

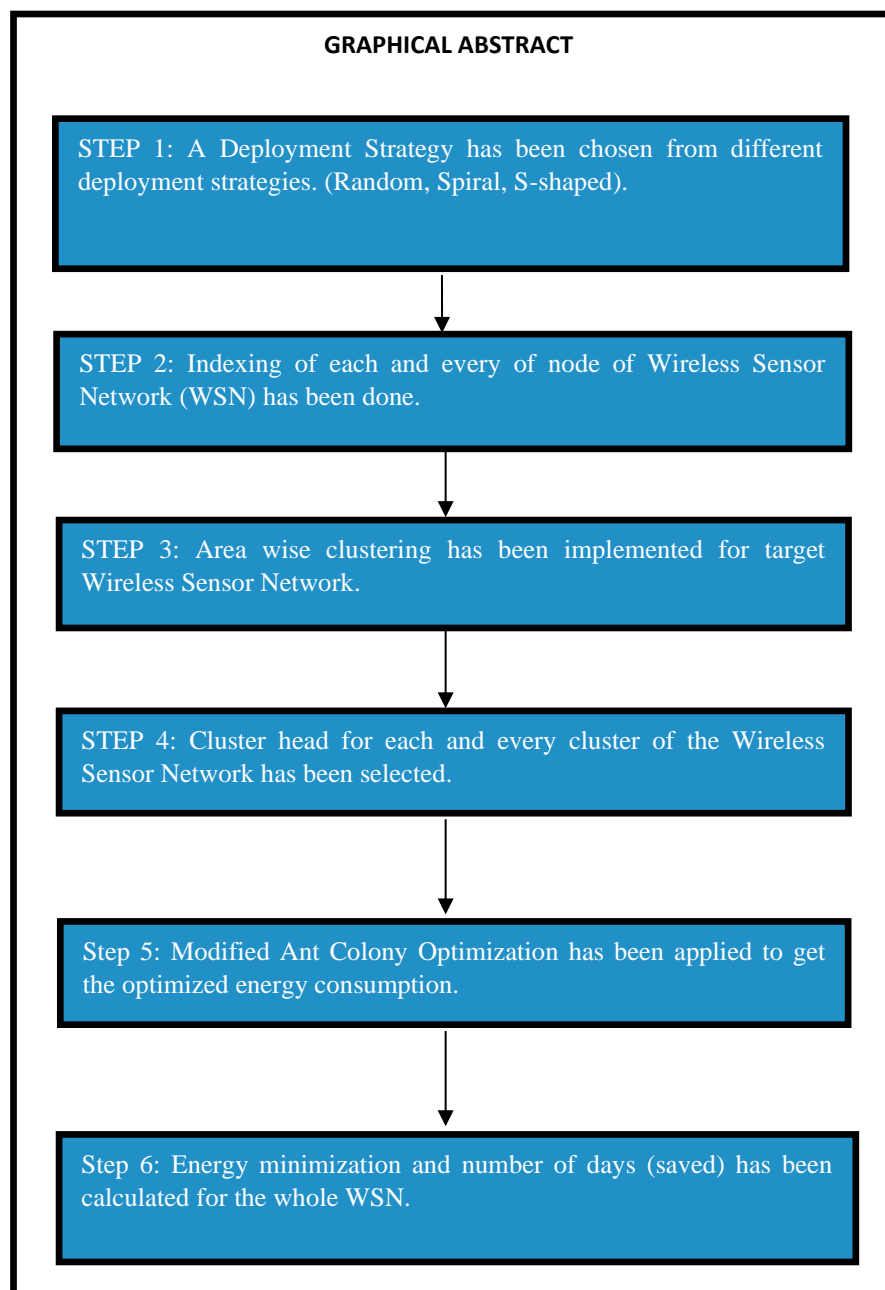
New Title: Construction of efficient Wireless Sensor Networks for Energy Minimization using modified ACO Algorithm.

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1. Abstract

In this paper, we have proposed different deployment strategies and we have applied area-wise clustering along with modified Ant Colony Optimization to minimize the energy consumption.

BACKGROUND: Previously some deployment strategies were used to enhance the lifetime of WSN but in our research, we have applied some novel deployment strategies (random, spiral, and S-pattern) along with a novel clustering process (i.e., area-wise clustering) to get better results than the existing literature as shown in Table 4.

OBJECTIVE: The main objective of the research article is to enhance the lifetime of Wireless Sensor Network with the help of different deployment strategies (random, spiral, and S-pattern), a novel clustering process (i.e., area-wise clustering), and a Meta-heuristic algorithm (modified ACO).

METHOD: We have applied different methods for deployment strategies (random, spiral, and S-pattern), clustering process (i.e., area-wise clustering), and modified versions of ACO to get the desired results.

RESULT:

Random Deployment: 11.15 days to 15.09 days.

Spiral Deployment: 11.25 days to 15.23 days.

S-Pattern Deployment: 11.33 days to 15.33 days.

CONCLUSION: In this research, the lifetime of WSN has been increased to a significant level theoretically. To choose the best result set from all the obtained results set some parameters such as equivalent distribution, number of iterations, maximum energy has been set to a allowable range. In practical life the level may not match with the theoretical result due to physical dependencies like external environmental factors.

Keywords: Wireless Sensor Network (WSN), Deployment Strategy, Clustering Process, Ant Colony Optimization (ACO), Meta-heuristic Methods, Cluster Head (CH).

2. Introduction

Wireless sensor network is employed in various fields like medicine, agriculture, meteorology, etc. WSN eases many tasks in real life especially in area of surveillance. It can be solution of some inspiring problems like “War Field Monitoring”, “Temperature Sensing”, “Pressure Sensing”, etc. Apart from sensing the major job of WSN is to transmit and receive data in the network. Wireless Sensor Network has a good range of applications in modern technology. WSN is a tiny device having

sensing, communicative, processing, and storage units with power back-up usually by a non-rechargeable battery. The WSN nodes are deployed within the target area to collect various sorts of important information and transfer that information to the sink node. Nowadays this sort of network is getting used to facilitate modern army for “environmental monitoring” [1], “Battlefield Monitoring” [2], “Body Area Network” (BAN), “Intelligent Household”, “Smart Home System” etc. The Sink node [3] is the controller communicative node acting as an administrator node in the WSN.

