### **Decision Tree Induction**

Non-metric Methods

#### Numerical Attributes

- Nearest-neighbor -- distance
- Neural networks: two similar inputs leads to similar outputs
- SVMs: Dot Product

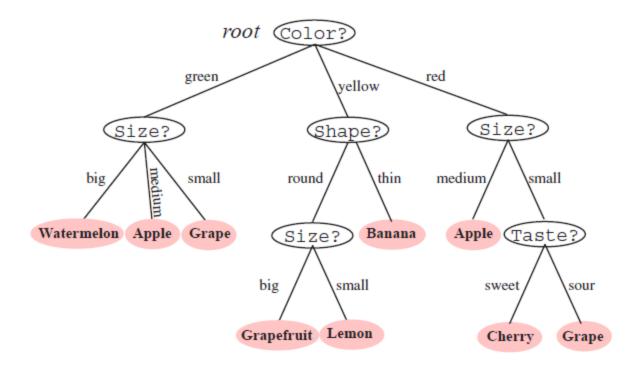
#### Non-metric data

- Nominal attributes
- Color, taste
- Strings: DNA

- Probability based
  - Naïve Bayes
- Rule based
  - Decision trees

#### **Decision Tree**

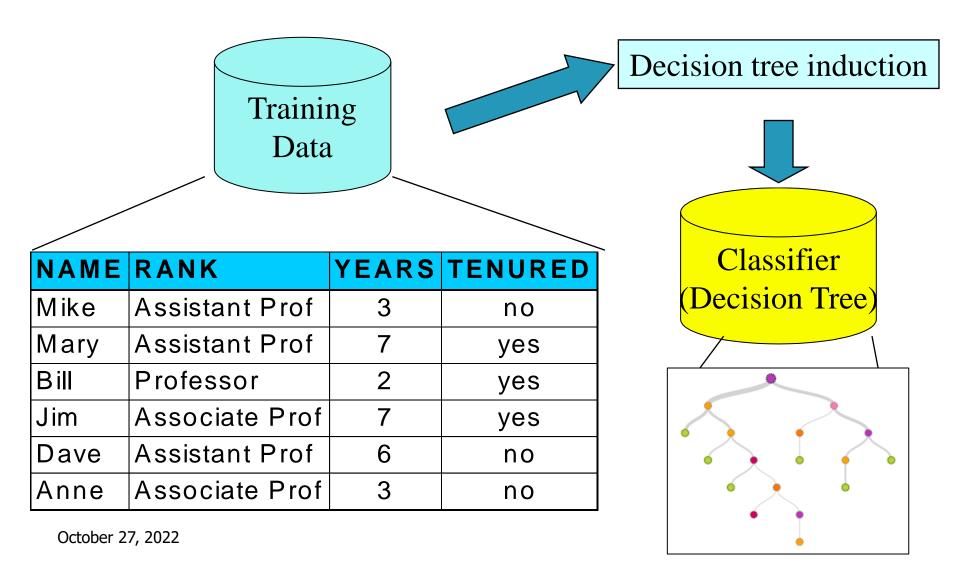
Rules in the form of a hierarchy.



Why are decision trees so popular?

- Why are decision trees so popular?
- Interpretability
  - You can give human understandable explanation for the decision being made.

