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Knowledge Representation and Reasoning

Project number 2:
Deterministic Action With Cost
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1 Introduction

A dynamic system (DS) is viewed as

- a collection of objects, together with their properties, and
- a collection of actions which, while performed, change properties of objects (in consequence, the state of the world).

Let C2 be a class of dynamic systems satisfying the following assumptions:

1. Inertia law
2. Complete information about all actions and fluent.
3. Only Determinism
4. Only sequential actions are allowed.
5. Characterizations of actions:
 - Precondition represented by set of literals(a fluent or its negation);if a precondition does not hold, the action is executed but with empty effect
 - Postcondition (effect of an action) represented by a set of literals.
 - Cost $k \in N$ of an action, actions with empty effects cost 0. Each action has a fixed cost, if it leads to non-empty effects.
6. Effects of an action depends on the state where the action starts.
7. All actions are performed in all states.
8. Partial description of any state of the system are allowed.
9. No constraints are defined.

2 Syntax

2.1 Signature :

A signature is a pair $\Upsilon = (F, Ac, K)$ where F is a set of fluents; Ac is a set of actions and K is a set of positive integers representing Cost of each action $A_n \in Ac$.

2.2 Literal :

A literal is either a fluent f or its negation $\neg f$.

Notation: for a fluent $f \in F$, we write \bar{f} to denote the literal corresponding to f , i.e., either f or $\neg f$.

2.3 Statements :

The system and changes occurring within can be described through a sequence of statements defined in the table:

Statement	Format	Description
Initial Statement	Initially α holds where α is the initial condition with a set of fluent values.	Initial condition α of the fluent set F_α where $F_\alpha = \{f_1, f_2, \dots, f_n\}$ where $f_i \in F$ and $i = 1$ to n .
Effect Statement	A causes α if g_1, \dots, g_k	If the action A is performed in any state satisfying g_1, \dots, g_k , then in the resulting state α holds.
Value Statement	α after $A_1 \dots A_n$	The condition α always (must) hold after performing the sequence $A_1 \dots A_n$ of actions.
Cost Statement	A costs C_β , a numerical cost value where $C_\beta \in K$	If the action A is performed in any satisfying g_1, \dots, g_k then in the resulting state a cost of C_β is used. C_β is a numerical value in Cost set K

Table 1: Syntax Table

3 Semantics

- A state is a function $\sigma : F \rightarrow \{0, 1\}$. For any $f \in F$, if $\sigma(f) = 1$, then we say that f holds in σ and write $\sigma \models f$. If $\sigma(f) = 0$, then we write $\sigma \models \neg f$ and say that f does not hold in σ . Let σ stand for the set of all states.
- A transition function is a mapping $\Upsilon : (Ac, K) \times \sigma \rightarrow \sigma$. For any $\sigma \in \Sigma$, for any $A \in Ac$ and for any K_i in K , $\Upsilon(A, K_i), \sigma$ is the state resulting from performing the action A in the state σ .
- In a transition function $\Upsilon : (A, K_i) \times \sigma \rightarrow \sigma$. For any $A_i \in Ac$ there exists a cost value $K_i \in K$ where $i = 1$ to n respectively.

- A transition function is generalized to the mapping $\Upsilon^* : (Ac^*, K) \times \sigma \rightarrow \sigma$ as follows: $\Upsilon^* (\varepsilon, \sigma) = \sigma$, $\Upsilon^* (((A1, K_1), \dots, (An, K_n)), \sigma) = \Upsilon((An, K_n), \Upsilon^* ((A1, K_1) \dots, (An-1, K_{n-1})))$.
- Let L be an action language of the class A over the signature $\Upsilon = (F, Ac, K)$. A structure for L is a pair $S = (\Upsilon, \sigma_0)$ where Υ is a transition function and $\sigma_0 \in \Sigma$ is the initial state
- Let $S = (\Upsilon, \sigma_0)$ be a structure for L. A statement s_β is true in S, in symbols $S \models s_\beta$, iff s_β is of the form f after A1, . . . , An, then $\Upsilon(((A1, K_1), \dots, (An, K_n)), \sigma_0) \models f$; if s_β is of the form A causes f if $g1, \dots, gk$ and costs K_i , then for every $\sigma \in \Sigma$ such that $\sigma \models gj$, $j = 1, \dots, k$, $\Upsilon((A, K_i), \sigma) \models f$.

