

Exam.	Back		
Level	BE	Full Marks	80
Programme	BEL, BEX, BCT	Pass Marks	32
Year / Part	II / I	Time	3 hrs.

Subject: - Electromagnetics (EX503)

✓ Candidates are required to give their answers in their own words as far as practicable.

✓ Attempt *t All questions.*

✓ The figures in the margin indicate **Full Marks**.

✓ **Necessary formula is attached herewith.**

→ A represents a vector and → a_{subscript} denotes a unit vector along the direction given by the subscript.

✓ Assume suitable data if necessary.

- Convert the vector $\vec{F} = F_x \vec{a}_x + F_y \vec{a}_y + F_z \vec{a}_z$ to both spherical coordinate system. [5]
- Find the electric field intensity in all three regions due to an infinite sheet parallel plate capacitor having surface charge density $\rho_s \text{ C/m}^2$ and $-\rho_s \text{ C/m}^2$ and placed at $y = 0$ and $y = b$ respectively. Let a uniform line charge density, 3 nC/m , at $y = 3$; uniform surface charge density, 0.2 nC/m^2 at $x = 2$. Find \vec{E} at the origin. [4+4]
- What is dipole? Derive the equation for potential and electric field due to dipole at a distant point P. [1+6]
- Derive Poisson's equation. By solving Laplace's equation, find the capacitance of a parallel plate capacitor with potential difference between the plates equals V_0 . [1+5]
- Verify stoke's theorem for the field $\vec{H} = \left(\frac{3r^2}{\sin \theta} \right) \vec{a}_\theta + 54r \cos \theta \vec{a}_\phi \text{ A/m}$ in free space for the conical surface defined by $\theta = 20^\circ$, $0 \leq \phi \leq 2\pi$, $0 \leq r \leq 5$. Let the positive direction of \vec{ds} be \vec{a}_θ . [8]
- Consider a boundary at $z = 0$ for which $\vec{B}_1 = 2 \vec{a}_x - 3 \vec{a}_y + \vec{a}_z \text{ mT}$, $\mu_1 = 4 \text{ } \mu\text{H/m}$ ($z > 0$), $\mu_2 = 7 \text{ } \mu\text{H/m}$ ($z < 0$) and $\vec{K} = 80 \vec{a}_x \text{ A/m}$ at $z = 0$. Find \vec{B}_2 [8]
- Explain how Ampere's law conflict with continuity equation and how it is corrected? Derive conduction and displacement current in a capacitor. [4+3]
- Derive the expression for electric and magnetic fields for a uniform plane wave propagating in a perfect dielectric medium. [5+3]
- A 9.4 GHz uniform plane wave is propagating in a medium with $\epsilon_r = 2.25$ and $\mu_r = 1$. If the magnetic field intensity is 7 mA/m and the material is loss less, find
 - Velocity of propagation
 - The wave length
 - Phase constant
 - Intrinsic impedance
 - Magnitude of electric field intensity[1+1+1+2+2]

10. A lossless line having an air dielectric has a characteristics impedance of 400Ω . The line is operating at 200 MHz and $Z_{in} = 200 - j200 \Omega$. Find (a) SWR (b) Z_L , if the line is 1 m long; (c) the distance from the load to the nearest voltage maximum. [2+4+2]

11. Differentiate between transmission line and waveguide. A rectangular waveguide having cross-section of $2 \text{ cm} \times 1 \text{ cm}$ is filled with a lossless medium characterized by $\epsilon = 4\epsilon_0$ and $\mu_r = 1$. Calculate the cut-off frequency of the dominant mode. [4+2]

12. Write short notes on antenna and its properties. [2]

DIVERGENCE

$$\text{CARTESIAN } \nabla \cdot \vec{D} = \frac{\partial D_x}{\partial x} + \frac{\partial D_y}{\partial y} + \frac{\partial D_z}{\partial z}$$

$$\text{CYLINDRICAL } \nabla \cdot \vec{D} = \frac{1}{\rho} \frac{\partial}{\partial \rho} (\rho D_\rho) + \frac{1}{\rho} \frac{\partial D_\phi}{\partial \phi} + \frac{\partial D_z}{\partial z}$$

$$\text{SPHERICAL } \nabla \cdot \vec{D} = \frac{1}{r^2} \frac{\partial}{\partial r} (r^2 D_r) + \frac{1}{r \sin \theta} \frac{\partial (\sin \theta D_\theta)}{\partial \theta} + \frac{1}{r \sin \theta} \frac{\partial D_\phi}{\partial \phi}$$

GRADIENT

$$\text{CARTESIAN } \nabla V = \frac{\partial V}{\partial x} \hat{a}_x + \frac{\partial V}{\partial y} \hat{a}_y + \frac{\partial V}{\partial z} \hat{a}_z$$

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$$\text{SPHERICAL } \nabla V = \frac{\partial V}{\partial r} \hat{a}_r + \frac{1}{r} \frac{\partial V}{\partial \theta} \hat{a}_\theta + \frac{1}{r \sin \theta} \frac{\partial V}{\partial \phi} \hat{a}_\phi$$

CURL

$$\text{CARTESIAN } \nabla \times \vec{H} = \left(\frac{\partial H_z}{\partial y} - \frac{\partial H_y}{\partial z} \right) \hat{a}_x + \left(\frac{\partial H_x}{\partial z} - \frac{\partial H_z}{\partial x} \right) \hat{a}_y + \left(\frac{\partial H_y}{\partial x} - \frac{\partial H_x}{\partial y} \right) \hat{a}_z$$

$$\text{CYLINDRICAL } \nabla \times \vec{H} = \left(\frac{1}{\rho} \frac{\partial H_z}{\partial \phi} - \frac{\partial H_\phi}{\partial z} \right) \hat{a}_\rho + \left(\frac{\partial H_\rho}{\partial z} - \frac{\partial H_z}{\partial \rho} \right) \hat{a}_\phi + \frac{1}{\rho} \left(\frac{\partial (\rho H_\phi)}{\partial \rho} - \frac{\partial H_\phi}{\partial \phi} \right) \hat{a}_z$$

$$\text{SPHERICAL } \nabla \times \vec{H} = \frac{1}{r \sin \theta} \left(\frac{\partial (H_\phi \sin \theta)}{\partial \theta} - \frac{\partial H_\theta}{\partial \phi} \right) \hat{a}_r + \frac{1}{r} \left(\frac{1}{\sin \theta} \frac{\partial H_r}{\partial \phi} - \frac{\partial (r H_\phi)}{\partial r} \right) \hat{a}_\theta + \frac{1}{r} \left(\frac{\partial (r H_\theta)}{\partial r} - \frac{\partial H_r}{\partial \theta} \right) \hat{a}_\phi$$

