

# Matrix Chain Multiplication

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Given a sequence of matrices, find the most efficient way to multiply these matrices together. The efficient way is the one that involves the least number of multiplications.

The dimensions of the matrices are given in an array **arr[]** of size **N** (such that N = number of matrices + 1) where the **i<sup>th</sup>** matrix has the dimensions (**arr[i-1] x arr[i]**).

## Example 1:

```
Input: N = 5
arr = {40, 20, 30, 10, 30}
Output: 26000
Explanation: There are 4 matrices of dimension
40x20, 20x30, 30x10, 10x30. Say the matrices are
named as A, B, C, D. Out of all possible combinations,
the most efficient way is (A*(B*C))*D.
The number of operations are -
20*30*10 + 40*20*10 + 40*10*30 = 26000.
```

## Example 2:

```
Input: N = 4
arr = {10, 30, 5, 60}
Output: 4500
Explanation: The matrices have dimensions
10*30, 30*5, 5*60. Say the matrices are A, B
and C. Out of all possible combinations, the
most efficient way is (A*B)*C. The
number of multiplications are -
10*30*5 + 10*5*60 = 4500.
```

## Your Task:

You do not need to take input or print anything. Your task is to complete the function **matrixMultiplication()** which takes the value **N** and the array **arr[]** as input parameters and returns the minimum number of multiplication operations needed to be performed.

**Expected Time Complexity:**  $O(N^3)$

**Expected Auxiliary Space:**  $O(N^2)$

```
import sys
class Solution:
    def matrixMultiplication(self, N, matrix):
        # code here
        dp = [[0]*(len(matrix)-1) for _ in range(len(matrix)-1)]
        for gap in range(len(matrix)-1):
            i = 0
            j = gap
            while j<len(matrix)-1:
                if gap==0:
                    dp[i][j]=0
                elif gap==1:
                    dp[i][j] = matrix[i]*matrix[j]*matrix[j+1]
                else:
                    temp = sys.maxsize
                    for k in range(i,j):
                        left = dp[i][k]
                        right = dp[k+1][j]
                        selfMult = matrix[i]*matrix[k+1]*matrix[j+1]
                        temp = min(temp,left+right+selfMult)
                    dp[i][j] = temp
                i = i+1
                j = j+1
        return dp[0][-1]
```