Depending upon the nature of WSN, it is classified into two types and those are static WSN [4] and dynamic WSN [5]. In the case of static WSN, the whole unit is mounted and fixed to a certain fixed point (co-ordinate system is maintained referencing “sink node” as origin). In the case of dynamic WSN, the node is dynamic, though the sink node is generally mounted to a fixed coordinate (generally considered as origin). Now depending upon the need and purpose the node is selected to develop the communication network. In our experiment, static nodes were used where the coordinate of the sink node [6] as well as typical nodes are fixed and permanent (considered as origin).

In the case of a typical WSN design, the sensor nodes are deployed to cover the target area. [7]. The sensor nodes are deployed to sense the required data like weather information or enemy related information in case of battle field of modern war system and transfer it to the sink node may be directly or via another sensor node. Now in the case of our research, the target area has been clustered. A cell structure is defined as the arrangement of cells in a particular network. The cell structure may be triangular or square in structure but not circular. A circular cell structure leaves out a lot of areas. Out of the remaining square was chosen as the triangular structure cannot cover more area as compared to the square cell structure. In this paper, our objective is to minimize the energy consumption of a WSN. The traversal path is being minimized to cover every cell of the particular path as well as the traversal path between the sink node and cells. The movement of the ants motivated us in using a modified Ant Colony Optimization technique though which provides us the shortest path.

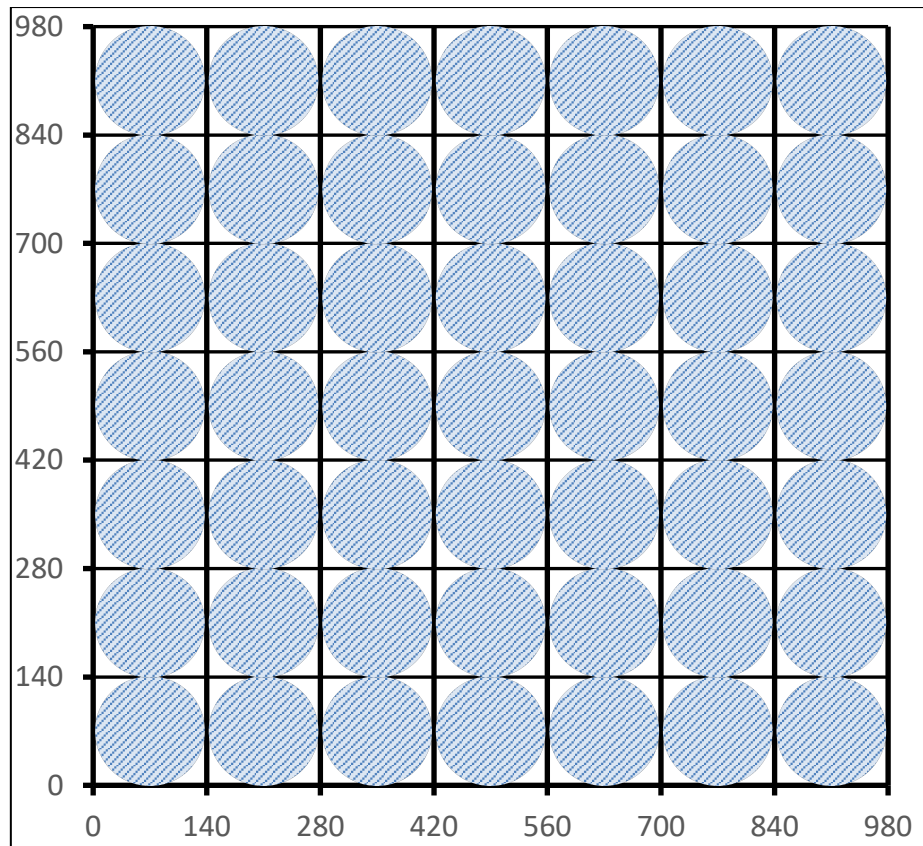


Figure1: Clusterization of the whole area using circular cluster cell structure.

