

STORAGE DEVELOPER CONFERENCE



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*BY Developers FOR Developers*

A **SNIA** Event

# Power of Chaos: Long-term Security for Post-quantum Era

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# Agenda

- Post-quantum era
- Chaos cryptography
- Conclusion



# Post Quantum Era

Risks for classical cryptography



# Asymmetric cryptography

- Security foundations
  - Integer factorization
  - Discrete logarithms

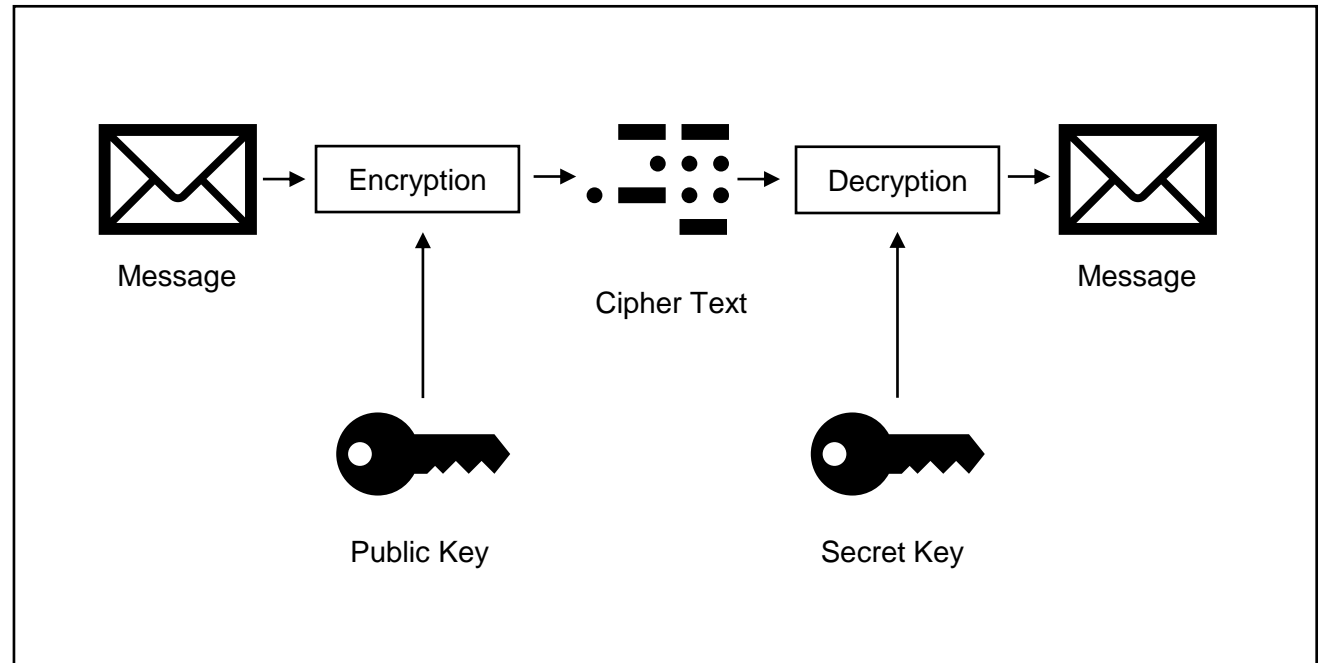


Figure 1: Asymmetric cryptography

# Post-quantum era

- Quantum computers

- Qubits

- Superimposition
    - Entanglement

- Shor's algorithms

- Impact on classical cryptography

- RSA scheme
    - Finite Field Diffie-Hellman key exchange
    - Elliptic Curve Diffie-Hellman key exchange

