



QHack

Quantum Coding Challenges











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6. Hamiltonian Sandwich

0 points

Welcome to the QHack 2023 daily challenges! Every day for the next four days, you will receive two new challenges to complete. These challenges are worth no points — they are specifically designed to get your brain active and into the right mindset for the competition. You will also learn about various aspects of PennyLane that are essential to quantum computing, quantum machine learning, and quantum chemistry. Have fun!

Tutorial #6 — Hamiltonians

You will be tasked with creating the Hamiltonian

$$H = rac{1}{3} \sum_{i < j} X_i X_j - \sum_{i = 0}^{n-1} Z_i,$$

where n is the number of qubits, X_i and Z_i are the familiar Pauli X and Z operators, respectively, and $\sum_{i < j}$ denotes a sum over all pairs (e.g. for n = 3, the pairs are (i, j) = (0, 1), (0, 2), (1, 2)). Note that we're indexing from 0!

In this challenge, you need to create the following quantum circuit simulation that returns the expectation value of this Hamiltonian.

To be clear, each wire represents n qubits, and $|0\rangle$ really means $|0\rangle^{\otimes n}$, i.e. the $|0\rangle$ state for each of these n qubits. Also, be mindful that the H gates represent the Hadamard gate, not the Hamiltonian (which is not unitary, in general)!

Challenge code

In the code below, you must complete two functions:

- hamiltonian: responsible for creating the Hamiltonian in question for a general number of qubits (num_wires). You must complete this function.
- expectation_value: simulates the circuit in question and returns the expectation

Here are some helpful resources and hints:

- The X_iX_j term, mathematically, denotes a *tensor product* between the two Pauli-X operators. Here are some ways you can perform this in PennyLane:
 - use the @ operator to take the tensor product between operators;
 - USE qml.prod.
- qml.Hamiltonian
- Operator arithmetic

Input

As input to this problem, you are given the number of qubits n, num_wires (int).

Output

This code must output the expectation value of the Hamiltonian (float).

If your solution matches the correct one within the given tolerance specified in check (in this case it's a 1e-4 relative error tolerance), the output will be "correct!"

Otherwise, you will receive a "Wrong answer" prompt.

Good luck!

```
Help
Code
                                                                                    1 import json
          import pennylane as qml
          import pennylane.numpy as np
       4 def hamiltonian(num wires):
              """A function for creating the Hamiltonian in question for a general
              number of qubits.
       6
       7
       8
              Args:
       9
                  num_wires (int): The number of qubits.
      10
      11
              Returns:
      12
                   (qml.Hamiltonian): A PennyLane Hamiltonian.
```

```
16
        return
17
18 def expectation value(num wires):
        """Simulates the circuit in question and returns the expectation value
19
20
        Hamiltonian in question.
21
22
        Args:
23
             num_wires (int): The number of qubits.
24
25
        Returns:
26
             (float): The expectation value of the Hamiltonian.
27
28
29
        # Put your solution here #
30
31
        # Define a device using qml.device
32
        dev =
33
                                                                                 34
        @qml.qnode(dev)
35 ,
        def circuit(num_wires):
             """A quantum circuit with Hadamard gates on every qubit and that
36
             the expectation value of the Hamiltonian in question.
37
             .....
38
39
40
             # Put Hadamard gates here #
41
42
             # Then return the expectation value of the Hamiltonian using qml
43
             return
44
45
        return circuit(num_wires)
46
```

```
# These functions are responsible for testing the solution.
47
48 def run(test case input: str) -> str:
49
        num wires = json.loads(test case input)
50
        output = expectation value(num wires)
51
52
        return str(output)
53
54 v def check(solution_output: str, expected_output: str) -> None:
        solution output = json.loads(solution output)
56
        expected output = json.loads(expected output)
        assert np.allclose(solution_output, expected_output, rtol=1e-4)
57
58
                                                                              ₽ 🖴
    test_cases = [['8', '9.33333']]
59
                                                                                 60 v for i, (input_, expected_output) in enumerate(test_cases):
        print(f"Running test case {i} with input '{input }'...")
61
62
63 ,
        try:
             output = run(input )
64
65
        except Exception as exc:
66 ,
             print(f"Runtime Error. {exc}")
67
68
69 ,
        else:
             if message := check(output, expected output):
70 ,
71
                 print(f"Wrong Answer. Have: '{output}'. Want: '{expected_output}'.
72
73 <sub>v</sub>
            else:
                 print("Correct!")
74
                                 Copy all
                                                                    Submit
                                                                Open Notebook
                                                                           Reset
```