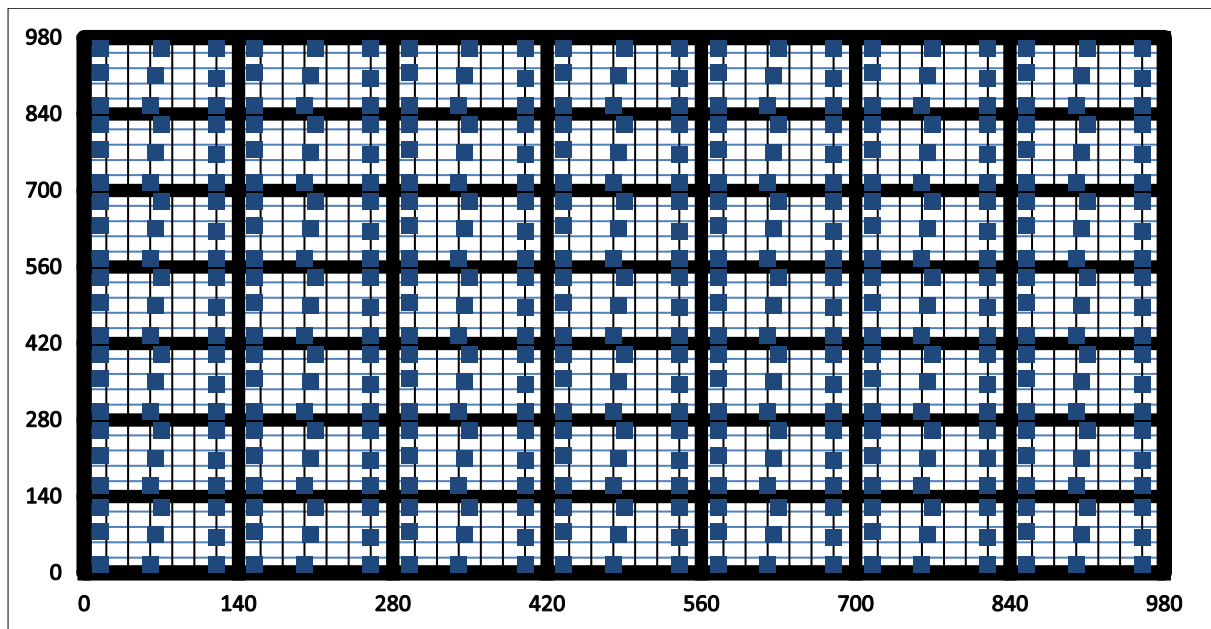


Figure 2: Clusterization of the whole area using square cluster cell structure.

The shaded circle indicates clusterization of the whole area using circular cluster cell structure (Figure 1). We can see that there are gaps between the circular clusters [8] which lead to wastage of space. Due to this reason circular clustering has not been adopted.

The whole area has been divided into multiple square structures (Figure 2). The dots in the figure denote the position of WSN nodes. The nodes have been arranged in such a manner that the maximum area is covered by each node while maintaining the uniformity. This deployment will vary in the case of real-life WSN deployment.

Each cell consists of more than one sensor node (denoted as N). The sink node (denoted as SN) acts as a control point like the local server node [9]. The main aim of the network is to transfer information from one node of a particular cell to another node of an adjacent cell using minimum total power consumption. Each cell is considered as one cluster and each cluster having an active sensor node. The active node of each cluster is called Cluster-Head (CH) [10]. The Cluster-Head is connected with another Cluster-Head of different cell or cluster and thus a network is established. The established network will persist until all Cluster-Head becomes fully exhausted due to a shortage of power backup and after that, the exhausted Cluster-Head will be replaced by another Cluster-Head and so on until all cluster heads of the cluster become exhausted. Here two types of communication will take place i.e., inter-cluster communication (CH-CH communication) [3] or Sink-Cluster communication (SN-CH communication).

The WSN lifetime is dependent on the battery life of the WSN. The lifetime of WSN depends upon so many design factors like the “Deployment Strategy” of WSN nodes and the “Clustering Process”. The deployment strategy has a great effect on the power consumption and

Network coverage of sensor networks. In the clustering process, the area is divided into many clusters for creating the congestion-free transmission. After clustering, some specific nodes are selected to design the network and some of them are designated as “Cluster Head” or “Leader node” for those clusters. After that, a modified version of the ACO algorithm has been implemented for getting the shortest path to design an effective and succinct network for the minimization of energy consumption. The obtained result by applying different deployment strategies has been compared with an identical network of various works of literature. A significant amount of

energy saving has been observed and recorded for the proposed algorithm. The obtained result has been compared with some existing literature and it claimed better results than other implemented results of existing literature.

In section 2 we have done the “Literature Survey” which indicates the related work about WSN by different researchers. After that, the “solution methodology” is described in section 3 where we have discussed how a modified ACO helps to find the shortest path. Then after in sections 5 and 6, we have introduced “numerical data analysis” and “data representation” where we displayed the data in terms of tables and pictures. In section 6 we have explained the “Result Analysis” which has been represented in terms of “number of days” the network can sustain. At last, we have completed a conclusion in section 7 which discussed the scope for future work.

2. LITERATURE SURVEY

Kurt et.al [11] has suggested a new power optimization technique to increase network lifetime. Pughat et.al [12] have proposed the technique of DPM (Dynamic Power Management) which helps to control the duty cycle efficiently which helps in minimize power consumption. Yildiz et.al [13] explained how minimized handshaking helps in reducing the optimized power level which in turn increases the lifetime of the WSN. Akbas et.al [14] discussed how to maintain a balance between data packets size and transmission energy. Small data packet size increases the transmission energy while large data packet size will be difficult to transmit hence can result in loss of data. Hua et.al [15] suggested the concept of a UAV (unmanned aerial vehicle) that helps in establishing a flexible movement path that helps in reliable communication. Lei et.al [16] Expressed the concept of IWSMACO which is a modified version of ACO (Ant colony optimization) based on the information weight factor. Paniri et.al [17] Suggested MLACO (method based on ant colony optimization) which uses supervised and unsupervised learning algorithms. Arjunan et.al [18] Introduce a hybrid algorithm based on fuzzy logic unequal clustering and ACO. Here fuzzy logic is used to select cluster heads. Gajjar et.al [19] Explained how the LEACH cluster algorithm can be used to select cluster heads which reduces the consumption of energy. Boubrima et.al [20] suggested that deployment is an important concept of WSN. Aznoli et.al [21] Proposed deployment can be classified as deterministic and non-deterministic. Tsai et.al [22] Introduced a new meta-heuristic algorithm called SE (Search

Economics) to solve the deployment problem of WSN. Benatia et.al [23] Proposed MODS (Multi-Objective deployment strategy) for solving the placement problem to optimize it. Arya et.al [24] Suggested optimizing the physical distance and signal strength between two nodes. Mohajerani et.al [25] Advise us to use a routing algorithm that uses special parameters to reduce energy consumption by each node. Gajjar et.al [26] explained to use a combination of ACO based MAC and unequal clustering cross-layer protocol for cluster head selection. Nayyar et.al [27] suggested using swarm intelligence based computational techniques to improve the overall WSN.

3. SOLUTION METHODOLOGY

In our paper, a modified version of the ACO algorithm is implemented for the minimization of consumed energy in WSN. This technique has acquired attention due to its precision towards the optimal results. In Ant Colony Optimization, several artificial ants build solutions are considered towards the optimization problem. These exchange data about the quality of these results via a communication media, “pheromone trail, which is reminiscent of the one adopted by real ants” [28].

