On the Round Complexity of Randomized Byzantine Agreement



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Randomized BA & Problem Statement

- Each P_i holds input $v_i \in \{0,1\}$.
- Agreement: All honest parties output the same bit.
- Validity: $\exists i$ s.t. (honest) P_i outputs v_i .

We prove bounds on the halting probability after 1 or 2 rounds.

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Micali's BA (ITCS'17) halts after 3 rounds with constant probability.

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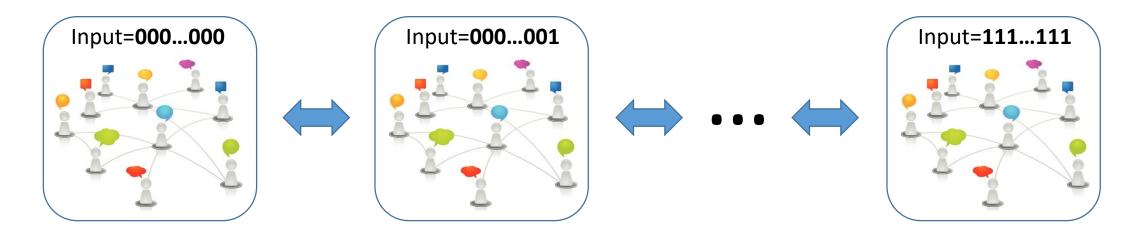
For all* BA protocols and under plausible combinatorial assumption:



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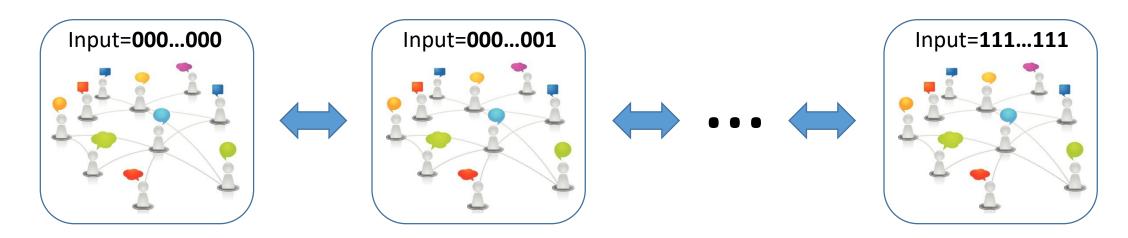
Our Technique

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• However, for randomized protocols, the above chain fails.

The randomness can be used to distinguish adjacent executions.



Our Technique (cont'd)

• Solution:

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• Our attack gives rise to an isoperimetric-type inequality.

Unrealistic cases reduce to KKL & Friedgut's junta theorem.

General case is left as open problem.



Thank You!

Available on eprint & arXiv:

https://eprint.iacr.org/2019/868

https://arxiv.org/abs/1907.11329