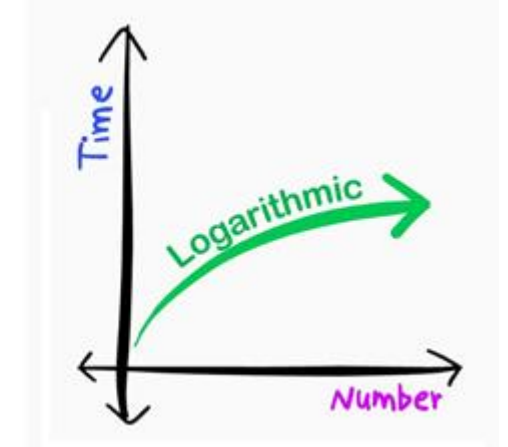
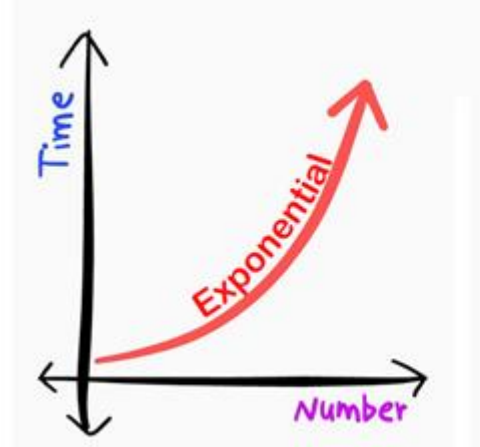


Figure 2: Classical Vs Quantum computers to break cryptosystem

# Quantum safe algorithms

- Lattice
  - Code
  - Hash
  - Non-commutative
  - Multivariate
  - Isogeny
- 

## Academics and Industry

- PyCrypto
- European Telecommunications Standards Institute (ETSI)
- Institute of Quantum Computing

# Where we need quantum safe cryptography?

- Medical records
  - 5 – 100 years
- Implantable wearable devices
  - Biomedical devices
- Financial institutions
  - Tax
- Communication

# Chaos-Based Cryptography





# Chaos

- Properties

- Deterministic
  - Mathematical model
- Nonlinear
  - Logistic map
- Sensitive dependence
  - Butterfly effect

# Chaos – Deterministic

- Mathematical model
  - Discrete equations
    - Logistic map
  - Differential equations
    - Lorenz system