LAPLACIAN

$$\text{CARTESIAN } \nabla^2 V = \frac{\partial^2 V}{\partial x^2} + \frac{\partial^2 V}{\partial y^2} + \frac{\partial^2 V}{\partial z^2}$$

$$\text{CYLINDRICAL } \nabla^2 V = \frac{1}{\rho} \frac{\partial}{\partial \rho} \left(\rho \frac{\partial V}{\partial \rho} \right) + \frac{1}{\rho^2} \frac{\partial^2 V}{\partial \phi^2} + \frac{\partial^2 V}{\partial z^2}$$

$$\text{SPHERICAL } \nabla^2 V = \frac{1}{r^2} \frac{\partial}{\partial r} \left(r^2 \frac{\partial V}{\partial r} \right) + \frac{1}{r^2 \sin \theta} \frac{\partial}{\partial \theta} \left(\sin \theta \frac{\partial V}{\partial \theta} \right) + \frac{1}{r^2 \sin^2 \theta} \frac{\partial^2 V}{\partial \phi^2}$$

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1. An uniform Electric Field Intensity in certain region is given by $\vec{E} = ya_x - xy a_y + za_z$. Transform this field vector into cylindrical co-ordinate at a point P(2, 45°, 3). [5]
2. A uniform line charge density of 150 $\mu\text{C/m}$ lies at $x = 2$, $z = -4$ and a uniform sheet of charge equal to 25 nC/m^2 is placed at $z = 5$ plane. Find \vec{D} at point (1, 2, 4) and convert it to the spherical coordinate system. [5+3]
3. Given the potential function $V = \frac{20\cos\theta}{r^2}$ V in free space and point P is located at $r = 3\text{m}$, $\theta = 60^\circ$, $\phi = 30^\circ$ find: a) \vec{E}_P b) $\frac{dV}{dN}$ at P c) unit normal vector at P d) ρ_V at P. [2+1+1+2]
4. Define Relaxation time Constant (RTC). Derive an expression for RTC. Given the vector current density $\vec{J} = 10\rho^2 z a_\rho - 4\rho \cos^2\phi a_\phi$ mA/m². Find the current flowing outward through the circular band $\rho = 3$, $0 < \phi < 2\pi$, $2 < z < 2.8$. [1+3+4]
5. Show that the vector magnetic potential can be defined in both the regions where \vec{J} is equal or non-equal to zero. Use the concept of vector magnetic potential to derive the Magnetic Field Intensity due to an infinite current carrying filament carrying DC current I. [3+5]
6. State Stoke's theorem. Given the field $\vec{H} = \frac{1}{2} \cos\left(\frac{\phi}{2}\right) a_\rho - \sin\left(\frac{\phi}{2}\right) a_\phi$ A/m, evaluate both sides of Stroke's theorem for the path formed by the intersection of the cylinder $\rho = 3$ and the plane $z = 2$, and for the surface defined by $\rho = 3$, $0 \leq z \leq 2$, and $z = 0$, $0 \leq \rho \leq 3$. [1+7]
7. State Faradays Law. Correct the equation $\nabla \times \vec{H} = \vec{J}$ with necessary arguments and derivation for time varying field. [2+4]
8. Derive the expressions for reflection coefficient and transmission coefficient for the reflection of uniform waves at normal incidence. [8]

9. At 50 MHz, a lossy dielectric material is characterized by $\epsilon = 3.6\epsilon_0$, $\mu = 2.1\mu_0$ and $\sigma = 0.08 \text{ S/m}$. If $\vec{E}_s = 6e^{-\gamma x} \hat{a}_z \text{ V/m}$, Compute: [2+2+4]
- Propagation Constant
 - Wavelength
 - \vec{H}_s
10. State the condition for lossless transmission line. A lossless transmission line is 80 cm long and operates at a frequency of 600 MHZ. The line parameters are $L = 0.25\mu\text{H/m}$ and $C = 100 \text{ pF/m}$. Find a) characteristics impedance b) phase constant c) phase velocity. [1+2+3+2]
11. Differentiate between Transmission line and waveguide. Consider a rectangular waveguide with $\epsilon_r = 2$, $\mu_r = 1$ with dimensions $a = 1.07 \text{ cm}$, $b = 0.43 \text{ cm}$ find the cut off frequency for TM_{11} mode and the dominant mode. [1+4]
12. Write short notes on antenna and its parameters. [2]

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1. Define a vector field. A field vector is given by an expression

$$\vec{A} = \frac{1}{\sqrt{x^2 + y^2 + z^2}} \left(X \hat{a}_x + Y \hat{a}_y + Z \hat{a}_z \right), \text{ transform this vector in cylindrical coordinate system at point } (2, 30^\circ, 6) \quad [2+3]$$

2. Given the flux density $\vec{D} = (2 \cos \theta / r^3) \hat{a}_r + (\sin \theta / r^3) \hat{a}_\theta \text{ C/m}^2$, evaluate both sides of the divergence theorem for the region defined by $1 < r < 2, 0 < \theta < \frac{\pi}{2}, 0 < \phi < \frac{\pi}{2}$. [8]
3. Define electric dipole and polarization. The region $z < 0$ contains a dielectric material for which $\epsilon_{r1} = 2.5$ while the region $z > 0$ is characterized by $\epsilon_{r2} = 4$. Let $\vec{E}_1 = -30 \hat{a}_x + 50 \hat{a}_y + 70 \hat{a}_z \text{ V/m}$. Find: (a) \vec{E}_2 (b) \vec{D}_2 (c) polarization in region 2 (\vec{P}_2) . [2+2+2+1+1]
4. State the uniqueness theorem and prove this theorem for Laplace's equation. [1+5]
5. A current density in certain region is given as: $\vec{J} = 20 \sin \theta \cos \phi \hat{a}_r + \frac{1}{r} \hat{a}_\phi \text{ A/m}^2$, Find: [5+3]
- i) The average value of J_r over the surface $r = 1, 0 < \theta < \pi/2, 0 < \phi < \pi/2$
 - ii) $\frac{\delta p_v}{\partial t}$
6. Show that $\nabla \times \vec{E} = 0$ for static electric field. The region $y < 0$ (Region 1) is air and $y > 0$ (Region 2) has $\mu_r = 10$. If there is a uniform magnetic field $\vec{H} = 5 \hat{a}_x + 6 \hat{a}_y + 7 \hat{a}_z \text{ A/m}$ in region 1, find \vec{B} and \vec{H} in region 2. [2+3+3]
7. Find the amplitude of the displacement current density in a metallic conductor at 60 Hz, if $\epsilon = \epsilon_0, \mu = \mu_0, \sigma = 5.8 \times 10^7 \text{ S/m}$, and $\vec{J} = \sin(377t - 117.1z) \hat{a}_x \text{ MA/m}^2$. [5]