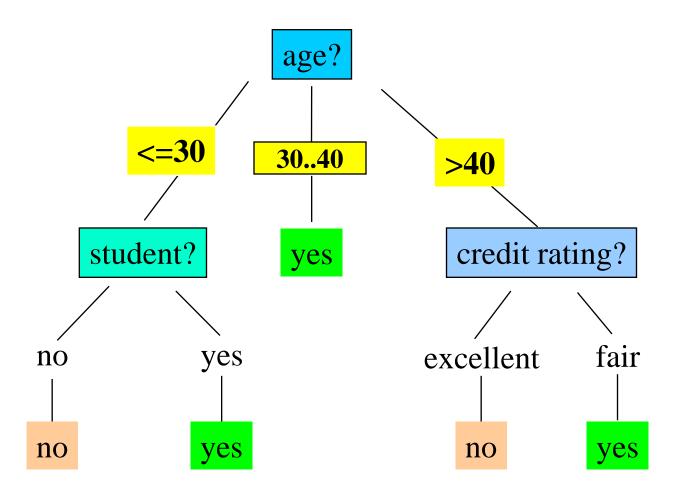
## We need to work with a training set



## You need to work with a training set

age	income	student	cred_rati	buys_comp
<=30	high	no	fair	no
<=30	high	no	excellent	no
3140	high	no	fair	yes
>40	medium	no	fair	yes
>40	low	yes	fair	yes
>40	low	yes	excellent	no
3140	low	yes	excellent	yes
<=30	medium	no	fair	no
<=30	low	yes	fair	yes
>40	medium	yes	fair	yes
<=30	medium	yes	excellent	yes
3140	medium	no	excellent	yes
3140	high	yes	fair	yes
>40	medium	no	excellent	no

#### Output: A Decision Tree for "buys\_computer"



#### How to create a Decision Tree

- From root to leaves it is created
- For root, choose the attribute to be used for testing. This gives child nodes for the root.
- For each child, again choose the attribute to be tested. ....

#### Issues

- Criteria for choosing an attribute?
- You can achieve 100% accuracy with training set?!
  - Overfitting
- When you stop building the tree?

 Are there various types of DT induction methods?? ID3, C4.5 and CART.

#### Decision tree induction

 They adopt a greedy (i.e., nonbacktracking), top-down recursive divide-and-conquer approach.

- Node subset of training patterns
- Root → training set.
- Leaf → class label.

## Impurity measures

Entropy impurity (information impurity)

$$i(N) = -\sum_{j} P(\omega_j) \log_2 P(\omega_j)$$

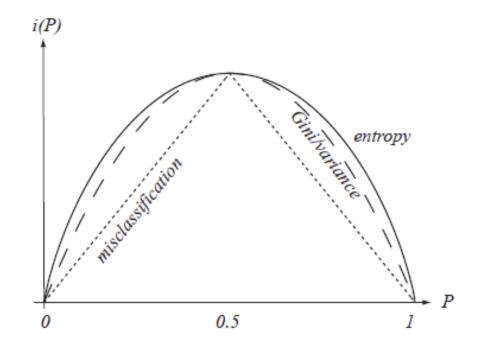
Gini impurity (variance impurity)

$$i(N) = 1 - \sum_{j} P^{2}(\omega_{j})$$

Misclassification impurity

$$i(N) = 1 - \max_{j} P(\omega_{j})$$

## For a two category case



- That which drops the impurity greater.
  - Try to become pure quickly.

$$\Delta i(N) = i(N) - (P_L i(N_L) + (1 - P_L) i(N_R)),$$

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where  $N_L$  and  $N_R$  are the left and right descendent nodes,  $i(N_L)$  and  $i(N_R)$  their impurities, and  $P_L$  is the fraction of patterns at node N that will go to  $N_L$ 

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Then the "best" test value s is the choice for T that maximizes  $\Delta i(T)$ .

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## Information gain

- This is drop in entropy impurity !!
- For an attribute A, often written as Gain(A)

# Gain(age) ??

age	income	student	cred_rati	buys_comp
<=30	high	no	fair	no
<=30	high	no	excellent	no
3140	high	no	fair	yes
>40	medium	no	fair	yes
>40	low	yes	fair	yes
>40	low	yes	excellent	no
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(yes, no) = (9, 5)

## Gain(age) ??

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$$(yes, no) = (9, 5)$$

$$i(root) = I(9,5)$$

$$I(9,5) = -\frac{9}{14} \log \frac{9}{14} - \frac{5}{14} \log \frac{5}{14}$$

$$= 0.94$$

age	Yes	No	<b>I</b> mpurity
<=30	2	3	0.971
3040	4	0	0
>40	3	2	0.971

$$\Delta i(age) = 0.94 - \left(\frac{5}{14}I(2,3) + \frac{4}{14}I(4,0) + \frac{5}{14}I(3,2)\right)$$
$$= 0.69$$

We call this Gain(age) = 0.69.