# Chaos – Nonlinear

## ■ Logistic Map

$$x_{n+1} = r x_n (1 - x_n),$$

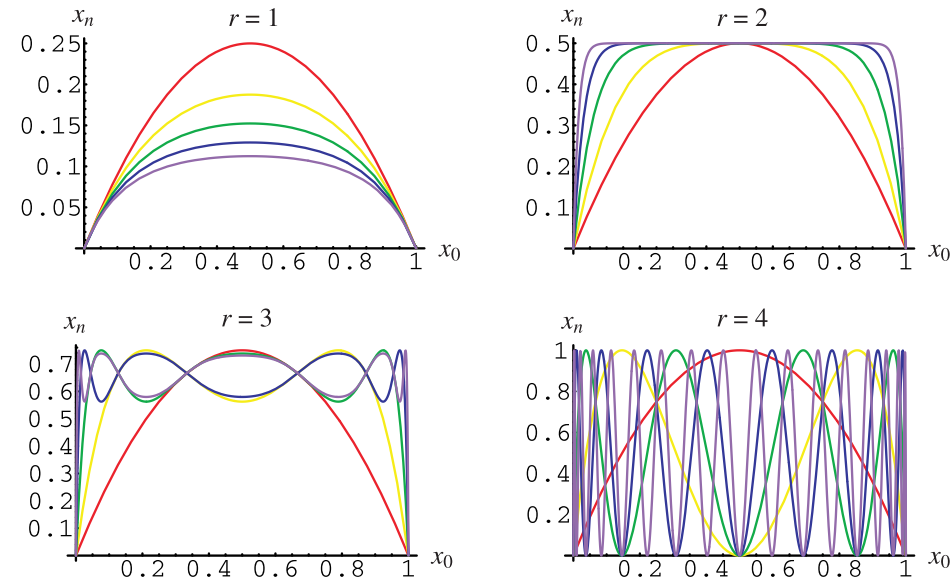


Figure 3: Plotting logistic map for different values of  $r$

# Chaos – Sensitive dependence

- Butterfly effect

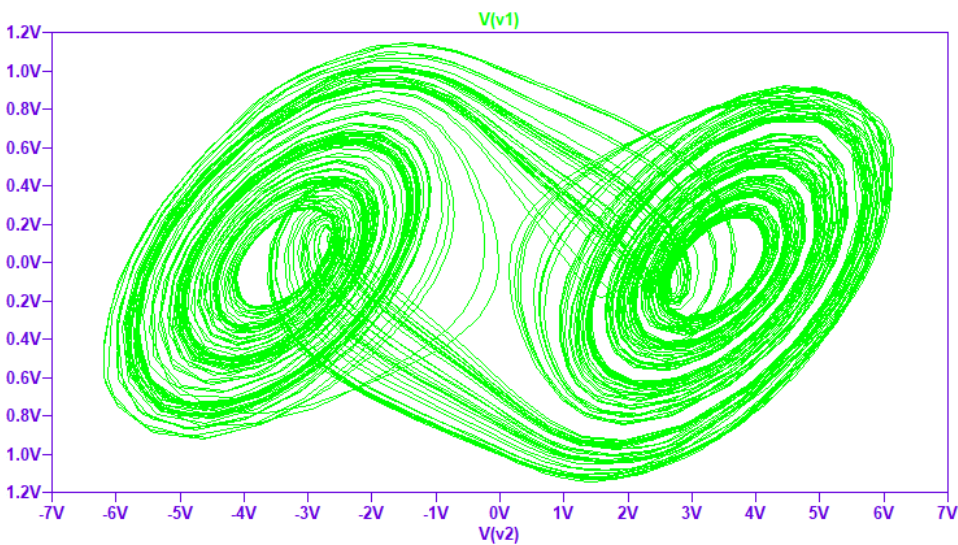


Figure 4: Double scroll attractor for Chau chaotic equations

0.1	0.101
0.3465	0.34957615
0.871785338	0.875384762
0.430336302	0.419982181
0.943815831	0.937849022
0.204155905	0.2244097
10.62553365	0.670092448
0.901829019	0.851113953
10.34085374	0.48786812
10.864989	0.961933347
0.449614656	0.140977693
0.952726071	0.466246485
0.173400554	0.958113696
0.551831287	0.15450759
0.952157043	0.50294473

$$x_{n+1} = r x_n (1 - x_n),$$

# Cryptographic algorithms and chaotic system

Cryptographic algorithms	Chaotic Systems
Finite set of integers	(sub)set of real numbers
Algebraic methods	Analytic method
Rounds	Iterations
Key (Boolean) – Discrete keyspace	Parameters (real) – Continuous keyspace
Diffusion	Sensitivity to change in initial condition
Security and performance	?