8. Explain the phenomena when a plane wave is incident normally on the interface between two different Medias. Derive the expression for reflection and transmission coefficient. [8]
9. A uniform plane wave in non-magnetic medium has $\vec{E} = 50 \cos(10^8 t + 2z) \hat{a}_y$ V/m . Find:
- The direction of propagation
 - Phase constant β , wavelength λ , velocity v_p , relative permittivity ϵ_r , intrinsic impedance η
 - \vec{H}
- [1+5+2]
10. Determine the primary constants (R , L , C and G) on the transmission line when the measurement on the line at 1 KHz gave the following results: $z_0 = 710 \angle -16^\circ$, $\alpha = 0.01$ neper/m and $\beta = 0.035$ rad/m. [8]
11. Explain the modes supported by a rectangular waveguide. Calculate the cut off frequencies of the first four propagating modes for an air filled copper waveguide with dimension $a = 2.5$ cm, $b = 1.2$ cm. [2+4]
12. Write short notes on antenna and its types. [2]

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Examination Control Division
 2073 Chaitra

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1. Express a scalar potential field $V = x^2 + 2y^2 + 3z^2$ in spherical coordinates. Find value of V at a point P(2, 60°, 90°). [3+2]
2. Derive the expression of Electric field intensity due to a line charge using Gauss Law. Find Electric flux density at point P(5,4,3) due to a uniform line charge of 2 nC/m at $x = 5$, $y = 3$, point charge 12 nC at Q(2,0,6) and uniform surface charge density of 0.2 nC/m² at $x = 2$. [4+4]
3. State the physical significance of divergence. Derive the Divergence theorem. Given the potential $V = \frac{10}{r^2} \sin\theta \cos\phi$; find the electric flux density \vec{D} at $\left(2, \frac{\pi}{2}, 0\right)$. [2+2+3]
4. Derive Laplace's equation. Find the capacitance of a co-axial cable using Laplace's equation. [1+5]
5. State Ampere's circuital law. By using Biot Savart's law, derive an expression for magnetic field intensity (\vec{H}) due to an infinite length filament carrying a direct current I. [2+6]
6. Flux density at medium with $\mu_1 = 15$ is $\vec{B}_1 = 1.2a_x + 8a_y + 4a_z T$. Find \vec{B} , \vec{H} and the angles between the field vectors and tangent to the interface at second medium, if second medium has $\mu_2 = 1$, and interface plane is $z = 0$. [3+2+3]
7. State and derive the expression of motional emf (electromotive force). Consider two parallel conductors placed at $x = 0$ and $x = 5$ cm in a magnetic field $\vec{B} = 6a_z$ mWb/m². A high resistance voltmeter is connected at one end and a conducting bar is sliding at other end with velocity $\vec{v} = 18a_y$ m/s. Calculate the induced voltage and show the polarity of induced voltage across the voltmeter. [1+3+3]
8. What is standing wave? Derive the equation of Electric field and Magnetic field and SWR of standing wave? [1+7]

9. An EM wave travels in free space with the electric field component $\vec{E} = \left(15\vec{a}_y - 5\vec{a}_z \right) \cos(\omega t - 3y + 5z) \text{ V/m}$. Find (a) ω and λ (b) the magnetic field component. [2+2+3]
10. A 50Ω lossless transmission line is 30 m long and is terminated with a load $Z_L = 60 + j40\Omega$. The operating frequency is 20 MHz and velocity on the line is $2.5 \times 10^8 \text{ m/s}$. Find [2+2+4]
- i) Reflection coefficient
 - ii) Standing wave ratio
 - iii) Input impedance
11. Explain TE and TM modes? Consider a rectangular waveguide with $\epsilon_r = 2.25$ and $\mu_r = 1$ with dimensions $a = 1.07$, $b = 0.43$. Find the cut-off frequency for TM_{11} mode and dominant mode. [2+4]
12. Write short notes on antenna and its type. [2]

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1. Transform $\vec{A} = 10\vec{a}_x - 8\vec{a}_y + 6\vec{a}_z$; at point p(10,-8,6) to cylindrical coordinate system. [5]
2. A line charge of 8nC/m is located at $x = -1$, $y = 2$, a point charge of 6mC at $y = -4$ and a surface charge of 30 pC/m^2 at $z = 0$. If the potential at origin is 100V , find the potential at P (4,1,3). [7]
3. Explain the Continuity equation. The current density in certain region is approximated by $\vec{J} = \left(\frac{0.1}{r}\right) e^{-10^6 t} \vec{a}_r \text{A/m}^2$ in spherical coordinates. (a) How much current is crossing the surface $r = 50 \text{cm}$ at $t = 1 \mu\text{s}$? (b) Find $\rho_v(r,t)$ assuming that $\rho_v \rightarrow 0$ as $t \rightarrow \infty$. [2+6]
4. Find the equation for Energy Density in the electrostatic field. [6]
5. Differentiate between scalar and vector magnetic potential. Derive an expression for the magnetic field intensity (\vec{H}) at a point due to an infinite filament carrying a direct current I, placed on z-axis using ampere's circuital law. [2+6]
6. State and prove Stoke's theorem. Given $\vec{H} = 10 \sin \theta \vec{a}_r$ in free space. Find the current in \vec{a}_r direction having $r = 3, 0 \leq \theta \leq 90^\circ, 0 \leq \phi \leq 90^\circ$. [3+5]
7. Within a certain region, $\epsilon = 10^{-11} \text{ F/m}$ and $\mu = 10^{-5} \text{ H/m}$.
If $\vec{B}_x = 2 \times 10^{-4} \cos 10^5 t \sin 10^{-3} y \vec{a}_x \text{T}$: (a) Use $\nabla \times \vec{H} = \epsilon \frac{\partial \vec{E}}{\partial t}$ to find \vec{E} ; (b) Find the total magnetic flux passing through the surface $x = 0, 0 \leq y \leq 40 \text{m}, 0 \leq z \leq 2 \text{m}$, at $t = 1 \mu\text{s}$. [4+4]
8. Derive an expression for standing wave ratio of uniform plane wave in terms of reflection coefficient. Find the reflection coefficient for the interface between air and fresh water ($\epsilon = 81\epsilon_0, \sigma \approx 0$), in case of normal incidence. [5+3]

9. The magnetic field intensity (\vec{H}) in free space is given as,

$$\vec{H}(x,t) = 10 \cos(10^8 t + \beta x) \vec{a}_y \text{ A/m}$$
 find:

[2+1+3]

- a) Phase constant (β)
- b) Wavelength
- c) $|\vec{E}(x,t)|$ at P (0.1,0.2,0.3) at $t = 1 \text{ nS}$

10. A 300Ω transmission line is lossless, 0.25λ long, and is terminated in $Z_L = 500 \Omega$. The line has a generator with $90^\circ \angle 0^\circ \text{V}$ in series with 100Ω connected to the input. Find (a) the load voltage (b) voltage at the midpoint of the line.

[4+4]

11. Determine the cut-off frequency for an air filled rectangular waveguide with $a = 2.5 \text{ cm}$ and $b = 1.25 \text{ cm}$ for TE_{11} mode.

