

```
class Node:

    def __init__(self, key):
        self.key = key
        self.left = None
        self.right = None


class BinarySearchTree:

    def __init__(self):
        self.root = None

    # a) Insert (Handle duplicate entries)

    def insert(self, key):
        def _insert(root, key):
            if root is None:
                return Node(key)
            if key < root.key:
                root.left = _insert(root.left, key)
            elif key > root.key:
                root.right = _insert(root.right, key)
            else:
                print(f"Duplicate entry '{key}' ignored.")
            return root

        self.root = _insert(self.root, key)

    # b) Delete

    def delete(self, key):
        def _delete(root, key):
            if root is None:
                return None
            if key < root.key:
                root.left = _delete(root.left, key)
            elif key > root.key:
                root.right = _delete(root.right, key)
            else:
                if root.left is None and root.right is None:
                    return None
                if root.left is None:
                    return root.right
                if root.right is None:
                    return root.left
                temp = root.left
                while temp.right is not None:
                    temp = temp.right
                temp.right = root.right
            return root

        _delete(self.root, key)
```

```
    return root

    if key < root.key:
        root.left = _delete(root.left, key)

    elif key > root.key:
        root.right = _delete(root.right, key)

    else:
        if root.left is None:
            return root.right

        elif root.right is None:
            return root.left

        temp = self._min_value_node(root.right)
        root.key = temp.key
        root.right = _delete(root.right, temp.key)

    return root

self.root = _delete(self.root, key)
```

```
def _min_value_node(self, node):
    current = node

    while current.left is not None:
        current = current.left

    return current
```

```
# c) Search

def search(self, key):
    def _search(root, key):
        if root is None or root.key == key:
            return root

        if key < root.key:
```

```
    return _search(root.left, key)
    return _search(root.right, key)
return _search(self.root, key) is not None
```

d) Display tree (Traversal)

```
def inorder(self):
    def _inorder(root):
        if root:
            _inorder(root.left)
            print(root.key, end=" ")
            _inorder(root.right)
    _inorder(self.root)
    print()
```

e) Display - Depth of tree

```
def depth(self):
    def _depth(root):
        if root is None:
            return 0
        return 1 + max(_depth(root.left), _depth(root.right))
    return _depth(self.root)
```

f) Display - Mirror image

```
def mirror(self):
    def _mirror(root):
        if root:
            root.left, root.right = root.right, root.left
            _mirror(root.left)
```

```

    _mirror(root.right)

    _mirror(self.root)

# g) Create a copy

def copy(self):

    def _copy(root):

        if root is None:

            return None

        new_node = Node(root.key)

        new_node.left = _copy(root.left)

        new_node.right = _copy(root.right)

        return new_node

    new_tree = BinarySearchTree()

    new_tree.root = _copy(self.root)

    return new_tree

```

h) Display all parent nodes with their child nodes

```

def display_parents(self):

    def _display_parents(root):

        if root:

            if root.left or root.right:

                print(
                    f"Parent: {root.key}, Left Child: {root.left.key if root.left else None}, Right Child:
{root.right.key if root.right else None}")

                _display_parents(root.left)

                _display_parents(root.right)

    _display_parents(self.root)

```

```
# i) Display leaf nodes

def display_leaves(self):

    def _display_leaves(root):

        if root:

            if root.left is None and root.right is None:

                print(root.key, end=" ")

                _display_leaves(root.left)

                _display_leaves(root.right)

            _display_leaves(self.root)

    print()
```

```
# j) Display tree level-wise
```

```
def level_order(self):

    if self.root is None:

        return

    queue = [self.root]

    while queue:

        current = queue.pop(0)

        print(current.key, end=" ")

        if current.left:

            queue.append(current.left)

        if current.right:

            queue.append(current.right)

    print()
```

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# Example usage
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```
bst = BinarySearchTree()  
bst.insert(50)  
bst.insert(30)  
bst.insert(70)  
bst.insert(20)  
bst.insert(40)  
bst.insert(60)  
bst.insert(80)  
  
print("Inorder Traversal:")  
bst.inorder()  
  
print("Depth of Tree:", bst.depth())  
  
print("\nParent Nodes:")  
bst.display_parents()  
  
print("\nLeaf Nodes:")  
bst.display_leaves()  
  
print("\nLevel Order Traversal:")  
bst.level_order()  
  
print("\nMirror Image:")  
bst.mirror()  
bst.inorder()
```

```
print("\nCopy of BST:")
bst_copy = bst.copy()
bst_copy.inorder()
```

```
print("\nDeleting 70:")
bst.delete(70)
bst.inorder()
```