# Chaotic system architecture

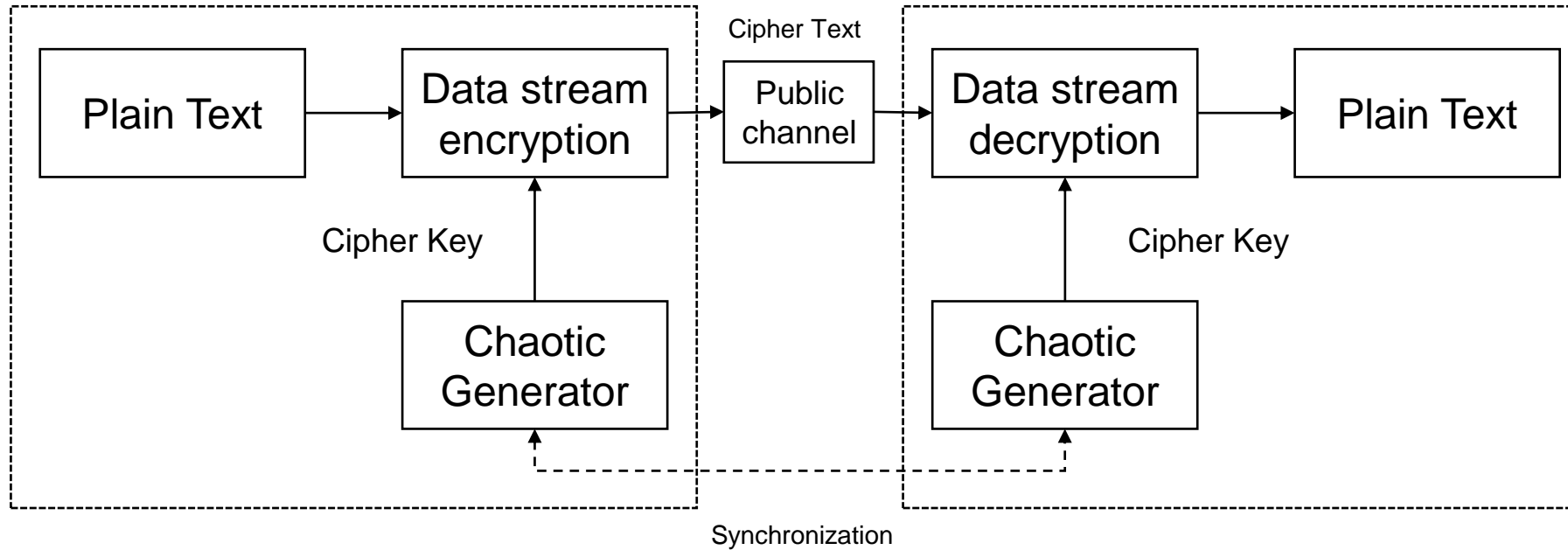


Figure 5: High level architecture of chaotic cryptography

# Chua chaotic circuit

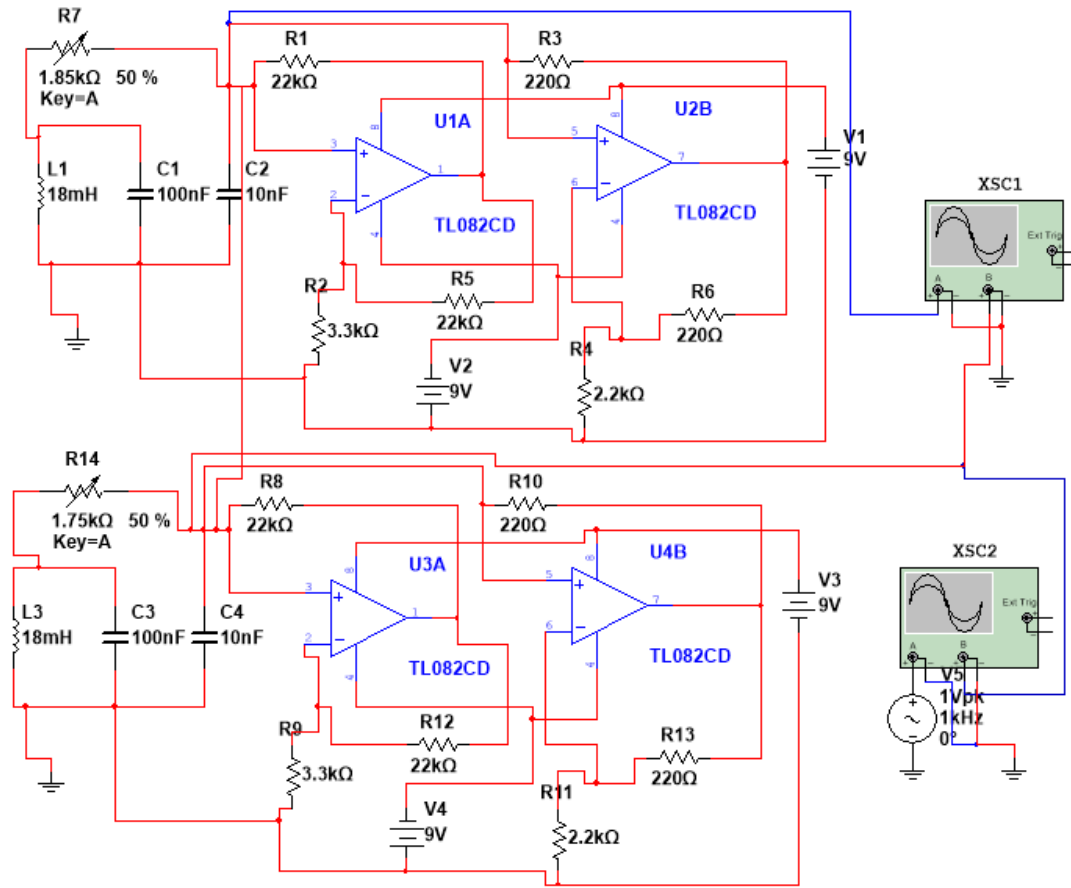