[4]

12. Write short notes on:

[2+2]

- a) Loss tangent
- b) Antenna types and properties

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1. Express the uniform vector field $\vec{F} = 5\vec{a}_x$ in (a) cylindrical components (b) spherical components. [2+3]
2. Derive the expression for the electric field intensity due to an infinitely long line charge with uniform charge density ρ_L by using Gauss's law. A uniform line charge density of 20 nC/m is located at $y=3$ and $z=5$. Find \vec{E} at P(5,6,1) [4+4]
3. Derive an expression to calculate the potential due to a dipole in terms of the dipole moment (\vec{p}) . A dipole for which $\vec{p} = 3\vec{a}_x - 5\vec{a}_y + 10\vec{a}_z$ nC.m is located at the point (1,2,-4). Find \vec{E} at P. [4+4]
4. Assuming that the potential V in the cylindrical coordinate system is function of ρ only, solve the Laplace's equation and derive the expression for the capacitance of coaxial capacitor of length L using the same solution of V. Assume the inner conductor of radius a is at potential V_0 with respect to the conductor of radius b. [6]
5. State and derive expression for Stoke's theorem. Evaluate the closed line integral of \vec{H} from $P_1(5,4,1)$ to $P_2(5,6,1)$ to $P_3(0,6,1)$ to $P_4(0,4,1)$ to P_1 using straight line segments, if $\vec{H} = 0.1y^3\vec{a}_x + 0.4x\vec{a}_z$ A/m. [1+3+4]
6. Define scalar magnetic potential and show that it satisfies the Laplace's equation. Given the vector magnetic potential $\vec{A} = -(\rho^2/4)\hat{a}_z$ Wb/m, calculate the total magnetic flux crossing the surface $\phi = \pi/2$, $1 \leq \rho \leq 2$ m and $0 \leq z \leq 5$ m. [1+2+5]
7. How does $\nabla \times \vec{H} = \vec{J}$ conflict with continuity equation in time varying fields. How is this conflict rectified in such fields? [2+3]
8. Derive the expression for electric and magnetic fields for a uniform plane wave propagating in a perfect dielectric space. [5+3]
9. A lossless dielectric material has $\sigma = 0, \mu_r = 1, \epsilon_r = 4$. An electromagnetic wave has magnetic field expressed as $\vec{H} = -0.1\cos(\omega t - z)\vec{a}_x + 0.5\sin\cos(\omega t - z)\vec{a}_y$ A/m. Find:
 - Angular frequency (ω)
 - Wave impedance (η)
 - \vec{E}
[2+2+4]

10. Consider a two-wire 40Ω line ($Z_0 = 40\Omega$) connecting the source of 80 V , 400 kHz with series resistance 10Ω to the load of $Z_L = 60\Omega$. The line is 75 m long and the velocity on the line is $2.5 \times 10^8 \text{ m/s}$. Find the voltage $V_{in,s}$ at input end and $V_{L,s}$ at output end of the transmission line. [8]

11. Why does a hollow rectangular waveguide not support TEM mode? A rectangular air-filled waveguide has a cross-section of $45 \times 90 \text{ mm}$. Find the cut-off frequencies of the first four propagating modes. [2+4]

12. Write short notes on antenna and its types. [2]

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CURL

$$\text{CARTESIAN } \nabla \times \vec{H} = \left(\frac{\partial H_z}{\partial y} - \frac{\partial H_y}{\partial z} \right) \hat{a}_x + \left(\frac{\partial H_x}{\partial z} - \frac{\partial H_z}{\partial x} \right) \hat{a}_y + \left(\frac{\partial H_y}{\partial x} - \frac{\partial H_x}{\partial y} \right) \hat{a}_z$$

$$\text{CYLINDRICAL } \nabla \times \vec{H} = \left(\frac{1}{\rho} \frac{\partial H_z}{\partial \phi} - \frac{\partial H_\phi}{\partial z} \right) \hat{a}_\rho + \left(\frac{\partial H_\rho}{\partial z} - \frac{\partial H_z}{\partial \rho} \right) \hat{a}_\phi + \frac{1}{\rho} \left(\frac{\partial (\rho H_\phi)}{\partial \rho} - \frac{\partial H_\rho}{\partial \phi} \right) \hat{a}_z$$

$$\text{SPHERICAL } \nabla \times \vec{H} = \frac{1}{r \sin \theta} \left(\frac{\partial (H_\phi \sin \theta)}{\partial \theta} - \frac{\partial H_\theta}{\partial \phi} \right) \hat{a}_r + \frac{1}{r} \left(\frac{1}{\sin \theta} \frac{\partial H_r}{\partial \phi} - \frac{\partial (r H_\phi)}{\partial r} \right) \hat{a}_\theta + \frac{1}{r} \left(\frac{\partial (r H_\theta)}{\partial r} - \frac{\partial H_r}{\partial \theta} \right) \hat{a}_\phi$$

LAPLACIAN

$$\text{CARTESIAN } \nabla^2 V = \frac{\partial^2 V}{\partial x^2} + \frac{\partial^2 V}{\partial y^2} + \frac{\partial^2 V}{\partial z^2}$$

$$\text{CYLINDRICAL } \nabla^2 V = \frac{1}{\rho} \frac{\partial}{\partial \rho} \left(\rho \frac{\partial V}{\partial \rho} \right) + \frac{1}{\rho^2} \frac{\partial^2 V}{\partial \phi^2} + \frac{\partial^2 V}{\partial z^2}$$

$$\text{SPHERICAL } \nabla^2 V = \frac{1}{r^2} \frac{\partial}{\partial r} \left(r^2 \frac{\partial V}{\partial r} \right) + \frac{1}{r^2 \sin \theta} \frac{\partial}{\partial \theta} \left(\sin \theta \frac{\partial V}{\partial \theta} \right) + \frac{1}{r^2 \sin^2 \theta} \frac{\partial^2 V}{\partial \phi^2}$$

Exam.	New Back (2066 & Later Batch)		
Level	BE	Full Marks	80
Programme	BEL, BEX, BCT	Pass Marks	32
Year / Part	H / I	Time	3 hrs.

Subject: - Electromagnetics (EX503)

- ✓ Candidates are required to give their answers in their own words as far as practicable.
- ✓ Attempt All questions.
- ✓ The figures in the margin indicate Full Marks.
- ✓ Necessary formulas are attached herewith.
- ✓ Assume suitable data if necessary.
- ✓ Assume that the **Bold Faced** letter represents a vector and $\mathbf{a}_{\text{subscript}}$ represents a unit vector.