The original ACO algorithm acknowledged as the Ant System was presented in [28]. A brief discussion on ACO is followed next.

In this algorithm, we have used the ants as the solution variance which solves the optimization problem by applying state transition rule. The solution can be enhanced by “the Local Search Algorithm”. Then the ant adapts “...the amount of pheromone on the visited edges by applying a local pheromone updating rule” [28]. Once all ants have finished their operations, “the amount of pheromone is modified by applying a global updating rule” [28]. ACO activity may be realized with the following two equations Equation 1 and Equation 2.

$$\tau_{ij} = \begin{cases} (1 - \rho) \cdot \tau_{ij} + \rho \cdot \Delta\tau_{ij}, & \text{if } (i, j) \in \text{best solution} \\ \tau_{ij} & \text{otherwise} \end{cases} \quad (1)$$

The local pheromone updating rule is shown in Equation 2.

$$\tau_{ij} = \{\tau_{ij} \cdot (1 - \varphi) + \varphi \cdot \tau_0 \quad (2)$$

Contribution: Modification in ACO algorithm: At first the ANT solution is updated using local update rule. Then the updated ANT solution is modified using global update rule and ultimately the ANT

solution is compared with a previous feasible solution and has taken the following strategies:

- If both (before modification by global update rule and after modification by global update rule) solution is feasible then choose the ANT solution for which the nearest value of global optimum is achieved.
- If anyone solution is in-feasible then discard it and obtain the feasible ANT solution.
- If both (before modification by global update rule and after modification by global update rule) solution is in-feasible then discard the ANT solution and find the next ANT solution.
- In this paper, a modified meta-heuristic algorithm is used (i.e., modified ACO algorithm) that has been used, for selecting the cluster head of the efficient WSN to get the efficient network route.

Pseudo-code for modified ACO

Step 1: Initialize the parameters of the ACO algorithm, including the number of ants to be deployed, the maximum number of iterations, the tune-able parameters, and the initial level of pheromone.

Step 2: Randomly select a node within any cluster and select the other node from another cluster until all the clusters are covered and follow the ACO rule (ACO update rule).

Step 3: If all paths have been traversed by each ant, then continue; otherwise go to step 2.

Step 4: Evaluate the path using the update rule to achieve accuracy depending upon verification.

Step 5: After evaporation of the pheromone, find the ant with the best path. Only permit those ants to deposit pheromone on its traversed paths. If the maximum number of iteration max has not reached go back to step 2; otherwise, go to the next step.

Step 6: Search for the globally best path which produces the highest accuracy among all local best solutions.

Step 7: End

In this paper, the entire process of network formation has been done through the following steps:

3.1. Indexing for Sensor Nodes: The sensor nodes to be deployed must be indexed virtually ~~just~~ to denote or keep track of each sensor nodes before and after the deployment. This indexing process will also ~~help~~ to ~~construct~~ the network. The indexing has been proposed by the help of row and column number of the cell (as depicted in figure 2.). It also helps us to ~~get~~ to ~~know~~ the row and column number of the matrix of the target area. The indexing is a sequential number.

