, 2), sympy.symbols('x0:15')))

```

```

128 SVGCircuit(two_qubit_pool(*cirq.GridQubit.rect(1, 2), sympy.symbols('x0:6')))
129 def quantum_conv_circuit(bits, symbols):
130     circuit = cirq.Circuit()
131     for first, second in zip(bits[0::2], bits[1::2]):
132         circuit += two_qubit_unitary([first, second], symbols)
133     for first, second in zip(bits[1::2], bits[2::2] + [bits[0]]):
134         circuit += two_qubit_unitary([first, second], symbols)
135     return circuit
136 SVGCircuit(
137     quantum_conv_circuit(cirq.GridQubit.rect(1, 8), sympy.symbols('x0:15')))
138 def quantum_pool_circuit(source_bits, sink_bits, symbols):
139     circuit = cirq.Circuit()
140     for source, sink in zip(source_bits, sink_bits):
141         circuit += two_qubit_pool(source, sink, symbols)
142     return circuit
143 test_bits = cirq.GridQubit.rect(1, 8)
144
145 SVGCircuit(
146     quantum_pool_circuit(test_bits[:4], test_bits[4:], sympy.symbols('x0:6')))
147 def create_model_circuit(qubits):
148     model_circuit = cirq.Circuit()
149     symbols = sympy.symbols('qconv0:63')
150     # Cirq uses sympy.Symbols to map learnable variables. TensorFlow Quantum
151     # scans incoming circuits and replaces these with TensorFlow variables.
152     model_circuit += quantum_conv_circuit(qubits, symbols[0:15])
153     model_circuit += quantum_pool_circuit(qubits[:4], qubits[4:],
154                                         symbols[15:21])
155     model_circuit += quantum_conv_circuit(qubits[4:], symbols[21:36])
156     model_circuit += quantum_pool_circuit(qubits[4:6], qubits[6:],
157                                         symbols[36:42])
158     model_circuit += quantum_conv_circuit(qubits[6:], symbols[42:57])
159     model_circuit += quantum_pool_circuit([qubits[6]], [qubits[7]],
160                                         symbols[57:63])
161     return model_circuit
162
163
164 cluster_state_bits = cirq.GridQubit.rect(1, 8)
165 readout_operators = cirq.Z(cluster_state_bits[-1])
166
167 excitation_input = tf.keras.Input(shape=(), dtype=tf.dtypes.string)
168 cluster_state = tfq.layers.AddCircuit()(
169     excitation_input, prepend=cluster_state_circuit(cluster_state_bits))
170
171 quantum_model = tfq.layers.PQC(create_model_circuit(cluster_state_bits),
172                                readout_operators)(cluster_state)
173
174 qcnn_model = tf.keras.Model(inputs=[excitation_input], outputs=[quantum_model])
175
176 tf.keras.utils.plot_model(qcnn_model,
177                             show_shapes=True,

```



```

178         show_layer_names=False ,
179         dpi=70)
180 train_excitations , train_labels , test_excitations , test_labels = generate_data(
181     cluster_state_bits )
182
183
184 @tf.function
185 def custom_accuracy(y_true , y_pred):
186     y_true = tf.squeeze(y_true)
187     y_pred = tf.map_fn(lambda x: 1.0 if x >= 0 else -1.0, y_pred)
188     return tf.keras.backend.mean(tf.keras.backend.equal(y_true , y_pred))
189
190
191 qcnn_model.compile(optimizer=tf.keras.optimizers.Adam(learning_rate=0.02) ,
192                   loss=tf.losses.mse ,
193                   metrics=[custom_accuracy])
194
195 history = qcnn_model.fit(x=train_excitations ,
196                         y=train_labels ,
197                         batch_size=16 ,
198                         epochs=500 ,
199                         verbose=1 ,
200                         validation_data=(test_excitations , test_labels))
201 readouts = [cirq.Z(bit) for bit in cluster_state_bits[4:]]
202
203
204 def multi_readout_model_circuit(qubits):
205     """Make a model circuit with less quantum pool and conv operations."""
206     model_circuit = cirq.Circuit()
207     symbols = sympy.symbols('qconv0:21')
208     model_circuit += quantum_conv_circuit(qubits , symbols[0:15])
209     model_circuit += quantum_pool_circuit(qubits[:4] , qubits[4:] ,
210                                         symbols[15:21])
211     return model_circuit
212
213
214 excitation_input_dual = tf.keras.Input(shape=() , dtype=tf.dtypes.string)
215
216 cluster_state_dual = tfq.layers.AddCircuit()(
217     excitation_input_dual , prepend=cluster_state_circuit(cluster_state_bits))
218
219 quantum_model_dual = tfq.layers.PQC(
220     multi_readout_model_circuit(cluster_state_bits) ,
221     readouts)(cluster_state_dual)
222
223 d1_dual = tf.keras.layers.Dense(8)(quantum_model_dual)
224
225 d2_dual = tf.keras.layers.Dense(1)(d1_dual)
226
227 hybrid_model = tf.keras.Model(inputs=[excitation_input_dual] , outputs=[d2_dual])

```