- (1) Express the vector field, $\mathbf{G} = (x^2 + y^2)^{-1}(x\mathbf{a}_x + y\mathbf{a}_y)$ in cylindrical components and cylindrical variables. [5]
- (2) Find \mathbf{D} at the point (-3, 4, 2) if the following charge distributions are present in free space: point charge, 12 nC, at P(2, 0, 6); uniform line charge density, 3 nC/m, at $x = -2$, $y = 3$; uniform surface charge density, 0.2 nC/m² at $x = 2$. [7]
- (3) Two uniform line charges, 8 nC/m each, are located at $x = 1$, $z = 2$, and at $x = -1$, $y = 2$ in free space. If the potential at the origin is 100V, find V at P(4, 1, 3). [7]
- (4) State the Uniqueness theorem and prove that the solution of Poisson's equation is unique. [1+6]
- (5) Write the equation of the Vector Magnetic Potential in differential form. Using the same equation, derive the equation for magnetic field intensity at a point due to an infinite filament carrying a uniformly distributed dc current I. [1+5]
- (6) Calculate the value of the vector current density; (a) in cylindrical coordinates at P_1 ($\rho = 1.5$, $\phi = 90^\circ$, $z = 0.5$) if $\mathbf{H} = \frac{2}{\rho}(\cos 0.2\phi) \mathbf{a}_\rho$. [3+3]
 (b) in spherical coordinates at P_2 ($r = 2$, $\theta = 30^\circ$, $\phi = 20^\circ$) if $\mathbf{H} = \frac{1}{\sin \theta} \mathbf{a}_\theta$.
- (7) State and derive the Stoke's theorem. [1+3]
- (8) What is an input intrinsic impedance? Derive an expression for the input intrinsic impedance using the concept of reflection of uniform plane waves. [2+6]

- (9) The electric field amplitude of a uniform plane wave propagating in the free space in \mathbf{a}_z direction is 250 V/m. If $\mathbf{E} = E_x \mathbf{a}_x$ and $\omega = 1.00 \text{ Mrad/s}$, find: (a) the frequency; (b) the wavelength; (c) the period; (d) the amplitude of \mathbf{H} . [2+2+1+3]
- (10) Find the amplitude of the displacement current density inside a typical metallic conductor where $f = 1 \text{ kHz}$, Conductivity $\sigma = 5 \times 10^7 \text{ mho/m}$, dielectric constant $\epsilon_R = 1$; and the conduction current density $\mathbf{J} = 10^7 \sin(6283 t - 444 z) \mathbf{a}_x \text{ A/m}^2$. [6]
- (11) A 50Ω lossless line has a length of 0.4λ . The operating frequency is 300 MHz. A load $Z_L = 40 + j30 \Omega$ is connected at $z = 0$, and the Thevenin equivalent source at $z = -l$ is $12\angle 0^\circ$ in series with $Z_{Th} = 50 + j0 \Omega$. Find: (a) The Reflection Coefficient Γ (b) The Voltage Standing Wave Ratio (VSWR) and (c) The input Impedance Z_{in} . [2+2+4]
- (12) Explain why it is not possible to use waveguides at lower frequencies? Explain the transverse electric (TE) and transverse magnetic (TM) modes used in rectangular waveguides. [2+4]
- (13) Give the definition of an antenna. Explain the properties of any one type of antenna that you have studied during your electromagnetics course. [1+1]

Exam.	Regular		
Level	BE	Full Marks	80
Programme	BEL, BEX, BCT	Pass Marks	32
Year / Part	II / I	Time	3 hrs.

Subject: - Electromagnetic (EX503)

- ✓ Candidates are required to give their answers in their own words as far as practicable.
- ✓ Attempt All questions.
- ✓ The figures in the margin indicate Full Marks.
- ✓ Necessary formula sheet is attached herewith.
- ✓ $\vec{a}_{\text{subscript}}$ denote a unit vector along the direction given by the subscript.
- ✓ Assume suitable data if necessary.

1. Transform the vector $4\vec{a}_x - 2\vec{a}_y - 4\vec{a}_z$ into spherical coordinates at point P(-2,-3,4) [5]
2. State and write the mathematical equation of Gauss Law. Using the same law, derive an expression for electric field intensity (\vec{E}) in between the two co-axial cylindrical conductors having inner radius 'a' and outer radius 'b', each infinite in extent and assuming a surface charge density ρ_s on the outer surface of the inner conductor. [1+6]
3. State the physical significance of potential gradient. Assuming that the potential V in the spherical coordinate system is a function of r only, solve the Laplacian equation and derive the expression for the capacitance of a spherical capacitor using the same solution of V. [2+6]
4. Within the cylinder $\rho = 2$, $0 < z < 1$ the potential given by: $V = 100 + 50\rho + 150\rho \sin\phi$ find: [2+1+2+1]
 - a) Electric Field Intensity (\vec{E}) at P (1, 60° , 0.5) in free space
 - b) Potential Gradient $\left(\frac{dV}{dN}\right)$
 - c) Volume Charge Density (ρ_v) at P($1, 60^\circ, 0.5$) in free space
 - d) How much charge lies within the cylinder?
5. State the physical significance of Curl. Evaluate both sides of stokes theorem for the field $\vec{A} = 6xy \vec{a}_x - 3y^2 \vec{a}_y$ A/m and the rectangular path around the region; $2 \leq x \leq 5$, $-1 \leq y \leq 1$, $z = 0$. Let the positive direction of ds be \vec{a}_z . [2+6]
6. Explain the physical significance of the equation $\oint_s \vec{B} \cdot d\vec{s} = 0$. Given the vector magnetic potential $\vec{A} = \rho^2/8 \vec{a}_z$ Wb/m. Calculate the total magnetic flux crossing the surface $\phi = \pi/4$, $1 \leq \rho \leq 3$ m, $0 \leq z \leq 5$ m. [2+6]

7. Explain motional emf and transformer emf with necessary mathematical derivations. A straight conductor of 0.2m lies along x-axis with one end at the origin. If this conductor is subjected to the magnetic flux density $\vec{B} = 0.08 \vec{a}_y \text{ T}$ and velocity $v = 2.5 \sin 10^3 t \vec{a}_z \text{ m/s}$. Calculate the emf induced in the conductor. [6+2]
8. Define Transverse Electromagnetic (TEM) wave. Derive an expression electric field for a uniform plane wave propagating in a perfect dielectric media. [7+1]
9. A uniform plane wave in free space at a frequency of 12 MHz is given by $\vec{E} = 200 \cos(\omega t + 120x + 30^\circ) \vec{a}_y \text{ V/m}$, find (a) $|E_{\max}|$ (b) H at $x = 40\text{mm}$ and $t = 340\text{ps}$. [3+3]
10. A lossless transmission line with $Z_0 = 50\Omega$ has a length of 0.4λ . The operating frequency is 300MHz and it is terminated with a load $Z_L = 40+j30\Omega$. Find: [2+2+4]
- Reflection coefficient (Γ)
 - Standing wave ratio on the line (SWR)
 - Input impedance (Z_{in})
11. Explain Transverse Electric Mode and Transverse Magnetic Mode of a waveguide. [2+2]
12. Write short notes on: [2×2]
- Skin depth
 - Antenna and its types

Exam.	New Back (2066 & Later Batch)		
Level	BE	Full Marks	80
Programme	BEX, BCT, BEL	Pass Marks	32
Year / Part	II / I	Time	3 hrs.

