



An Efficient Python Approach for Simulation of Poisson Distribution



Introduction



Poisson distribution has some useful statistical properties such as its exponential structure allows for “exact” conditional test to be constructed. The distribution of Poisson is also selected part of many important models for testing biological appearance. There are also useful statistical properties of the Poisson distribution. It is additive; which is to say, a Poisson distribution itself has the number of independent Poisson variates.

DISCRETE PROBABILITY DISTRIBUTIONS



There are two types of statistical allocations: discrete and continuous. In data processing, transform is a discrete term. In the Monte Carlo simulation, discrete distributions can also occur. Simulation of Monte Carlo is a simulation method that guesses the probabilities of different results. It is used mainly to assist in predicting situations and identifying threats. Outcomes with discrete values can generate discrete allocations for exploration in the Monte Carlo simulation.

PROBABILITY MASS FUNCTION



In descriptive statistics, any data that is reported or obtained by numbering is discrete data

The distribution of probabilities reports all the potential consequences of a random experiment. Let's construct the distribution of a single coin flip as a trivial example:

$$P(Y = \text{heads}) = 0.5, P(Y = \text{tails}) = 0.5$$

POISSON DISTRIBUTION WITH PYTHON

There are several major market consequences of Poisson distribution. Companies also use it to predict the amount of transactions, provided that they know the average daily rate. In short, the distribution of Poisson allows to discover in a set time interval the uncertainty of an occurrence occurring larger or smaller than the already reported outlay (often noted as λ).

This formula provides its Probability Mass Function:

$$g(k, \lambda) = P(Y = k) = \frac{\lambda^k e^{-\lambda}}{k!} \quad (1)$$

where

k is the number of successes (the number of times a desired even happening)

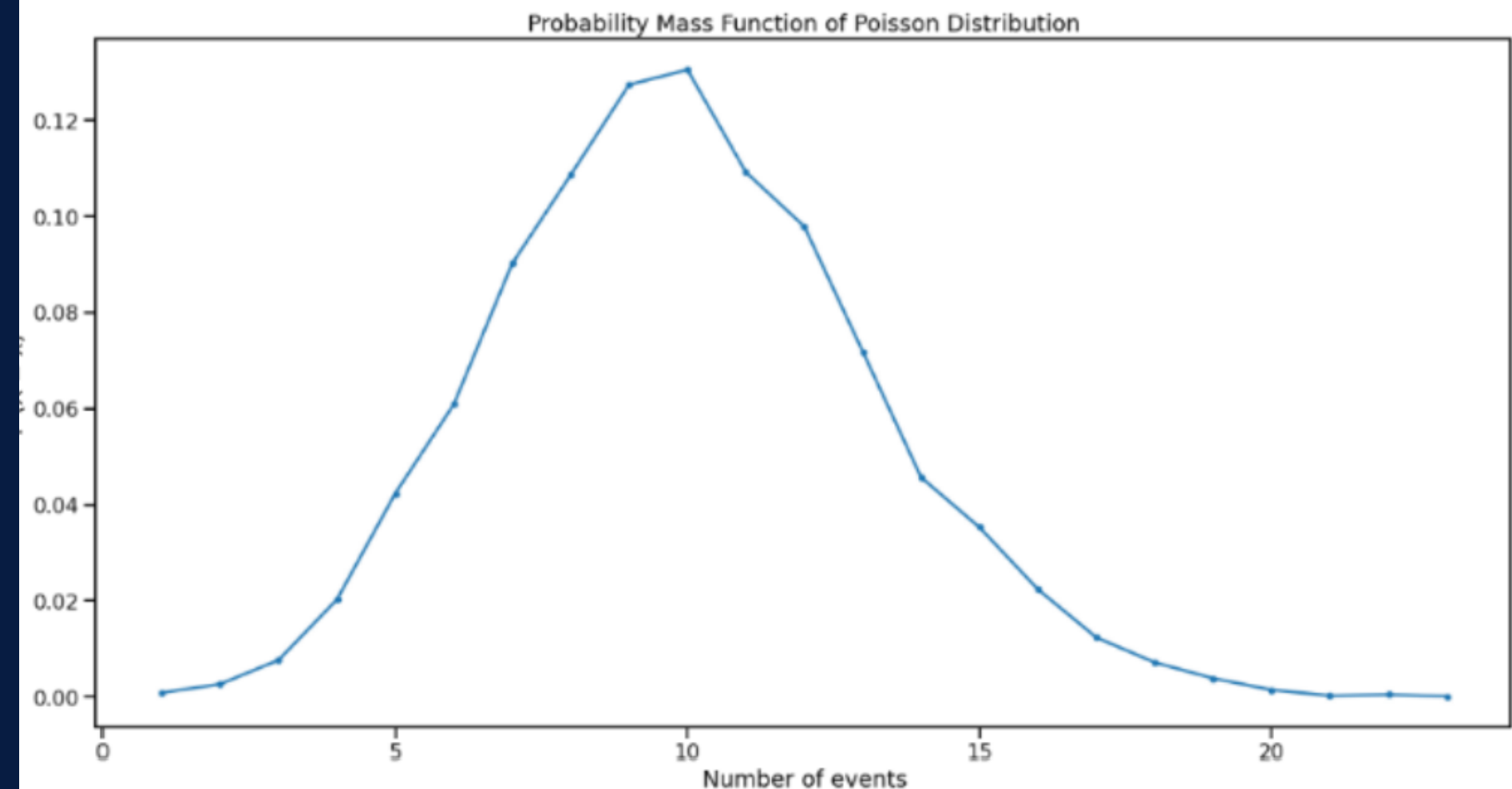
λ is the given rate

SIMULATING THE POISSON DISTRIBUTION

- To Simulate or draw samples from Poisson distribution. we first import and use its random module for simulation.
- To draw samples from a Poisson distribution, we only need the rate parameter λ . We will plug it into `np.random.poisson` function and specify the number of samples.
- Here, we are simulating a distribution with a rate of 10 and has 10k data points. To see this distribution, we will plot the results of its PMF. Though we could do it by hand, there is already a very good library called `empiricaldist`.
- `Pmf` has a function called `from_seq` which takes any distribution and computes the PMF.

- Recall that PMF shows the probabilities of each unique outcome, so in the above result, the outcomes are given as index and probabilities under probs. plotting it using matplotlib gives below graph.
- As expected, the highest probability is for the mean (rate parameter, λ).

Outcomes	Probability(Probs)
1	0.0009
2	0.0027
3	0.0077
4	0.0203
5	0.0424
6	0.0609



Conclusion



In this paper, the feature of probability mass was obtained from observations and the time of high probability was considered. In 75 percent of the cases, the Poisson distribution, including its probability mass function, gives the best fit. The effectiveness of new distributions shows that the effect on the hosting ability of the distribution function used is limited but still comparable to the influence. Therefore, any distribution of probabilities can be used with the aid of python libraries.



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