Let D be an action domain in the language L over the signature $\Upsilon = (F, Ac, K)$. A structure $S = (\Upsilon, \sigma_0)$ is a model of D iff

- (M1) for every statement $s_{beta} \in D$, $S \models s$;
(M2) for every $A_i \in Ac$ there exists $K_i \in K$ where $i = 1$ to n , for every $f, g1, \dots, gn \in F$, and for every $\sigma \in \Sigma$, if one of the following conditions holds:
(i) D contains an effect statement
A causes \bar{f} for the cost value k if $\bar{g1}, \dots, \bar{gn}$,
where $k \neq 0$ and $\sigma \models gi$ for some $i = 1, \dots, n$
(ii) D does not contain an effect statement
A causes \bar{f} if $g1, \dots, gn$
then $\sigma \not\models gi$ iff $\Psi((A, k), \sigma) \not\models gi$ for some $i = 1, \dots, n$, where $k = 0$.

4 Examples

4.1 Example 01

4.1.1 Description

Andrew wants to travel by his car to a place. Travelling costs him 50\$ if he uses fuel from the fuel tank of the car. If in case of emergency, Andrew is carrying a bottle of fuel as reserve, which can cost him 50\$ for travelling. buying Fuel costs him 100\$ if both fuel and reserve are empty. and buying causes both his Fuel and Reserve are filled.

4.1.2 Representation

Initially: Fuel \wedge Reserve
Travel causes \neg fuel if fuel
Travel cost 50
Travel causes \neg reserve if \neg fuel \vee reserve
Travel cost 50
Buy causes fuel, reserve if \neg fuel \vee reserve
But cost 100

4.1.3 Calculation

$$\Sigma = \{ \sigma_0, \sigma_1, \sigma_2 \}$$

$$\begin{aligned} \sigma_0 &= \{ \text{fuel, reserve} \} & \sigma_1 &= \{ \neg\text{fuel, reserve} \} \\ \sigma_2 &= \{ \neg\text{fuel, } \neg\text{reserve} \} \end{aligned}$$

$$\begin{aligned} \Psi(\text{Buy}, 0, \sigma_0) &= \sigma_0 & \Psi(\text{Travel}, 50, \sigma_0) &= \sigma_1 \\ \Psi(\text{Buy}, 0, \sigma_1) &= \sigma_1 & \Psi(\text{Travel}, 50, \sigma_1) &= \sigma_2 \\ \Psi(\text{Buy}, 100, \sigma_2) &= \sigma_1 & \Psi(\text{Travel}, 0, \sigma_2) &= \sigma_2 \end{aligned}$$

4.1.4 Graph

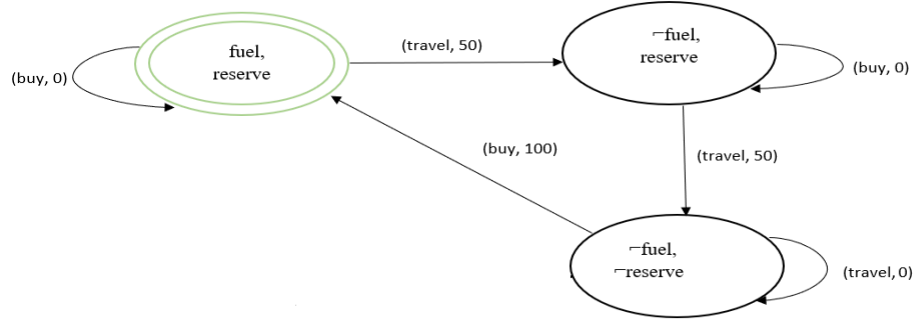


Figure 1: Example 01

4.2 Example 02

4.2.1 Description

John visits a painter to buy a specific painting. The cost of painting is 200\$ if its available in the shop. But if painting is not available then John needs to order a new one to be painted and will buy once its available. Order costs 50\$ At any time only one copy of painting is available and another one to be ordered once sold.

4.2.2 Representation:

Fluents: available, sold.

Actions: buy, order.