Subject: - Electromagnetic (EX503)

- ✓ Candidates are required to give their answers in their own words as far as practicable.
- ✓ Attempt All questions.
- ✓ The figures in the margin indicate Full Marks.
- ✓ Assume that the **Bold Faced** letter represents a vector and $\mathbf{a}_{\text{subscript}}$ represents a unit vector.
- ✓ Necessary figures are attached herewith.
- ✓ Assume suitable data if necessary.

1. At point P(-3,-4,5), express that vector that extends from P to Q(2,0,-1) in spherical coordinates. [5]
2. A point charge of $6\mu\text{C}$ (micro coulomb) is located at the origin, a uniform line charge density of 180nC/m lies along the x axis, and a uniform sheet of charge equal to 25nC/m^2 lies in the $z = 0$ plane. Find \mathbf{D} at B (1,2,4). [7]
3. Derive the equation for Energy Density in the electrostatic field. [7]
4. Derive the Laplacian Equation. Assuming that the potential V in the cylindrical coordinate system is the function of ' ρ ' only, solve the Laplacian Equation by Integration Method and derive the expression for the Capacitance of the Cylindrical Capacitor using the same solution of V. [2+5]
5. A current of 0.3 ampere in the \mathbf{a}_z direction in free space is in a filament parallel to the z-axis and passing through the point (1,-2,0). Find the Magnetic Field Intensity \mathbf{H} at (0,1,0) if the filament lies in the interval $-4 < z < 4$. [6]
6. State and derive the Stoke's theorem. [1+4]
7. Calculate the value of the vector current density in cylindrical coordinates at $P(\rho=1.5, \phi=90^\circ, z=0.5)$ if $\mathbf{H} = \frac{2}{\rho} (\cos 0.2\phi) \mathbf{a}_\rho$. [5]
8. An Electric field \mathbf{E} in free space is given as $\mathbf{E} = 200 \cos(10^8 t - \beta y) \mathbf{a}_z$ V/m. Find:
 - Phase Constant (β);
 - Wavelength (λ);
 - Magnetic Field Intensity \mathbf{H} at P (-0.1, 1.5, -0.4) at $t = 4$ nS.
[2+2+4]
9. Explain the term skin depth and loss tangent. Using Poynting Vector deduce the time-average power density for a lossless dielectric. [2+2+4]

10. Select the value of K so that each of the following pairs of fields satisfies Maxwell's equations in a region where $\sigma = 0$ and $\rho_v = 0$: [6]
- $\mathbf{D} = 5x \mathbf{a}_x - 2y \mathbf{a}_y + Kz \mathbf{a}_z \mu\text{C/m}^2$;
- $\mathbf{B} = 2 \mathbf{a}_y \text{ mT}$,
if $\mu = 0.25 \text{ H/m}$ and $\epsilon = 0.01 \text{ F/m}$.
11. A lossless transmission line with $Z_0 = 50 \Omega$ is 200 m long. It is terminated with a load, $Z_L = 30 + j60 \Omega$, and operated at a frequency of 0.5 MHz. Let the velocity $v = 0.6c$ on the line where $c = \text{velocity of light} = 3 \times 10^8 \text{ m/s}$. Find: [2+2+4]
- (a) The reflection coefficient (Γ).
 - (b) The voltage standing wave ratio on the line (VSWR).
 - (c) The input impedance (Z_{in}).
12. Explain why it is not possible to use waveguides at lower frequency? Write short notes on different types of modes used in rectangular waveguides. [2+4]
13. Give the definition of an antenna and list the different types of antenna that you have studied during your electromagnetics course. [1+1]

9. Find the amplitude of displacement current density inside a typical metallic conductor where $f = 1\text{KHz}$, $\sigma = 5 \times 10^7 \text{ mho/m}$, $\epsilon_r = 1$ and the conduction current density is
$$\vec{J} = 10^7 \sin(6283t - 444z) \hat{a}_y \text{ A/m}^2$$

[4]

10. Write all the Maxwell equations for the time varying field point form as well as integral form.

[4]

11. A lossless transmission line with $Z_0 = 50 \Omega$ with length 1.5 m connects a voltage $V_g = 60\text{V}$ source to a terminal load of $Z_L = (50+j50) \Omega$. If the operating frequency $f = 100 \text{ MHz}$, generator impedance $Z_g = 50 \Omega$ and speed of wave equal to the speed of the light. Find the distance of the first voltage maximum from the load. What is the power delivered to the load?

[4+4]

12. What are the techniques that can be taken to match the transmission line with mismatched load? Explain any one.

[2]

13. Write short notes on:

[2×3]

- a) Modes in rectangular wave guide
- b) Antenna and its types

Exam.		Regular	
Level	BE	Full Marks	80
Programme	BEL, BEX, BCT	Pass Marks	32
Year / Part	II / I	Time	3 hrs.

Subject: - Electromagnetics (EX503)

- ✓ Candidates are required to give their answers in their own words as far as practicable.
- ✓ Attempt All questions.
- ✓ The figures in the margin indicate Full Marks.
- ✓ Necessary formula are attached herewith.
- ✓ Assume suitable data if necessary.

1. Transform the Vector $\vec{A} = y \vec{a}_x + x \vec{a}_y + z \vec{a}_z$ into cylindrical co-ordinates at a point $p(2, 45^\circ, 5)$ [5]

2. Along the z-axis there is a uniform line of charge with $\rho_L = 4\pi \text{ Cm}^{-1}$ and in the x = 1 plane there is a surface charge with $\rho_s = 20 \text{ Cm}^{-2}$. Find the Electric Flux Density at $(0.5, 0, 0)$ [6]

3. Define Uniqueness theorem. Assuming that the potential V in the cylindrical coordinate system is the function of 'ρ' only, solve the Laplacian Equation by integration method and derive the expression for the Capacitance of the co-axial capacitor using the same solution of V. [2+5]

4. Define Electric Dipole and Polarization. Consider the region $y < 0$ be composed of a uniform dielectric material for which the relative permittivity (ϵ_r) is 3.2 while the region $y > 0$ is characterized by $\epsilon_r = 2$. Let the flux density in region 1 be [2+3+3]

$$\vec{D}_1 = -30 \vec{a}_x + 50 \vec{a}_y + 70 \vec{a}_z \text{ nC/m}^2.$$

Find:

a) Magnitude of Flux density and Electric fields intensity at region 2.
 b) Polarization (\vec{P}) in region 1 and region 2

5. State Ampere's circuital law and stoke's theorem. Derive an expression for magnetic field intensity (\vec{H}) due to infinite current carrying filament using Biot Savart's Law. [1+2+5]

6. Differentiate between scalar and vector magnetic potential. The magnetic field intensity in a certain region of space is given as $\vec{H} = (2\rho + z) \vec{a}_\rho + \frac{2}{z} \vec{a}_z \text{ A/m}$. Find the total current passing through the surface $\rho = 2$, $\pi/4 < \phi < \pi/2$, $3 < z < 5$, in the \vec{a}_ρ direction. [3+5]

7. State Faraday's law and correct the equation $\nabla \times \vec{E} = 0$ for time varying field with necessary derivation. Also modify the equation $\nabla \times \vec{H} = \vec{J}$ with necessary derivations for time varying field. [1+3+4]

8. Derive an expression for input intrinsic impendence using the concept of reflection of uniform plane waves. [6]

Exam.	New Back (2066 & Later Batch)		
Level	BE	Full Marks	80
Programme	BEL, BEX, BCT	Pass Marks	32
Year / Part	II / I	Time	3 hrs.