Figure 6: Circuit realization of Chau chaotic circuit

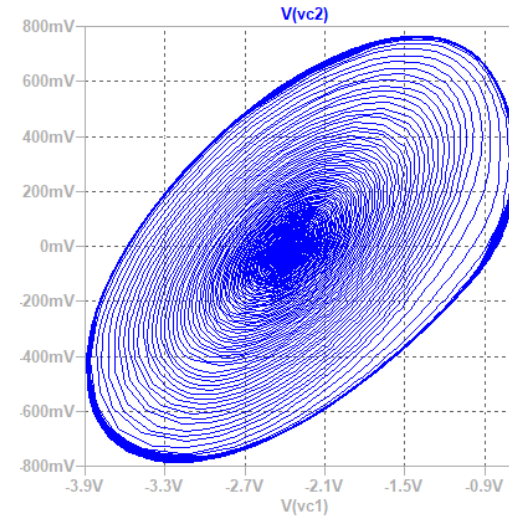


Figure 7: Single scroll attractor

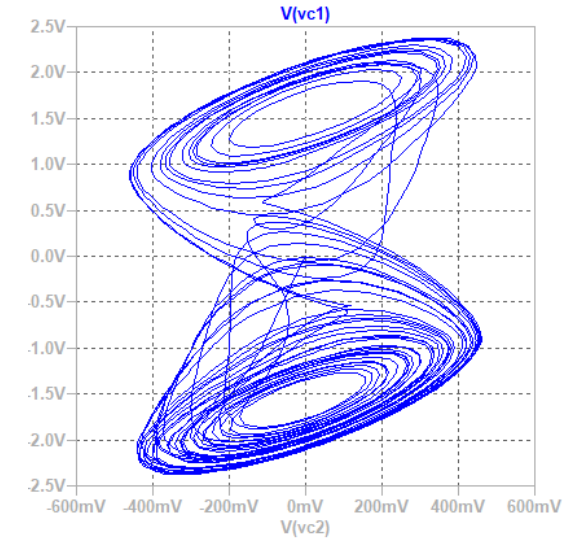


Figure 8: Double scroll attractor

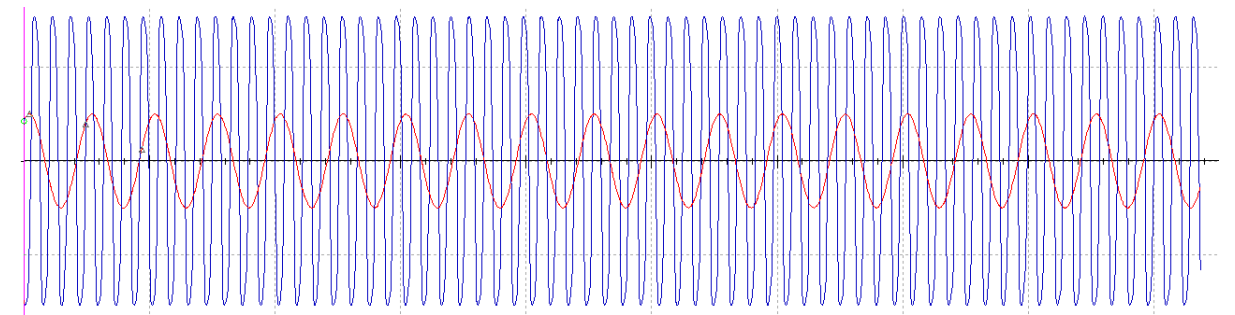


