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$$y = \frac{2x}{1+x} \rightarrow \frac{dy}{dx} = \frac{2}{(1+x)^2}$$

A (0,1)

B (x_t, y_t)

$$m = \frac{dy}{dx}$$

$$y_t - 1 = m(x_t - 0)$$

$$y_t - 1 = \frac{2}{(1+x_t)^2} (x_t) \quad \text{--- (1)}$$

∴ B lies on the curve

$$\text{So, } y_t = \frac{2x_t}{1+x_t} \quad \text{--- (2)}$$

Substituting (2) in (1),

$$\frac{2x_t}{1+x_t} = \frac{2x_t}{(1+x_t)^2} + 1$$

$$\Rightarrow 2x_t(1+x_t) = 2x_t + (1+x_t)^2$$

$$\Rightarrow 2x_t + 2x_t^2 = 2x_t + 1 + x_t^2 + 2x_t$$

$$\Rightarrow \boxed{x_t^2 - 2x_t - 1 = 0}$$

$$x_t = \frac{2 \pm \sqrt{4+4}}{2} = \frac{2 \pm 2\sqrt{2}}{2} //$$