

# Boolean Parenthesization

Given a boolean expression **S** of length **N** with following symbols.

Symbols

'T' ---> true

'F' ---> false

and following operators filled between symbols

Operators

& ---> boolean AND

| ---> boolean OR

^ ---> boolean XOR

Count the number of ways we can parenthesize the expression so that the value of expression evaluates to true.

## Example 1:

```
Input: N = 7
```

```
S = T|T&F^T
```

```
Output: 4
```

```
Explanation: The expression evaluates
to true in 4 ways ((T|T)&(F^T)),
(T|(T&(F^T))), ((T|T)&F)^T and (T|((T&F)^T)).
```

## Example 2:

```
Input: N = 5
```

```
S = T^F|F
```

```
Output: 2
```

```
Explanation: ((T^F)|F) and (T^(F|F)) are the
only ways.
```

## Your Task:

You do not need to read input or print anything. Your task is to complete the function **countWays()** which takes N and S as input parameters and returns number of possible ways modulo 1003.

**Expected Time Complexity:**  $O(N^3)$

**Expected Auxiliary Space:**  $O(N^2)$

```
class Solution:
    def countWays(self, N, S):
        # code here
```

```

operators = []
exps = []
for ele in S:
    if ele in ('T','F'):
        exps.append(ele)
    else:
        operators.append(ele)
n = len(exps)
dpTrue = [[0]*n for _ in range(n)]
dpFalse = [[0]*n for _ in range(n)]
for gap in range(n):
    i = 0
    j = gap
    while j<n:
        if gap==0:
            if exps[i] == 'T':
                dpTrue[i][j] = 1
                dpFalse[i][j] = 0
            else:
                dpTrue[i][j] = 0
                dpFalse[i][j] = 1
        else:
            for k in range(i,j):
                oprt = operators[k]
                ltc = dpTrue[i][k]
                rtc = dpTrue[k+1][j]
                lfc = dpFalse[i][k]
                rfc = dpFalse[k+1][j]
                if oprt == '&':
                    dpTrue[i][j] += ltc*rtc
                    dpFalse[i][j] += lfc*rtc + ltc*rfc + lfc*rfc
                elif oprt == '|':
                    dpTrue[i][j] += ltc*rtc + lfc*rtc + ltc*rfc
                    dpFalse[i][j] += lfc*rfc
                else:
                    dpTrue[i][j] += ltc*rfc + lfc*rtc
                    dpFalse[i][j] += lfc*rfc + ltc*rtc
            i = i+1
            j = j+1
return dpTrue[0][n-1]%1003

```