

# 1025. Divisor Game

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Alice and Bob take turns playing a game, with Alice starting first.

Initially, there is a number `n` on the chalkboard. On each player's turn, that player makes a move consisting of:

- Choosing any `x` with `0 < x < n` and `n % x == 0`.
- Replacing the number `n` on the chalkboard with `n - x`.

Also, if a player cannot make a move, they lose the game.

Return `true` if and only if Alice wins the game, assuming both players play optimally.

## Example 1:

**Input:** `n = 2`

**Output:** `true`

**Explanation:** Alice chooses 1, and Bob has no more moves.

## Example 2:

**Input:** `n = 3`

**Output:** `false`

**Explanation:** Alice chooses 1, Bob chooses 1, and Alice has no more moves.

```
def divisorGame(self, n: int) -> bool:
    if n==1 or n==3:
        return False
    if n==2:
        return True
    dp = [False for i in range(n+1)]
    dp[1] = False
    dp[2] = True
    dp[3] = False

    for i in range(4,n+1):
        if i%2!=0:
            dp[i] = dp[i-1] and dp[i-2]
        else:
            dp[i] = True
```

```
return dp[n]  
return (n & 1) == 0 #Method 2
```

Optimal strategy is if N is even Alice always wins as she will subtract 1 from N and give Odd to Bob who will only be able to subtract an odd from

N-1. Now, again Alice will do the same until Alice reach N=2 where she wins.

If N is odd Alice will always loose as she too wont have an option of subtracting anything but an odd from N.