Initially: $\neg\text{available} \wedge \neg\text{sold}$

buy causes $(\text{sold} \wedge \neg\text{available})$ if available

buy costs 200\$

order causes available if $\neg\text{available}$

order Cost: 50\$

4.2.3 Calculation:

$$\begin{aligned}\Sigma &= \{ \sigma_0, \sigma_1, \sigma_2, \sigma_3 \} \\ \sigma_0 &= \{ \neg \text{available}, \neg \text{sold} \} \\ \sigma_1 &= \{ \neg \text{available}, \text{sold} \} \\ \sigma_2 &= \{ \text{available}, \neg \text{sold} \} \\ \sigma_3 &= \{ \text{available}, \text{sold} \}\end{aligned}$$

$$\begin{aligned}\Psi(\text{buy}, \sigma_0) &= \sigma_0 \\ \Psi(\text{order}, \sigma_0) &= \sigma_1 \\ \Gamma(\text{buy}, \sigma_0) &= 0 \\ \Gamma(\text{order}, \sigma_0) &= 50\end{aligned}$$

$$\begin{aligned}\Psi(\text{buy}, \sigma_1) &= \sigma_2 \\ \Psi(\text{order}, \sigma_1) &= \sigma_1 \\ \Gamma(\text{buy}, \sigma_1) &= 200 \\ \Gamma(\text{order}, \sigma_1) &= 0\end{aligned}$$

$$\begin{aligned}\Psi(\text{buy}, \sigma_2) &= \sigma_2 \\ \Psi(\text{order}, \sigma_2) &= \sigma_1 \\ \Gamma(\text{buy}, \sigma_2) &= 0 \\ \Gamma(\text{order}, \sigma_2) &= 50\end{aligned}$$

$$\begin{aligned}\Psi(\text{buy}, \sigma_3) &= \sigma_2 \\ \Psi(\text{order}, \sigma_3) &= \sigma_3 \\ \Gamma(\text{buy}, \sigma_3) &= 200 \\ \Gamma(\text{order}, \sigma_3) &= 0\end{aligned}$$

4.2.4 Graph

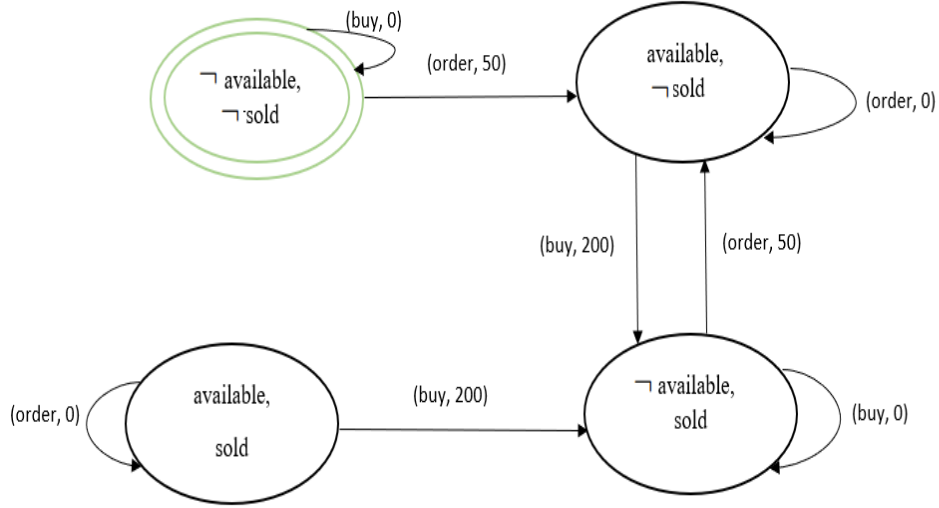


Figure 2: Example 02

4.3 Example 03

4.3.1 Description

There is a man. He can cook, eat, and play. Cooking makes food cooked. he can eat food if it is cooked. After eating he feels not hungry, and food is not cooked again. He can play. Playing makes him hungry. He just can play if he is not hungry. He just cooks when there is no food is cooked. Initially, he is hungry, and no food is cooked. In terms of energy, eating costs 5, cooking costs 15, playing costs 20.

4.3.2 Representation in language

Fluents: cooked, hungry.