Subject: - Electromagnetics (EX 503)

- ✓ Candidates are required to give their answers in their own words as far as practicable.
- ✓ Attempt All questions.
- ✓ The figures in the margin indicate Full Marks.
- ✓ Necessary formulas are attached herewith.
- ✓ Assume suitable data if necessary.

1. Given a vector field $\vec{D} = \frac{x\hat{a}_x + y\hat{a}_y}{x^2 + y^2}$, evaluate D at the point where $\rho=2$, $\Phi=0.2\pi$, and $Z=5$ in both cylindrical and Cartesian components. [5]
2. Define Gauss's law. A co-axial cable has inner conductors of radius r_1 , outer conductor of radius r_2 . Surface charge density on the surface of inner conductors is ρ_s . Use Gauss's law to derive an expression for electric field intensity in the region $r_1 \leq r \leq r_2$. [2+5]
3. Define potential field. Assuming that the potential V in the spherical coordinate system is function of r only, solve the laplacian equation and derive the expression for the capacitance of a spherical capacitor using the same solution of V. [1+6]
4. Use boundary condition to find E_2 in the medium 2 with boundary located at plane $Z=0$. Medium 1 is perfect dielectric characterized by $\epsilon_r=2.5$, medium 2 is perfect dielectric characterized by $\epsilon_{r2}=5$, electric field in medium 1 is $\vec{E}_1 = \hat{a}_x + 3\hat{a}_y + 3\hat{a}_z$ v/m. [7]
5. Given the magnetic vector potential $\vec{A} = -\frac{\rho^2}{4}\hat{a}_z$ Wb/m, Calculate the total magnetic flux crossing the surface $\Phi=\pi/2$, $1 \leq \rho \leq 2m$, $0 \leq Z \leq 5m$. [6]
6. Find the boundary condition for H and B at the interface between two isotropic homogeneous linear materials with permeabilities μ_1 and μ_2 . [6]
7. For magnetic vector potential given in cylindrical co-ordinate system as $\vec{A} = 5r^3 \hat{a}_z$ Wb/m in free space, find the magnetic field intensity, \vec{H} . [4]
8. Derive the equations to show that the electric field and the magnetic field component are in same phase for the wave propagation in perfect dielectric medium. [8]
9. Derive expressions for reflection co-efficient and transmission co-efficient for the case of normal incidence at boundary between two dielectric media where medium 1 is characterized by permittivity ϵ_1 , permeability μ_1 and medium 2 is characterized by permittivity ϵ_2 , permeability μ_2 . Also explain why the concept of reflection is necessary. [5+3]
10. Write down the Maxwell's equations in point and phasor form for time varying fields. Define the pointing vector. [4+2]
11. A load impedance of $(40+j70)\Omega$ terminates a 100Ω transmission line that is 0.3λ long. Find the reflection coefficient at the load and the voltage at the input of the line. [2+4]
12. Define transverse electric and transverse magnetic mode of wave propagation in wave guide. A rectangular wave guide has dimensions $a = 4.5\text{cm}$, $b=2.5\text{cm}$. The medium within wave guide has relative permittivity $\epsilon_r=1$, relative permeability $\mu_r=1$, conductivity $\sigma=0$ and conducting walls of wave guide are perfect conductors. Determine the cut off frequency for the modes $TE_{(1,0)}$, and $TM_{(1,1)}$. [2+2+2+2]
13. Write short notes on antenna and its properties. [2]

Exam.		Regular	
Level	BE	Full Marks	80
Programme	BEL, BEX, BCT	Pass Marks	32
Year / Part	II / I	Time	3 hrs.

Subject: - Electromagnetics (EX503)

- ✓ Candidates are required to give their answers in their own words as far as practicable.
- ✓ Attempt All questions.
- ✓ The figures in the margin indicate Full Marks.
- ✓ Necessary formulas are attached herewith.
- ✓ Assume suitable data if necessary.

1. Given a point P(-3, 4, 5), express the vector that extends from P to Q(2, 0, -1) in (a) Rectangular coordinates (b) Cylindrical coordinates (c) Spherical coordinates. [5]
2. Verify the divergence theorem (evaluate both sides of the divergence theorem) for the function $\vec{A} = r^2 \vec{a}_r + r \sin \theta \cos \phi \vec{a}_\theta$, over the surface of quarter of a hemisphere defined by: $0 < r < 3, 0 < \phi < \pi/2, 0 < \theta < \pi/2$. [6]
3. Given the potential field $V = 100xz/(x^2+4)$ volts in free space:
 - a) Find \vec{D} at the surface, $z=0$
 - b) Show that the $z=0$ surface is an equipotential surface
 - c) Assume that the $z=0$ surface is a conductor and find the total charge on that portion of the conductor defined by $0 < x < 2, -3 < y < 0$
[7]
4. State the uniqueness theorem and prove this theorem using Poisson's equation. [2+6]
5. State Amperes circuital law with relevant examples. The magnetic field intensity is given in a certain region of space as $\vec{H} = \frac{x+2y}{z^2} \vec{a}_y + \frac{2}{z} \vec{a}_z$ A/m. Find the total current passing through the surface $z = 4, 1 < x < 2, 3 < y < 5$, in the a_z direction. [3+5]
6. Define scalar and vector magnetic potential. Derive the expression for the magnetic field intensity at a point due to an infinite filament carrying a dc current I, placed on the z-axis, using the concept of vector magnetic potential. [3+5]
7. Define displacement current. Assume that dry soil has conductivity equal to 10^{-4} S/m, $\epsilon = 3\epsilon_0$ and $\mu = \mu_0$. Determine the frequency at which the ratio of the magnitudes of the conduction current density and displacement current density is unity. [2+5]
8. Derive the expression for electric field for a uniform plane wave propagating in a free space. [7]
9. State Poynting's theorem. An EM wave travels in free space with the electric field component $\vec{E} = (10\vec{a}_y + 5\vec{a}_z) \cos(\omega t + 2y - 4z)$ [V/m]. Find (a) ω and λ (b) the magnetic field component (c) the time average power in the wave. [1+2+2+2]
10. A lossless transmission line with $Z_0 = 50\Omega$ is 30m long and operates at 2 MHz. The line is terminated with a load $Z_L = (60+j40)\Omega$. If velocity (v) = 3×10^8 m/s on the line. Find (a) the reflection coefficient, (b) the standing wave ratio and the input impedance. [2+2+3]
11. Explain the modes supported by Rectangular waveguide. Define cutoff frequency and dominant mode for rectangular waveguide. [2+2+2]
12. Write short notes on:
 - a) Antenna types and properties
 - b) Quarter wave transformer
[2+2]

