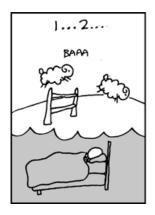
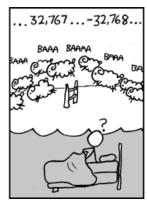
Great Reality #1: Ints are not Integers, Floats are not Reals

- **■** Example 1: Is $x^2 \ge 0$?
 - Float's: Yes!









- Int's:
 - 40000 * 40000 → 1600000000
 - 50000 * 50000 → ??
- **Example 2:** Is (x + y) + z = x + (y + z)?
 - Unsigned & Signed Int's: Yes!
 - Float's:
 - (1e20 + -1e20) + 3.14 --> 3.14
 - 1e20 + (-1e20 + 3.14) --> ??

Computer Arithmetic

Does not generate random values

Arithmetic operations have important mathematical properties

■ Cannot assume all "usual" mathematical properties

- Due to finiteness of representations
- Integer operations satisfy "ring" properties
 - Commutativity, associativity, distributivity
- Floating point operations satisfy "ordering" properties
 - Monotonicity, values of signs

Observation

- Need to understand which abstractions apply in which contexts
- Important issues for compiler writers and serious application programmers

Great Reality #2: You've Got to Know Assembly

- Chances are, you'll never write programs in assembly
 - Compilers are much better & more patient than you are
- But: Understanding assembly is key to machine-level execution model
 - Behavior of programs in presence of bugs
 - High-level language models break down
 - Tuning program performance
 - Understand optimizations done / not done by the compiler
 - Understanding sources of program inefficiency
 - Implementing system software
 - Compiler has machine code as target
 - Operating systems must manage process state
 - Creating / fighting malware
 - x86 assembly is the language of choice!

Great Reality #3: Memory MattersRandom Access Memory Is an Unphysical Abstraction

Memory is not unbounded

- It must be allocated and managed
- Many applications are memory dominated

Memory referencing bugs especially pernicious

Effects are distant in both time and space

■ Memory performance is not uniform

- Cache and virtual memory effects can greatly affect program performance
- Adapting program to characteristics of memory system can lead to major speed improvements

Memory Referencing Bug Example

```
typedef struct {
  int a[2];
  double d;
} struct_t;

double fun(int i) {
  volatile struct_t s;
  s.d = 3.14;
  s.a[i] = 1073741824; /* Possibly out of bounds */
  return s.d;
}
```

```
fun(0) → 3.14
fun(1) → 3.14
fun(2) → 3.1399998664856
fun(3) → 2.00000061035156
fun(4) → 3.14
fun(6) → Segmentation fault
```

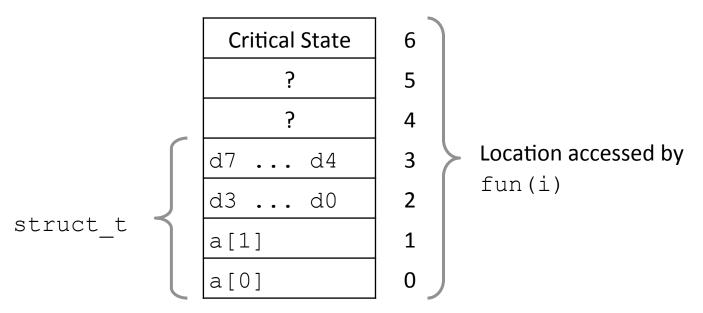
Result is system specific

Memory Referencing Bug Example

```
typedef struct {
  int a[2];
  double d;
} struct_t;
```

```
fun(0) → 3.14
fun(1) → 3.14
fun(2) → 3.1399998664856
fun(3) → 2.00000061035156
fun(4) → 3.14
fun(6) → Segmentation fault
```

Explanation:



Memory Referencing Errors

C and C++ do not provide any memory protection

- Out of bounds array references
- Invalid pointer values
- Abuses of malloc/free

Can lead to nasty bugs

- Whether or not bug has any effect depends on system and compiler
- Action at a distance
 - Corrupted object logically unrelated to one being accessed
 - Effect of bug may be first observed long after it is generated

■ How can I deal with this?

- Program in Java, Ruby, Python, ML, ...
- Understand what possible interactions may occur
- Use or develop tools to detect referencing errors (e.g. Valgrind)

Great Reality #4: There's more to performance than asymptotic complexity

- Constant factors matter too!
- And even exact op count does not predict performance
 - Easily see 10:1 performance range depending on how code written
 - Must optimize at multiple levels: algorithm, data representations, procedures, and loops
- Must understand system to optimize performance
 - How programs compiled and executed
 - How to measure program performance and identify bottlenecks
 - How to improve performance without destroying code modularity and generality

Memory System Performance Example

4.3ms _{2.0 GHz Intel Core i7 Haswell} 81.8ms

- Hierarchical memory organization
- Performance depends on access patterns
 - Including how step through multi-dimensional array

Why The Performance Differs