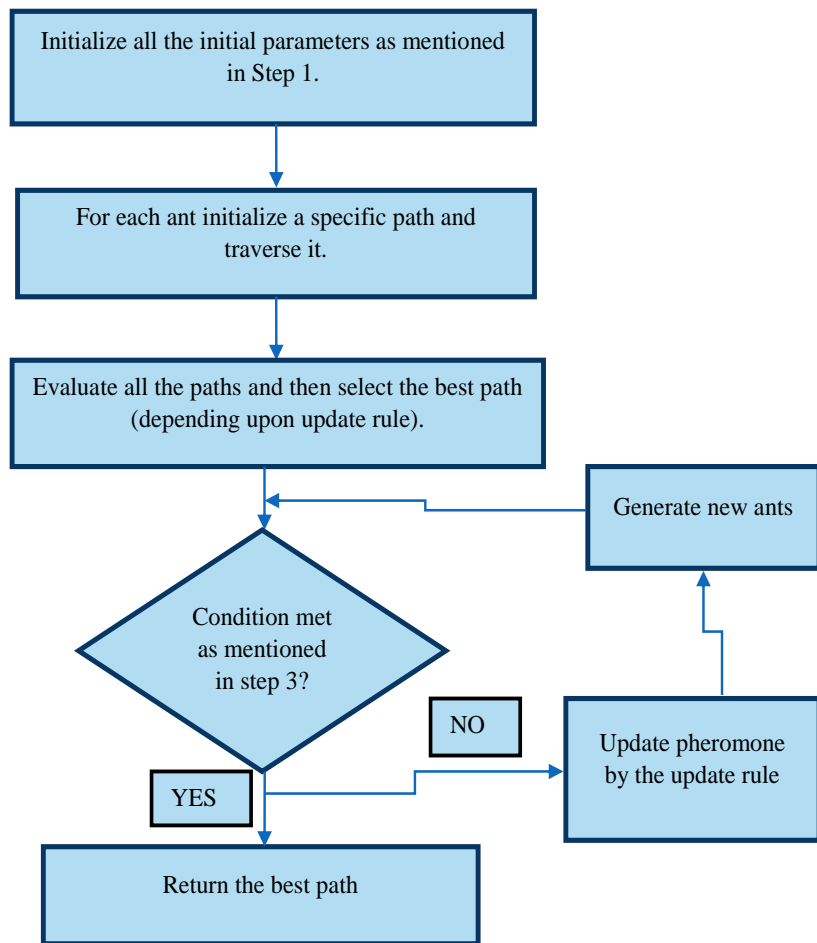


Figure 3: Flowchart of the modified ACO algorithm

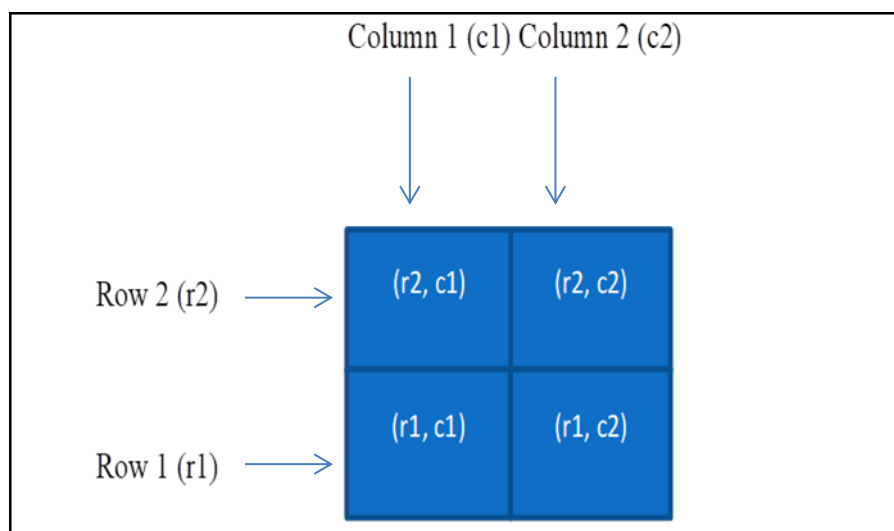


Figure 4: Structure of cluster cell and their representation

3.1.1 Indexing before Deployment: This is the indexing that is given to the sensor node before deployment. It will help us ~~just~~ to keep track of the total number of sensor nodes to be deployed and to maintain the sequence of sensor nodes. (Figure 6, 7, 8, 10, 11, 12, 14, 15, 16).

3.1.2. Indexing after Deployment: This type of indexing is much more important because this indexing is assigned to the sensor nodes after deployment. By this indexing, the sensor node will be denoted until the sensor node becomes fully exhausted. (Figure 9, 13, 17)

3.2. Clustering: Here clustering means dividing target area into some uniform or equal-size sectors. The aim is to construct an efficient network. The structure of cluster cells has been chosen as a square. It can be proved [29] that using square cluster-cell the target area can be covered properly. Here the term “efficient network” refers to the efficient and uniform coverage of the target area with no communication gap between the neighboring clusters.

3.3 Different strategies for the deployment of WSN nodes:

3.3.1. Random deployment of sensor nodes: Here we consider the deployment to be done from a certain distance. In the case of random deployment, it is very difficult to predict the position of sensor nodes. A fixed amount of nodes are deployed for a fixed amount of time. For example, suppose we have to deploy x amount of sensor nodes in y amount of time. Therefore we don't have any fixed strategy to cover the target area.

3.3.2. S pattern deployment: In this type of deployment deployment-strategy follow the S-pattern deployment of sensor nodes. The deployment time is considered a fixed period. The time interval between two deployments is assumed as fixed time and the path is followed as a fixed path.

Here the starting time and ending time of deployment are fixed and the deployment is done in between this period (see figure no 5 to 7).

3.3.3. Spiral deployment: In this type of deployment we follow the Spiral-pattern at the time of deployment of sensor nodes, other criteria are the same as previous deployment.

3.4. Selection of a sensor node as cluster head: The selection process has been done with the help

of a meta-heuristic algorithm i.e., ACO algorithm. The selection of a sensor node as a cluster head (CH) is an important job towards the development of an efficient network configuration because with the help of the cluster head only the internal network is formed.

Here in this paper, the selection of the cluster head has been done by calculating the uniform distance between different nodes in a cluster maintaining the following conditions:

- One cluster head has been selected from each cluster and the process has been done by the help of a meta-heuristic algorithm i.e., modified ACO algorithm.
- After the full exhaustion of energy of one cluster head, another sensor node is considered as an active cluster head and the previous cluster head becomes inactive.
- The intermediate network will sustain for some time and when the cluster head of any cluster cell will be exhausted it will form another network thus it will give stability to the whole network to perform for a longer period and ultimately when all the sensor-nodes of a particular cluster will be exhausted the whole network will go down.

3.5. WSN network configuration through modified ACO algorithm:

In the ACO Algorithm, we choose the minimized path for transmitting and receiving information among the nodes.

The linear problem as described below:

The energy consumption during successful data transmission between cluster head (CH) to cluster head (CH) and cluster head (CH) to sink node (SN) has been calculated and minimized using the below-maintained equations:

The energy consumption during successful data transmission between cluster head (CH) to cluster head (CH) and cluster head (CH) to sink node (SN) has been calculated and minimized using the below-maintained equations [31]:

$$k(R, d) = \text{Minimize} \left(E_{\text{communication}}^{\text{Total}}(R, d) \right) \quad (1)$$

Subject to,

$d \leq d_0$, for free-space propagation model and $d > d_0$ for two-ray ground propagation model.

Where d_0 is the threshold transmission distance.

Where,

$$E_{\text{communication}}^{\text{Total}}(R, d) = E_{\text{receiving}}^{\text{Total}}(R) + E_{\text{transmission}}^{\text{Total}}(R, d) \quad (2)$$

$$E_{\text{receiving}}^{\text{Total}}(R) = E_{\text{receiving}}^{\text{SN-CH}}(R) + E_{\text{receiving}}^{\text{CH-CH}}(R) \quad (3)$$

$$E_{\text{transmission}}^{\text{Total}}(R, d) = E_{\text{transmission}}^{\text{SN-CH}}(R, d) + E_{\text{transmission}}^{\text{CH-CH}} \quad (4)$$

$$E_{\text{transmission}}^{\text{SN-CH}}(R, d) = E_{\text{charge}}^{\text{SN-CH}}(R) + E_{\text{resonator}}^{\text{SN-CH}}(R, d) \quad (5)$$

$$E_{\text{transmission}}^{\text{CH-CH}}(R, d) = E_{\text{charge}}^{\text{CH-CH}}(R) + E_{\text{resonator}}^{\text{CH-CH}}(R, d) \quad (6)$$

$$E_{\text{receiving}}^{\text{SN-CH}}(R) = E_{\text{charge}}^{\text{SN-CH}}(R) * (R) \quad (7)$$

$$E_{\text{receiving}}^{\text{CH-CH}}(k) = E_{\text{charge}}^{\text{CH-CH}}(R) * (R) \quad (8)$$

$$E_{\text{resonator}}^{\text{SN-CH}}(R, d) = E_{\text{ts}}^{\text{SN-CH}} * d^2 \quad (9)$$

$$E_{\text{resonator}}^{\text{CH-CH}}(R, d) = E_{\text{ts}}^{\text{CH-CH}} * d^2 \quad (10)$$

