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Design and Analysis of Algorithm Tutorial-I

1. What do you understand by Asymptotic Notations.

Define different Asymptotic Notations with example.

Sol:

Alymptotic notations are the mathematical notations used to idescribe the numning time of an algorithm when the input tends towards a particular value or a limiting value.

For example: In bubble sout, when the input array is already sorted, the time taken by the algorithm is linear i.e. the best case.

But, when the input away is in surerse condition, the algorithm take the maximum time (quadratic) to sort the elements i.e. the worst case.

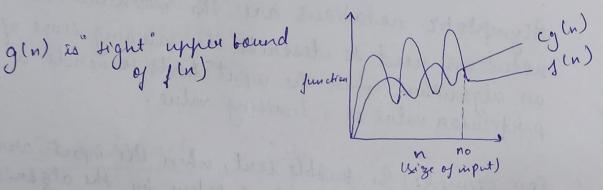
when the input away is neither sorted nor in nevers order, then it takes average time. These dwarfors are denoted using alymptotic notations.

There are mainly three asymptotic notations

- · Big-O notation
- · Omega notation
- · theta notation

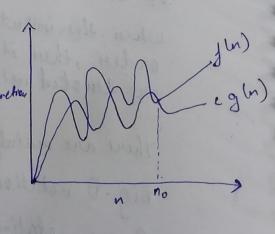
· Big-D Notation (D-notation)

Big-D notation orepresents the upper bound of the ounning time of an algorithm. Thus, it gives the worst-case complexity of an algorithm.



· Omega Notation (A-notation) Omega notation expresents the lower bound of the owning time of an algorithm. Thus, it provides the best case complexity of an algorithms.

1(n)= 1 (g(n)) 4f, fen) >, cg(n) 4 n> no for some constant c>0 g(n) is "tight" lower bound



a the to with the

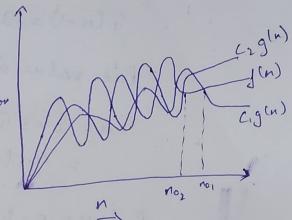
Theta notation encloses the function from above and below. Since it supers outs the upper and loneer bound of the sunning time of an algorithm, it is used lound of the sunning time of an algorithm of an algorithm. for analyzing the average-case complexity of an algorithm.

$$J(n) = O(g(n))$$

 $4f \cdot c.g(n) \leq J(n) \leq c_2 g(n)$

Jon some constant c, >0 furction and az>0

g(n) is both toght upper bound and lower bound of function f(n).



2. what should be time complexity of-11 2 = 1,2,4,8,...n for (i=1 ton) 1;= 1+2; 3 11011)

G.P. kth value = J TK = ask-1 Put n= 2k-1 el 2n = 2k of login: Klogi > log2 + log2 = x > logn +1 = K

d O(lagn)

$$9$$
 9.3 $\Gamma(n) = 13\Gamma(n-1) \times 100$, otherwise 1)

$$T(0) = 1$$

 $T(n) = 3T(n-1) - D$

Put
$$n = n - 1$$

$$T(n-1) = 3T(n-2) - D$$

$$7(n-2) = 37(n-3) - 9$$

$$g(n) = 3^{N} f(n-k)$$

$$q(n) = 3^n$$

Let n-k=D

$$F(n) = 2^{n} F(n-n) - (2^{n}-1)$$

$$F(n) = 2^{n} \cdot 1 - (2^{n}-1)$$

$$F(n) = 2^{n} \cdot 1 - (2^{n}-1)$$

$$F(n) = 2^{n} \cdot 1 - (2^{n}-1)$$

S. what should be time complemity of
int i=1, 8=1;

while (\$c=n)

i++;

\$=8+i;

paintf ("#");

We can define the sum is according to the gelation sia sin ti

S = 1+3+6+10+15+...

the value contained in & at the A ith iterations is the sum of first is positive integers. If is the sum of first is positive integers. If it is total number of iterations taken by the program, then while loop terminals the program, then while loop terminals

1 + 2 + 3 + ... + N = [N(N+1)/2] > n 1 + 2 + 3 + ... + N = [N(N+1)/2] > n 1 + 2 + 3 + ... + N = [N(N+1)/2] > n 1 + 2 + 3 + ... + N = [N(N+1)/2] > n 1 + 2 + 3 + ... + N = [N(N+1)/2] > n 1 + 2 + 3 + ... + N = [N(N+1)/2] > n 1 + 2 + 3 + ... + N = [N(N+1)/2] > n 1 + 2 + 3 + ... + N = [N(N+1)/2] > n 1 + 2 + 3 + ... + N = [N(N+1)/2] > n 1 + 2 + 3 + ... + N = [N(N+1)/2] > n

2) $K^2 + K = 2N$ $K^2 = 2N - K$ $K = \sqrt{2n - K}$ $= 0\sqrt{N}$ 2. Time Lamplemity of the above function $0\sqrt{N}$.

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3 = 10

Auce 8, 6 Pime complexity of
roid for (int n)

int i, count=0;

for (i=1; i x i z=n; ++i)

count++;

as $1^{2} < n$ $3 = 1, 2, 3, 4 - \dots, 5n$ $1 = 1, 2, 3, 4 - \dots, 5n$ $1 + 2 + 3 + 4 + \dots + 5n$ $3 = 1 + 2 + 3 + 4 + \dots + 5n$

```
Time complexity of "
8.7.
       roid & In (int n)
       1 int i, j, k, count = 0;
         Jou (i=n/2; i <= n; ++i)
            Joulie1; je=n; j=j+2)
              Jan | K=1; K=n; K= K+2)
     1001 K= K+2
       k=1,2,4,8,... n
        G. P. = a = 1, 8 = 2
              -1 ( Lx -1)
               logn = W
                                  n
                                  logn + logn
                    logn
                                 logn * logn
                    logn
                                    logn xlogn
                     logn
```

o (n * logn * logn)

o (n log²n)

(10)

```
8) Time complexity of
  function (int n)
        Jon 1 i = 1 ton) - 0 (n)
          1 jon (j=1 +0 n)
                h point(" 4");
                               - 0 (n2)
         quaction (n-3); — T(N/3)
     3 P(n) = P(n/3) + n2
        a=1, b=3 f(n)=n2
        c = log31 = 0
       ey n°=1 (fln1=n2)
      3 1 T (n) = 0 (n2)
```

Time lomplexity ofroid junction (int n)

for (i=1 +0 n)

for (j=1; j <=n; j=j+i)

print ("+")

3

10. For the Junctions, n'k and c'n, what is asymptotic relationship between these junctions?

Assume that K>=1 and C>1 are constants. Find out the value of C and P_0 for which relation holds.

The relation between $n^{-1}k$ and $e^{-1}n$ is $n^{k} = O(e^{n})$

as nx < a c ~ + n >, no and some constant as o

Jon no = 1

2) 14 4 a2'

of no=1 and a=2