

```

class Node:

    def __init__(self, key):

        self.key = key

        self.left = None

        self.right = None


class BinarySearchTree:

    def __init__(self):

        self.root = None


# a) Insert (Handle duplicate entries)

def insert(self, key):

    def _insert(root, key):

        if root is None:

            return Node(key)

        if key < root.key:

            root.left = _insert(root.left, key)

        elif key > root.key:

            root.right = _insert(root.right, key)

        else:

            print(f"Duplicate entry '{key}' ignored.")

        return root

    self.root = _insert(self.root, key)


# b) Delete

def delete(self, key):

    def _delete(root, key):

        if root is None:

```

```

        return root
    if key < root.key:
        root.left = _delete(root.left, key)
    elif key > root.key:
        root.right = _delete(root.right, key)
    else:
        if root.left is None:
            return root.right
        elif root.right is None:
            return root.left
        temp = self._min_value_node(root.right)
        root.key = temp.key
        root.right = _delete(root.right, temp.key)
    return root
self.root = _delete(self.root, key)

```

```

def _min_value_node(self, node):
    current = node
    while current.left is not None:
        current = current.left
    return current

```

c) Search

```

def search(self, key):
    def _search(root, key):
        if root is None or root.key == key:
            return root
        if key < root.key:

```

```
        return _search(root.left, key)
    return _search(root.right, key)
return _search(self.root, key) is not None
```

d) Display tree (Traversal)

```
def inorder(self):
    def _inorder(root):
        if root:
            _inorder(root.left)
            print(root.key, end=" ")
            _inorder(root.right)
    _inorder(self.root)
    print()
```

e) Display - Depth of tree

```
def depth(self):
    def _depth(root):
        if root is None:
            return 0
        return 1 + max(_depth(root.left), _depth(root.right))
    return _depth(self.root)
```

f) Display - Mirror image

```
def mirror(self):
    def _mirror(root):
        if root:
            root.left, root.right = root.right, root.left
            _mirror(root.left)
```

```
        _mirror(root.right)
    _mirror(self.root)
```

g) Create a copy

```
def copy(self):
    def _copy(root):
        if root is None:
            return None

        new_node = Node(root.key)
        new_node.left = _copy(root.left)
        new_node.right = _copy(root.right)
        return new_node

    new_tree = BinarySearchTree()
    new_tree.root = _copy(self.root)
    return new_tree
```

h) Display all parent nodes with their child nodes

```
def display_parents(self):
    def _display_parents(root):
        if root:
            if root.left or root.right:
                print(
                    f"Parent: {root.key}, Left Child: {root.left.key if root.left else None}, Right Child: {root.right.key if root.right else None}")
                _display_parents(root.left)
                _display_parents(root.right)
    _display_parents(self.root)
```

i) Display leaf nodes

```
def display_leaves(self):  
    def _display_leaves(root):  
        if root:  
            if root.left is None and root.right is None:  
                print(root.key, end=" ")  
                _display_leaves(root.left)  
                _display_leaves(root.right)  
    _display_leaves(self.root)  
    print()
```

j) Display tree level-wise

```
def level_order(self):  
    if self.root is None:  
        return  
    queue = [self.root]  
    while queue:  
        current = queue.pop(0)  
        print(current.key, end=" ")  
        if current.left:  
            queue.append(current.left)  
        if current.right:  
            queue.append(current.right)  
    print()
```

Example usage

```
bst = BinarySearchTree()
```

```
bst.insert(50)
```

```
bst.insert(30)
```

```
bst.insert(70)
```

```
bst.insert(20)
```

```
bst.insert(40)
```

```
bst.insert(60)
```

```
bst.insert(80)
```

```
print("Inorder Traversal:")
```

```
bst.inorder()
```

```
print("Depth of Tree:", bst.depth())
```

```
print("\nParent Nodes:")
```

```
bst.display_parents()
```

```
print("\nLeaf Nodes:")
```

```
bst.display_leaves()
```

```
print("\nLevel Order Traversal:")
```

```
bst.level_order()
```

```
print("\nMirror Image:")
```

```
bst.mirror()
```

```
bst.inorder()
```

```
print("\nCopy of BST:")
```

```
bst_copy = bst.copy()
```

```
bst_copy.inorder()
```

```
print("\nDeleting 70:")
```

```
bst.delete(70)
```

```
bst.inorder()
```