$E_{\text{resonator}}^{\text{CH-CH}}$ = energy required for the transmitting data packets between two adjacent cluster head for the amplifier to maintain an acceptable signal-to-noise ratio to transfer data messages reliably.

$E_{\text{resonator}}^{\text{SN-CH}}$ = energy required for the transmitting data packets between sink node and cluster head for the amplifier to maintain an acceptable signal-to-noise ratio to transfer data messages reliably.

$E_{\text{charge}}^{\text{CH-CH}}$ = Electronic energy degenerated during the transmission between two adjacent cluster heads.

$E_{\text{charge}}^{\text{SN-CH}}$ = Electronic energy degenerated during the transmission between the sink node and adjacent cluster head.

$E_{\text{transmission}}$ = amount of energy used by each node at the time of transmitting data packets.

$E_{\text{receiving}}$ = energy used for receiving data packets.

Measurement of distance between two cluster heads is done using the following formula

$$d_{xy} = \sqrt{(x_1 - x_2)^2 + (y_1 - y_2)^2}$$

E_{ts} = Amount of energy consumption by a single node for free-space propagation

Where (x_1, y_1) and (x_2, y_2) are coordinates of reference nodes and d_{xy} is the distance measured between two adjacent cluster heads and the notation d_{xy} and d are the same.

Now in terms of minimizing the total energy transmission and using the proposed ACO algorithm, the optimized path has been established as shown in Figure 5. The data used from Table 1. After getting an efficient path through the meta-heuristic algorithm i.e., ACO total energy saved was determined in hours. In this paper, the tolerance percentage has been fixed to $\pm 15\%$ which is the most acceptable tolerance in the case of Wireless Sensor Network. The designed network is an efficient network concerning the minimization of energy consumption.

In this section, the energy minimization problem was solved using ACO. The proposed method was tested using the data of Table 1 using the ACO algorithm and obtained the optimized path for the network for minimizing energy consumption.

The following parameter values are used in the experiment for simulating the system. [32].

4. NUMERICAL DATA ANALYSIS

Table 1: Parameters for simulation.

| Parameters | Values | Parameters | Values |
|---------------------------------|--|-----------------------------------|-----------|
| Deployment Area | 980 x 980 m ² | Data packet size (R) | 4096 bits |
| Total number of Clusters | 49 | Max no. of nodes (in the network) | 490 |
| The initial energy of each node | 1J | E_{charge} | 50nJ/bit |
| E_{ts} | 10pJ • bit ⁻¹ • m ⁻² | Maximum Number of Rounds | 6000 |

In Table 1, different units (Joule, Nano Joule, and Pico-Joule) were used Therefore to maintain uniformity, all calculations have been done in Pico-Joule in Table 2, Table 3 and Table 4. In this paper the best path is plotted for shortest distances (see Figure 9, 13, 17) obtained from the ACO algorithm for different deployments by solving the equations 1 to 10 based on the data supplied in Table 1. As the energy consumption is directly proportional to the distance between nodes that's why we have calculated the maximum coverage area. Table 1 shows the communication between the sink node and the cluster head, whereas Table 2, 3 and 4 shows the communication between adjustment cluster heads. In the below diagram we are going to show the 4 phases of forming a network and finding the shortest path. The first process is the deployment were three strategies namely random, spiral, and s-pattern have been used. (See Figures 6, 10 and 14 respectively). The next step is the division of the nodes into clusters or clustering (See Figure 7, 11, 15). The third process consists of electing the Cluster Heads. (See Figure 8, 12, 16) and the fourth process includes connecting all the cluster heads among themselves using the ACO algorithm (See Figure 9, 13, 17).

5. NUMERICAL DATA REPRESENTATION

Now the numerical data is being represented with the help of tabular format depicted below. With the help of table 2, Energy Saving (E_s) calculations applying random deployment and area-wise clustering processes have been done. With the help of table 3, Energy Saving (E_s) calculations have been done applying spiral deployment and area-wise Clustering Process. With the help of table 4, Energy Saving (E_s) calculations applying s-pattern deployment and area-wise Clustering Process have been done.

We have used certain notations to calculate the energies. A brief description of them is given below. (This notation can be found in Tables 2,3 and 4)

- 1) E_{tx0} : This indicates the actual energy required to transform the data packets from one node to another (equation 5 and 6)
- 2) $E_{tx(min)}$: This is E_{tx0} but after applying minimum possible tolerance.
- 3) $E_{tx(max)}$: This is also E_{tx0} but after applying maximum possible tolerance.
- 4) $total0$: This the total energy required during the whole communication (transmitting and receiving) among the nodes.
- 5) $totalxy(min)$: This is the total energy required but after applying minimum possible tolerance.
- 6) $totalxy(max)$: This is the total energy required but after applying maximum possible tolerance.
- 7) $maxEng$: This is the difference between $totalxy(max)$ and $totalxy(min)$.
- 8) $minEng$: This is the difference between $total0$ and $totalxy(min)$.
- 9) $avgEng$: This is the difference between $totalxy(max)$ and $total0$.