## For other attributes, their GAIN

$$Gain(income) = 0.029$$
  
 $Gain(student) = 0.151$   
 $Gain(credit\_rating) = 0.048$ 

So we choose age as the splitting attribute.

Similarly one can use other impurity measures

## Gini Index (IBM IntelligentMiner)

 If a data set T contains examples from n classes, gini index, gini(T) is defined as

$$gini(T)=1-\sum_{j=1}^{n} p_{j}^{2}$$

 $gini(T) = 1 - \sum_{j=1}^{n} p_{j}^{2}$  where  $p_{j}$  is the relative frequency of class j in T.

• If a data set T is split into two subsets  $T_1$  and  $T_2$  with sizes  $N_1$  and  $N_2$  respectively, the *gini* index of the split data contains examples from n classes, the gini index gini(T) is defined as

$$gini_{split}(T) = \frac{N_1}{N}gini(T_1) + \frac{N_2}{N}gini(T_2)$$

• The attribute provides the smallest  $gini_{split}(T)$  is chosen to split the node (need to enumerate all possible splitting points for each attribute).

But, there is one drawback with this approach!

- A split with large branching factor is often chosen.
  - So, telephone number is chosen.

$$\Delta i(s) = i(N) - \sum_{k=1}^{B} P_k i(N_k)$$

$$\sum_{k=1}^{B} P_k = 1.$$

## So, we penalize large branching factors

• This is called *gain ratio* (very often used with information gain).

$$\Delta i_B(s) = \frac{\Delta i(s)}{-\sum_{k=1}^B P_k \log_2 P_k}.$$

 Branching factor is more, the denominator is more.

#### **Extracting Classification Rules from Trees**

- Represent the knowledge in the form of IF-THEN rules
- One rule is created for each path from the root to a leaf
- Each attribute-value pair along a path forms a conjunction
- The leaf node holds the class prediction
- Rules are easier for humans to understand
- Example

```
IF age = "<=30" AND student = "no" THEN buys_computer = "no"
IF age = "<=30" AND student = "yes" THEN buys_computer = "yes"
IF age = "31...40" THEN buys_computer = "yes"
IF age = ">40" AND credit_rating = "excellent" THEN buys_computer = "yes"
IF age = ">40" AND credit_rating = "fair" THEN buys_computer = "no"
```

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## Avoid Overfitting in Classification

- The generated tree may overfit the training data
  - Too many branches, some may reflect anomalies due to noise or outliers
  - Result is in poor accuracy for unseen samples
- Two approaches to avoid overfitting
  - Prepruning: Halt tree construction early—do not split a node if this would result in the goodness measure falling below a threshold
    - Difficult to choose an appropriate threshold
  - Postpruning: Remove branches from a "fully grown" tree—get a sequence of progressively pruned trees
    - Use a set of data different from the training data to decide which is the "best pruned tree"

## Classification in Large Databases

- Classification—a classical problem extensively studied by statisticians and machine learning researchers
- Scalability: Classifying data sets with millions of examples and hundreds of attributes with reasonable speed
- Why decision tree induction in classification?
  - relatively faster learning speed (than other classification methods)
  - convertible to simple and easy to understand classification rules
  - can use SQL queries for accessing databases
  - comparable classification accuracy with other methods

# Scalable Decision Tree Induction Methods in Data Mining Studies

- SLIQ (EDBT'96 Mehta et al.)
  - builds an index for each attribute and only class list and the current attribute list reside in memory
- SPRINT (VLDB'96 J. Shafer et al.)
  - constructs an attribute list data structure
- PUBLIC (VLDB'98 Rastogi & Shim)
  - integrates tree splitting and tree pruning: stop growing the tree earlier
- RainForest (VLDB'98 Gehrke, Ramakrishnan & Ganti)
  - separates the scalability aspects from the criteria that determine the quality of the tree
  - builds an AVC-list (attribute, value, class label)

#### **Drawbacks**

- What we discussed are axis parallel
- For continuous valued attributes cut-points can be found.
  - Can be discretized (CART does).