Actions: cook, eat, play.

initially $\neg\text{cooked} \wedge \text{hungry}$
 cook causes cooked if $\neg\text{cooked}$
 cook cost 15
 eat causes $(\neg\text{cooked} \wedge \neg\text{hungry})$ if cooked
 eat cost 5
 play causes hungry if $\neg\text{hungry}$
 play cost 20

4.3.3 Calculation

$$\Sigma = \{\sigma_0, \sigma_1, \sigma_2, \sigma_3\}$$

$$\begin{aligned}
 \sigma_0 &= \{\neg\text{cooked}, \text{hungry}\} \\
 \sigma_1 &= \{\text{cooked}, \text{hungry}\} \\
 \sigma_2 &= \{\neg\text{cooked}, \neg\text{hungry}\} \\
 \sigma_3 &= \{\text{cooked}, \neg\text{hungry}\}
 \end{aligned}$$

$$\begin{aligned}
 \Psi(\text{eat}, \sigma_0) &= \sigma_0 \\
 \Psi(\text{cook}, \sigma_0) &= \sigma_1 \\
 \Psi(\text{play}, \sigma_0) &= \sigma_0 \\
 \Gamma(\text{eat}, \sigma_0) &= 0 \\
 \Gamma(\text{cook}, \sigma_0) &= 15 \\
 \Gamma(\text{play}, \sigma_0) &= 0
 \end{aligned}$$

$$\begin{aligned}
 \Psi(\text{eat}, 5, \sigma_1) &= \sigma_2 \\
 \Psi(\text{cook}, 0, \sigma_1) &= \sigma_1 \\
 \Psi(\text{play}, 0, \sigma_1) &= \sigma_1 \\
 \Gamma(\text{eat}, \sigma_1) &= 5 \\
 \Gamma(\text{cook}, \sigma_1) &= 0 \\
 \Gamma(\text{play}, \sigma_1) &= 0
 \end{aligned}$$

$$\begin{aligned}
 \Psi(\text{eat}, 0, \sigma_2) &= \sigma_2 \\
 \Psi(\text{cook}, 15, \sigma_2) &= \sigma_3 \\
 \Psi(\text{play}, 20, \sigma_2) &= \sigma_1 \\
 \Gamma(\text{eat}, \sigma_2) &= 0 \\
 \Gamma(\text{cook}, \sigma_2) &= 15 \\
 \Gamma(\text{play}, \sigma_2) &= 20
 \end{aligned}$$

$$\begin{aligned}
\Psi(\text{eat}, 5, \sigma_3) &= \sigma_2 \\
\Psi(\text{cook}, 0, \sigma_3) &= \sigma_3 \\
\Psi(\text{play}, 20, \sigma_3) &= \sigma_1 \\
\Gamma(\text{eat}, \sigma_3) &= 5 \\
\Gamma(\text{cook}, \sigma_3) &= 0 \\
\Gamma(\text{play}, \sigma_3) &= 20
\end{aligned}$$

4.3.4 Graph

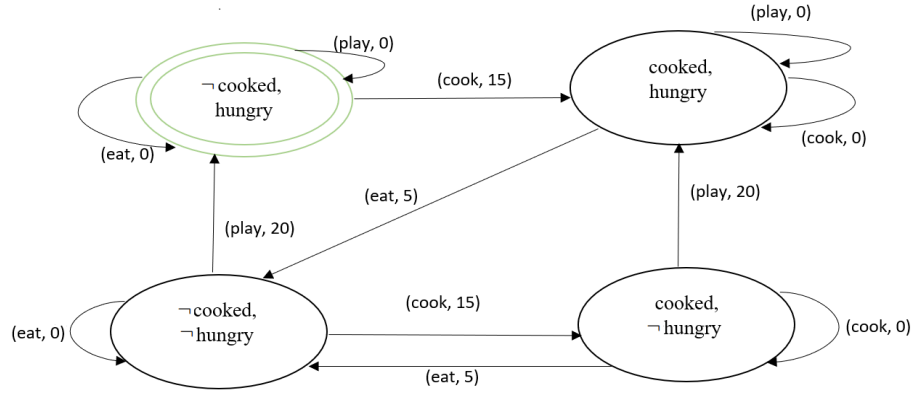


Figure 3: Example 03

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