```

228
229 tf.keras.utils.plot_model(hybrid_model ,
230                             show_shapes=True ,
231                             show_layer_names=False ,
232                             dpi=70)
233 hybrid_model.compile(optimizer=tf.keras.optimizers.Adam(learning_rate=0.02) ,
234                     loss=tf.losses.mse ,
235                     metrics=[custom_accuracy])
236
237 hybrid_history = hybrid_model.fit(x=train_excitations ,
238                                   y=train_labels ,
239                                   batch_size=16,
240                                   epochs=500,
241                                   verbose=1,
242                                   validation_data=(test_excitations ,
243                                                    test_labels))
244 plt.plot(hybrid_history.history['custom_accuracy'], label='Acc')
245 plt.plot(hybrid_history.history['val_custom_accuracy'], label='Val_Acc')
246 plt.title('Ensamble Model Accuracy')
247 plt.xlabel('Epochs')
248 plt.legend()
249 plt.ylabel('Accuracy')
250 plt.show()
251 plt.plot(hybrid_history.history['loss'], label='Loss')
252 plt.plot(hybrid_history.history['val_loss'], label='Val_Loss')
253 plt.title('Ensamble Model Loss')
254 plt.xlabel('Epochs')
255 plt.legend()
256 plt.ylabel('Loss')
257 plt.show()

```

9.2 Poster Presentation



PROJECT TITLE

Department of Computer Science & Engineering
School of Computing
1156CS601 – MINOR PROJECT
WINTER SEMESTER 21-22

ABSTRACT

Ensemble learning is the process by which multiple models, such as classifiers or experts, are strategically generated and combined to solve a particular computational intelligence problem. Ensemble learning is primarily used to improve the classification performance. We use the forest.gym device to simulate one QPU and the qiskit.aer device to simulate another. Each QPU makes an independent prediction, and an ensemble model is formed by choosing the prediction of the most confident QPU. The iris dataset is used in this project, consisting of three classes of iris flower. The TensorFlow quantum package was used to add the outcomes of the quantum circuits to dense layers for efficient classification.

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INTRODUCTION

Quantum machine learning is a research area that explores the interplay of ideas from quantum computing and machine learning. Quantum machine learning extends the pool of hardware for machine learning by an entirely new type of computing device — the quantum computer. Information processing with quantum computers relies on substantially different laws of physics known as quantum theory. We use the forest.gym device to simulate one QPU and the qiskit.aer device to simulate another. Each QPU makes an independent prediction, and an ensemble model is formed by choosing the prediction of the most confident QPU. The iris dataset is used in this consisting of three classes of iris flower. Using a pre-trained model and the PyTorch interface, we'll see that ensembling allows the QPUs to specialize towards different classes.

In the modern viewpoint, quantum computers can be used and trained as like neural networks. We can systematically adapt the physical control parameters, such as an electromagnetic field strength or a laser pulse frequency, to solve a problem. For example, a trained circuit can be used to classify the content of images, and by encoding the image into the physical state of the device and taking measurements.

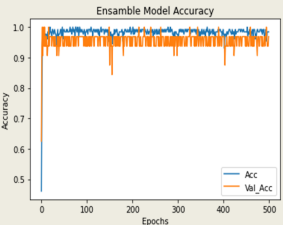
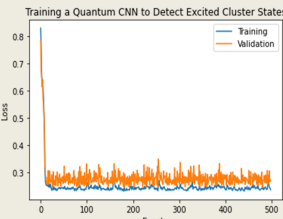
METHODOLOGIES

Quantum computing is a computing paradigm based on the laws of quantum mechanics, enabling a breakthrough in computing power. By carefully exploiting quantum effects such as interference or entanglement, quantum computers aim to efficiently solve particularly difficult problems that would be unsolvable for classical machines, with quantum advantages such as exponential acceleration. On the other hand, Quantum Machine Learning (QML) brings somewhat different research elements from the intersection with classical Machine Learning (ML) while using the computational advantage of quantum computing. There are many aspects and algorithms of QML, such as solving systems of linear equations, principal component analysis (QPCA) and support vector machines. In this article, we focus specifically on the Support Vector Machine (QSVM) model. Similar to support vector machines, the Quantum SVM algorithm (QSVM) is applied to classification problems that require a mapping of functions implicitly specified by a kernel (i.e., a function that is the inner product in the space of the functions being mapped represents). In particular, some previous papers analyze cases where the kernel computation is not classically efficient since it would scale exponentially with the size of the problem (i.e., large number of functions). In addition to speeding up kernel computation, other potential benefits of QSVM could include improved analysis performance (e.g., higher model accuracy), speedup of model training, and data protection.

RESULTS

- The quantum filters of the proposed HQCNN model were extended to three and it is named HQCNN-3QF in this section.
- The quantum filters are extracting features from the output of the AddCircuit layer. And combined using concatenate layer in the model.
- Each quantum filter produced 4 qubits of extracted information from the data. The layered architecture of the HQCNN-3QF was illustrated.

Table 1. The layered architecture of the HQCNN-3QF model



STANDARDS AND POLICIES

- Anacoda Prompt**
Anacoda prompt is a type of command line interface which explicitly deals with the ML/ML (Machine Learning) modules. And navigator is available in all the Windows, Linux and MacOS. The anacoda prompt has many number of IDE's which make the coding easier. The UI can also be implemented in python. Standard Used: ISO/IEC 10918-1:1994
- Jupyter**
It's like an open source web application that allows us to share and create the documents which contains the live code, equations, visualizations and narrative text. It can be used for data cleaning and transformation, numerical simulation, statistical modeling, data visualization, machine learning. Standard Used: ISO/IEC WD TR 24772-4

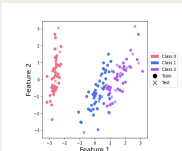


Figure 2: Ensemble classification with Forest and Qiskit devices

CONCLUSIONS

- A Deep Convolutional Neural Network is a part of deep neural networks commonly used to classify multimedia data such as images and audios.
- A quantum computing technique provides high computing power with low energy consumption; it is the best alternative to traditional computing techniques to perform complex tasks.
- The proposed HQCNN combines a quantum filter with the traditional fully connected network for speeding up the training process.
- The quantum filter consists of QConv and QPool layers for feature extraction from data. The fully connected neural network was introduced after the quantum filter process.

ACKNOWLEDGEMENT

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