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INSTITUTE OF ENGINEERING
Examination Control Division
2068 Shrawan

Exam.	New Back (2066 Batch)		
Level	BE	Full Marks	80
Programme	BEL, BEX, BCT	Pass Marks	32
Year / Part	H/I	Time	3 hrs

Subject: Electromagnetics

- ✓ Candidates are required to give their answers in their own words as far as practicable.
- ✓ Attempt All questions.
- ✓ The figures in the margin indicate Full Marks.
- ✓ Necessary data are attached herewith.
- ✓ Assume suitable data if necessary.

1. Transform vector field $\vec{A} = r \cos\phi \hat{a}_r + z \hat{a}_z$ at point $P(1, 30^\circ, 2)$ in cylindrical co-ordinate system to spherical co-ordinate system. [5]
2. Use Gauss's law to derive expression for electric field intensity in co-axial cable in the region $a < r < b$ where a is radius of inner conductor and b is radius of outer conductor. [5]
3. Derive the expression for energy density in electrostatic field. [5]
4. For a potential field $\psi V = r^2 z^2 \sin\phi$ at point $P(1, 45^\circ, 1)$ in cylindrical co-ordinate system determine (a) Potential V (b) Electric field \vec{E} (c) Electric flux density \vec{D} (d) Volume charge density ρ_v and (e) unit vector in direction of \vec{E} . [6]
5. Differentiate between curl and divergence with required expression and physical meaning. [5]
6. State Stokes's theorem. Find magnetic field intensity at the origin if surface current $\vec{K} = 2\hat{a}_z$ A/m flows in the plane $x = -2$. [4]
7. If magnetic flux density, $\vec{B} = \frac{\mu_0}{4\pi} \int_L \frac{Idl \times \vec{R}}{|\vec{R}|^3}$, then derive the expression for vector magnetic potential. [7]
8. Write about transformer emf and motional emf. [6]
9. What is polarization of wave vector? A time harmonic uniform plane wave $\vec{E}(x, y, z, t)$ with polarization in \hat{a}_x direction, and frequency 150MHz is moving in free space in negative y direction and has maximum amplitude 2V/m. Determine (a) The angular frequency ω (b) Phase constant β (c) Expression for $\vec{E}(x, y, z, t)$, and (d) Expression $\vec{H}(x, y, z, t)$. [6]
10. What do you mean by pointing vector? Derive it's equation. [6]
11. If a transmission line having a characteristic impedance, $Z_0 = 200\Omega$, is operating at frequency 15MHz, with propagation constant $\gamma = j0.5\text{m}^{-1}$, then determine (a) Velocity of propagation (b) Wave length (c) Inductance (d) Capacitance. [6]
12. Define transverse electric mode and transverse magnetic mode. A rectangular wave guide has dimensions $a = 3.5\text{cm}$, $b = 2\text{cm}$ and is to be operated below 15 GHz. The medium in the waveguide is air. Determine (a) Cut off frequency (b) Number of $TE_{m,n}$ and $TM_{m,n}$ modes that wave guide can support. [4]
13. Write short notes on: [8]
 - a) Smith chart and it's application
 - b) Antenna types and properties
 - c) Skin effect, loss tangent, propagation constant
 - d) Point form of Ampere's circuital law

[3x4]

Exam.		Regular	
Level	BE	Full Marks	80
Programme	BEL, BEX, BCT	Pass Marks	32
Year / Part	II / I	Time	3 hrs.

Subject: - Electromagnetics (EX 503)

- ✓ Candidates are required to give their answers in their own words as far as practicable.
- ✓ Attempt All questions.
- ✓ The figures in the margin indicate Full Marks.
- ✓ Necessary formulas are attached herewith.
- ✓ Assume suitable data if necessary.

1. Transform vector $\vec{A} = \rho \sin \phi \vec{a}_z$ at point $(1, 45^\circ, 2)$ in cylindrical co-ordinate system to a vector in spherical co-ordinate system. [5]

2. The region $X < 0$ is composed of a uniform dielectric material for which $\epsilon_{r1} = 3.2$, while the region $X > 0$ is characterized by $\epsilon_{r2} = 2$. The electric flux density at region $X < 0$ is $\vec{D}_1 = -30 \vec{a}_x + 50 \vec{a}_y + 70 \vec{a}_z \text{ nC/m}^2$ then find polarization (\vec{P}) and electric field intensity (\vec{E}) in both regions. [3+3] *3 lines*

3. Define an electric dipole. Derive expression for electric field because of electric dipole at a distance that is large compared to the separation between charges in the dipole. [2+6]

4. Define Relaxation Time Constant and derive an expression for the continuity equation. [3+4]

5. Derive the equations for magnetic field intensity for infinite long coaxial transmission line carrying direct current I and return current $-I$ in positive and negative Z-direction respectively. [7]

6. A current carrying square loop with vertices $A(0, -2, 2)$, $B(0, 2, 2)$, $C(0, 2, -2)$, $D(0, -2, -2)$ is carrying a dc current of 20A in the direction along A-B-C-D-A. Find magnetic field intensity \vec{H} at centre of the current carrying loop. [6]

7. Elaborate the significance of a curl of a vector field. [3]

8. Derive the expressions for the electric field \vec{E} and magnetic field \vec{H} for the wave propagation in free space. [8]

9. The phasor component of electric field intensity in free space is given by $\vec{E}_s = (100 < 45^\circ) e^{j50z} \vec{a}_x \text{ v/m}$. Determine frequency of the wave, wave impedance, \vec{H}_s , and magnitude of \vec{E} at $z = 10\text{mm}$, $t = 20\text{ps}$. [2+2+2+2]

10. Write short notes on: (a) Loss tangent (b) Skin depth and (c) Displacement current density. [2+2+2]

11. Explain impedance matching using both quarter wave transformer and single stub methods. [3+3]

12. Explain in brief the modes supported by rectangular waveguides. Consider a rectangular waveguide with $\epsilon_r = 2$, $\mu = \mu_0$ with dimensions $a = 1.07\text{cm}$, $b = 0.43\text{cm}$. Find the cut off frequency for TM_{11} mode and the dominant mode. [4+2+2]

13. Define antenna and list different types of antenna. [2]