





Quantum Coding Challenges











CHALLENGE COMPLETED

View successful submissions

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Unitary Operators and Beyond

200 points

Backstory

Zenda and Reece try to figure out Sqynet's Hamiltonian, before this eerie conscious quantum computer conquers the entirety of sector III. For this, they need to use their own (non-sentient) quantum computer to simulate the action of a Hamiltonian on a quantum state. How do they do this, if a Hamiltonian is,

The Coding Challenge Competition is now closed, but you are welcome to continue working on the challenges until QHack ends on Feb 28 @5pm ET.

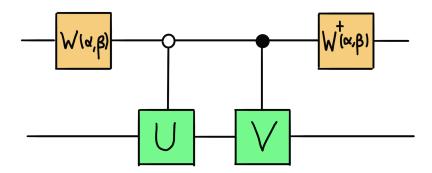
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Zenda and Reece know that the Hamiltonian that describes Sqynet is a linear combination of unitaries, that is

$$H = \sum_i lpha_i U_i.$$

We know that quantum circuits can implement unitary operations really easily, but is there a way to implement a sum of unitaries? Note that the sum of unitaries is not always a unitary, so how can we even do this? We can use measurements!

A circuit of the form



will probabilistically implement the combination of unitaries $\alpha U + \beta V$ on the bottom (main) register, where α and β are **positive real numbers**, without loss of generality. Here, the single-qubit unitary $W(\alpha,\beta)$ is represented by the matrix

$$W(lpha,eta) = rac{1}{\sqrt{lpha+eta}} egin{pmatrix} \sqrt{lpha} & -\sqrt{eta} \ \sqrt{eta} & \sqrt{lpha} \end{pmatrix}$$

The combination will only be applied on the bottom (main) register when we measure the state of the of the top (auxiliary) register to be $|0\rangle$.

Your task is to calculate the probability that this the linear combination of

This algorithm is often used for Hamiltonian simulation. Check out the Xanadu Ouantum Codebook to learn more!

Challenge code

You must complete the <code>linear_combination</code> function to build the above circuit that implements the linear combination

$$\alpha U + \beta V$$

of two single-qubit unitaries U and V, and returns the probabilities on the auxiliary register. For simplicity, we take α and β to be positive real numbers.

As a helper function, you are also asked to complete the \mathbb{W} function, which returns the unitary $W(\alpha, \beta)$.

Input

As input to this problem, you are given:

- U ([list(list(float))]): A 2×2 matrix representing the single-qubit unitary operator U.
- v ([list(list(float))]): A 2×2 matrix representing the single-qubit unitary operator V
- $_{ t alpha}$ ($_{ t float}$): The prefactor lpha of U in the linear combination, as above.
- beta (float): The prefactor β of V in the linear combination, as above.

Output

The output used to test your solution is a float corresponding to the probability of measuring $|0\rangle$ on the main register. This is the first element of your output of linear_combination. We will extract this element for you in our testing functions!

If your solution matches the correct one within the given tolerance specified in

Good luck!

```
Help
Code
                                                                                      1
         import json
       2
          import pennylane as qml
          import pennylane.numpy as np
       4 v def W(alpha, beta):
               """ This function returns the matrix W in terms of
       5
               the coefficients alpha and beta
       6
       7
       8
               Args:
       9
                   - alpha (float): The prefactor alpha of U in the linear combinat:
                   challenge statement.
      10
      11
                   - beta (float): The prefactor beta of V in the linear combination
      12
                   challenge statement.
      13
               Returns
      14
                   -(numpy.ndarray): A 2x2 matrix representing the operator W,
      15
                   as defined in the challenge statement
               .....
      16
      17
               # Put your code here #
      18
      19
               # Return the real matrix of the unitary W, in terms of the coefficie
      20
```

```
21
    dev = qml.device('default.qubit', wires = 2)
22
23
    @qml.qnode(dev)
24 def linear combination(U, V, alpha, beta):
        """This circuit implements the circuit that probabilistically calcula
        of the unitaries.
26
27
28
        Args:
             - U (list(list(float))): A 2x2 matrix representing the single-qual
29
            - V (list(list(float))): A 2x2 matrix representing the single-qul
30
            - alpha (float): The prefactor alpha of U in the linear combinat:
31
32
             - beta (float): The prefactor beta of V in the linear combination
33
34
        Returns:
            -(numpy.tensor): Probabilities of measuring the computational
35
36
            basis states on the auxiliary wire.
37
38
39
        # Put your code here #
40
        # Return the probabilities on the first wire
41
                                                                               42
    # These functions are responsible for testing the solution.
43
44 def run(test case input: str) -> str:
45
        dev = qml.device('default.qubit', wires = 2)
46
        ins = json.loads(test case input)
47
        output = linear_combination(*ins)[0].numpy()
48
49
        return str(output)
50
51 def check(solution output: str, expected output: str) -> None:
52
        solution_output = json.loads(solution_output)
53
        expected output = json.loads(expected output)
54
        assert np.allclose(
55
            solution_output, expected_output, rtol=1e-4
        ), "Your circuit doesn't look quite right "
56
57
    test cases = [['[ 0.70710678, 0.70710678], 0.70710678, -0.7071067 🗎 🗗
58
```

```
59 v for i, (input_, expected_output) in enumerate(test_cases):
         print(f"Running test case {i} with input '{input_}'...")
61
62 ,
         try:
63
             output = run(input_)
64
65 ,
         except Exception as exc:
             print(f"Runtime Error. {exc}")
66
67
         else:
68 ,
             if message := check(output, expected_output):
69 <sub>v</sub>
                  print(f"Wrong Answer. Have: '{output}'. Want: '{expected_output}'.
70
71
             else:
72 <sub>v</sub>
73
                  print("Correct!")
                                   Copy all
                                                                        Submit
                                                                   Open Notebook 🔼
                                                                                Reset
```