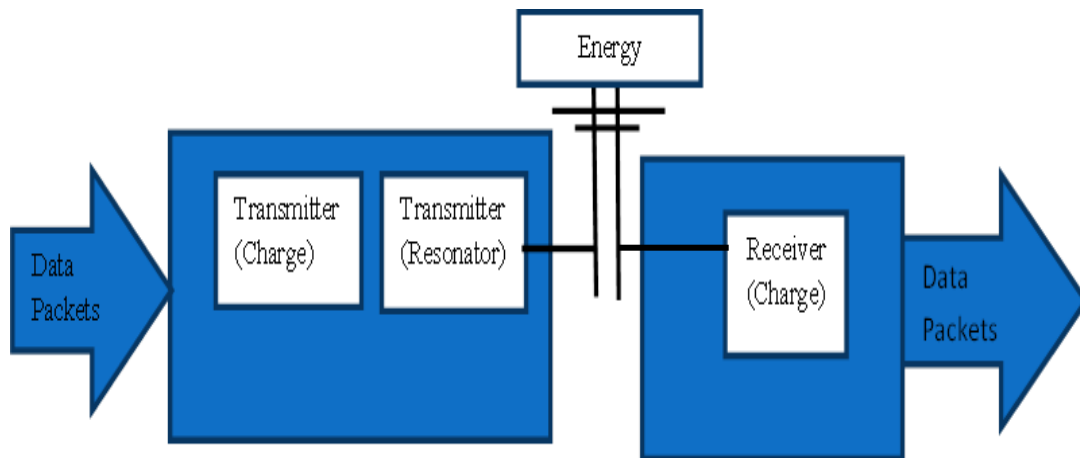


Figure 5: Block Diagram of WSN nodes with transmitter and receiver

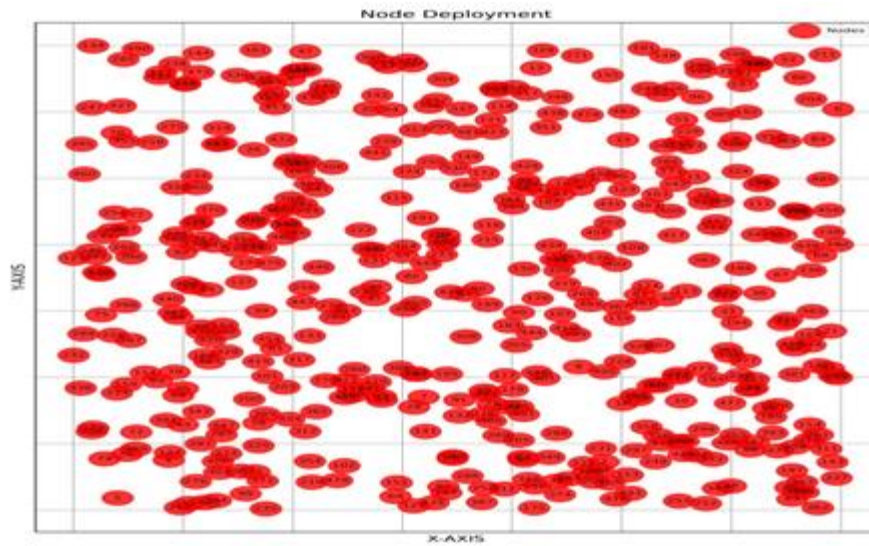


Figure 6: Random deployment: The above figure shows the random deployment of the nodes in the area.

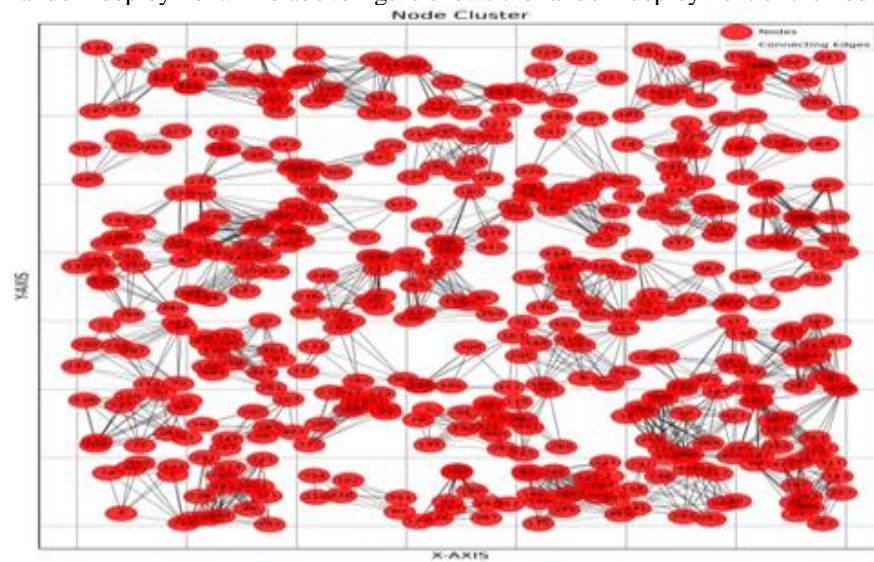


Figure 7: Random clustering-This figure shows how the nodes are grouped into clusters.

