

4. Write a menu driven program to implement the strict version of binomial min-heap; that is, after any operation, no two trees in the heap should have the same rank. Your program must implement the following functions.

**MAKE-HEAP()**: Create and return a new heap containing no elements.

**INSERT( $H, x$ )**: Insert node  $x$  into heap  $H$ .

**MINIMUM( $H$ )**: Return the value of the smallest key in the heap  $H$ . The function should run in  $O(1)$  time, in the worst case.

**UNION( $H1, H2$ )**: Create and return a new heap that contains all the nodes of heaps  $H1$  and  $H2$ . Heaps  $H1$  and  $H2$  are “destroyed” by this operation.

**EXTRACT-MIN( $H$ )**: Remove the node from heap  $H$  whose key is minimum and return a pointer to the node.

**DECREASE-KEY( $H, x, k$ )**: If node  $x$ 's key is at least  $k$ , decrease the value of its key by  $k$ . Otherwise, print -1.

**DELETE( $H, x$ )**: Delete node  $x$  from heap  $H$ .

Additionally, the program should maintain an array  $A$  (in the main function) to hold pointers to the nodes in the heap, as detailed in the **input format** section below.

### Input Format

The first line of the input contains a single integer  $n$ , the size of the array  $A$ .

Each of the following lines contains a string from the set {'insr', 'min', 'extr', 'decr', 'del', 'tc', 'stop'}, followed by zero, one or two integers, as specified below.

insr j k	- If $A[j]$ is not pointing to any node in the heap, then insert a new node with key 'k' into the heap and add a pointer from $A[j]$ to the new node.
min	- Print the value of the smallest key in the heap.
extr	- Print the value of the smallest key in the heap and delete the node containing this key.
decr j k	- If $A[j]$ is pointing to a node with key at least $k$ , decrease the key by $k$ .
del j	- Print the key of the node pointed to by $A[j]$ and delete the node.
tc	- Print the number of trees currently in the heap.
stop	- Terminate the program.

### Output Format

If an operation cannot be performed, print -1.

## Sample Input and Output

### Input:

```
10
insr 0 10
insr 2 20
insr 5 30
insr 1 40
insr 3 50
extr
insr 0 60
decr 3 45
extr
tc
min
del 5
```

### Output:

```
10
5
1
20
30
```