Figure 9: Plain text and encrypted information with Chaos

# Chua chaotic circuit

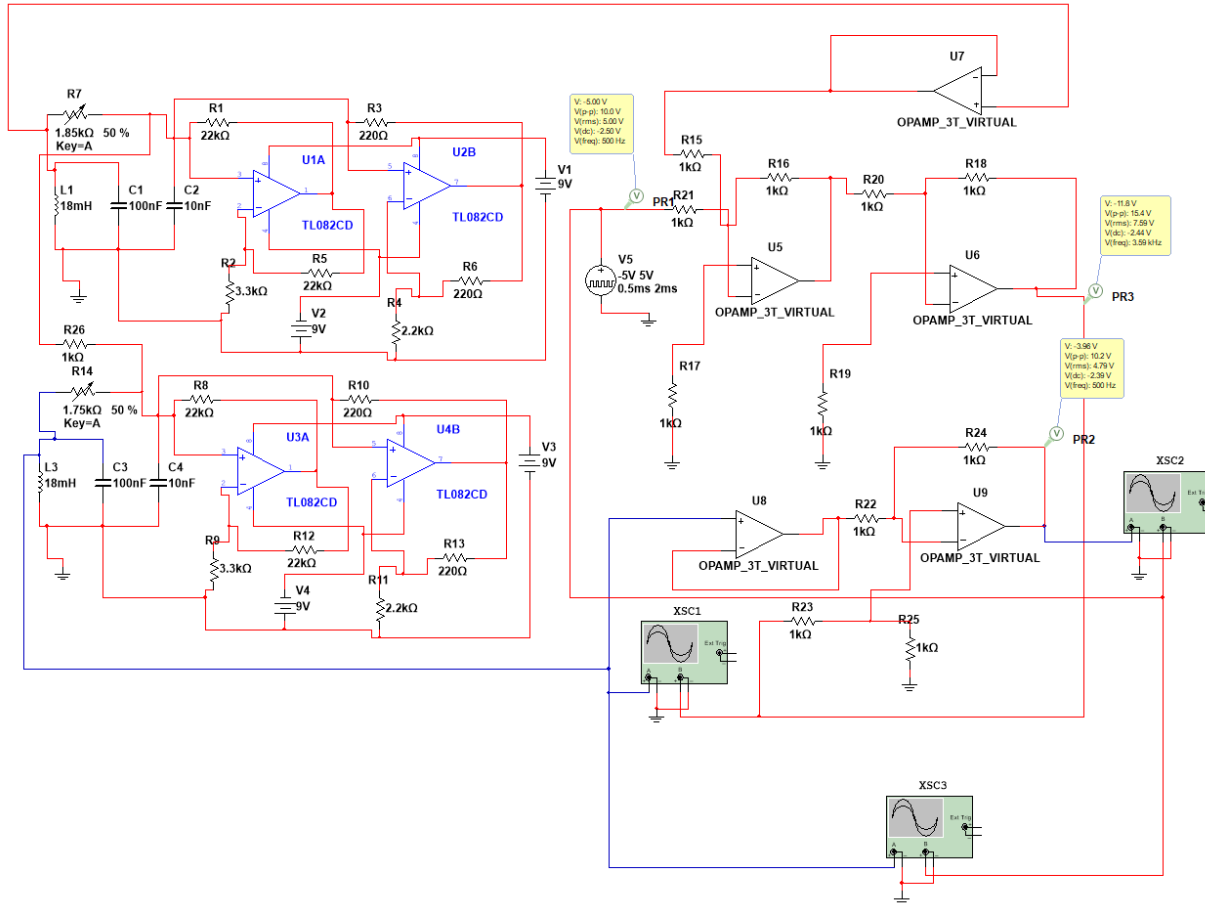


Figure 10: Circuit realization of Chau chaotic circuit with different initial values

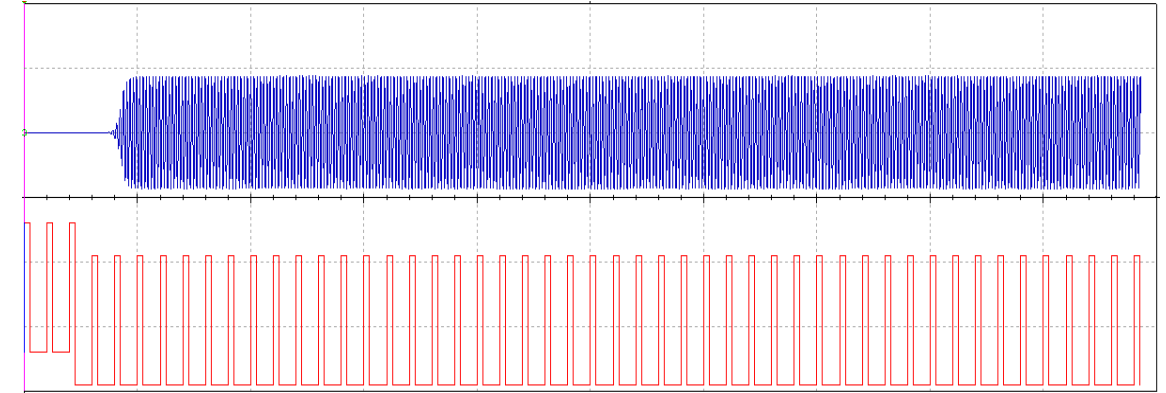


Figure 11: Actual message in red and encrypted message in blue

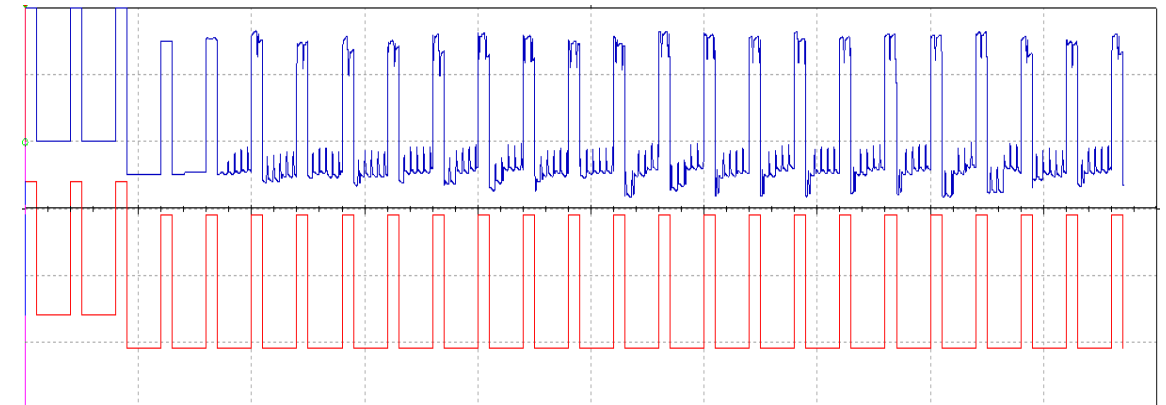


Figure 12: Actual message in red and decrypted message in blue



# Implementation challenges

- Definition of the key leading to non-chaotic behavior
- Nonuniform probability distribution function
- Return map reconstruction
- Low sensitivity to secret key
- Erosion of computational efficiency due to the structural complexity

# Design rule for chaos-based cryptography

- Exhaustive and rigorous definition of key and the keyspace
- Selection of chaotic maps with high sensitivity to control parameter mismatch
- Analysis of the performance of chaotic orbits as source of entropy
- Resistance to application-specific attacks
- Resistance to classical attacks

# Industrial Adoption



# National Institute of Standards and Technology (NIST)

- Lattice problems and hash functions
  - Public-key-encryption (1)
  - Digital signatures (3)
- Post-quantum Cryptography VPN, Microsoft
- PICNIC (Digital signature algorithms), Microsoft
- Quantum Safe services: Kyber, IBM
- AWS KMS API endpoints, AWS KMS

# Conclusion



# Conclusion

- Understanding chaos-based cryptology
- Challenges in implementing post-quantum era cryptography
- No silver bullet for quantum safe algorithms
- Growing industrial adoption
  - Chaos-based cryptography (?)



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