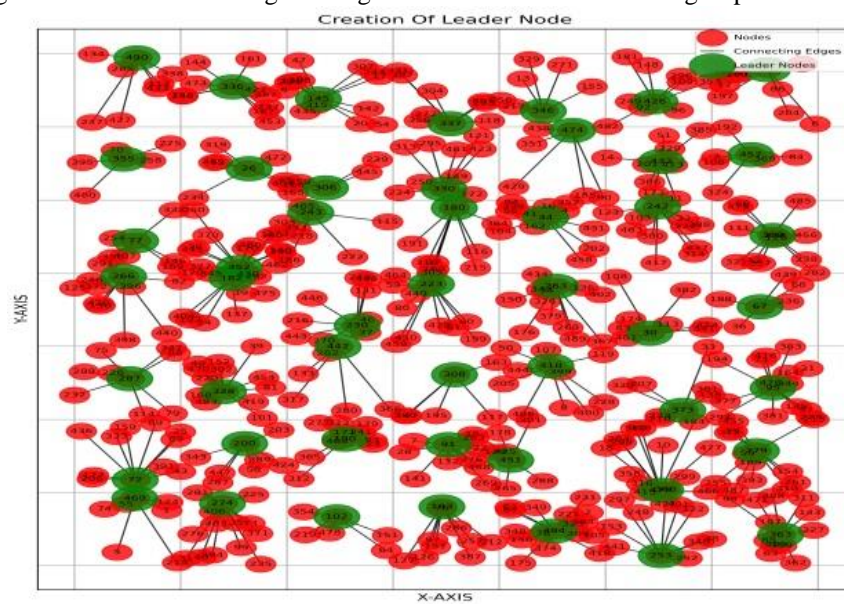


Figure 8: Leader Nodes of the clusters-The above figure shows the leader nodes of their respective clusters denoted by the green colour.

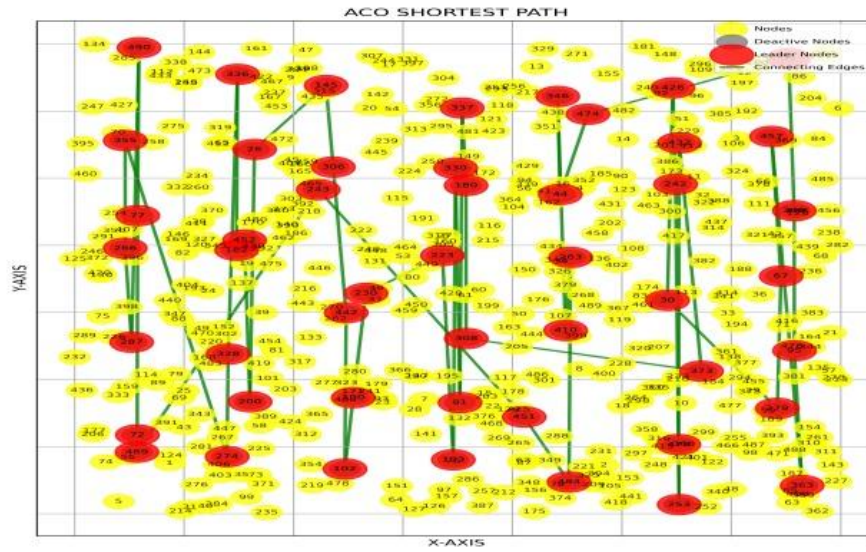


Figure 9: Shortest path after applying ACO Algorithm denoted by green lines.

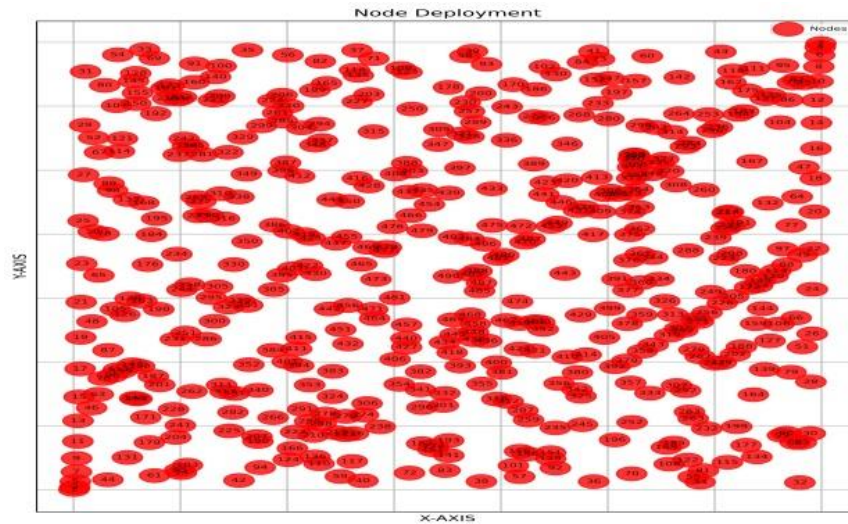


Figure 10: Spiral deployment-The above figure shows the deployment of nodes spirally starting from the upper left side and ending at the centre.

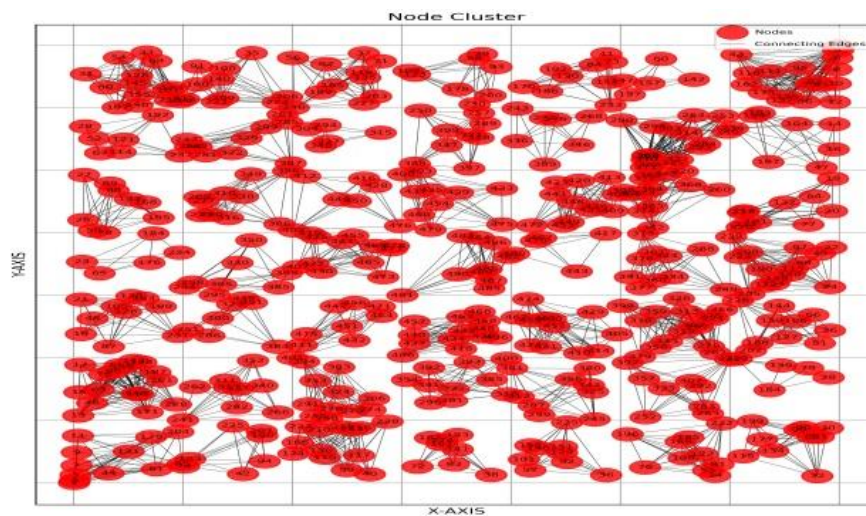


Figure 11: Spiral Clustering-This figure shows the clusters formed within the nodes and are connected through black lines.

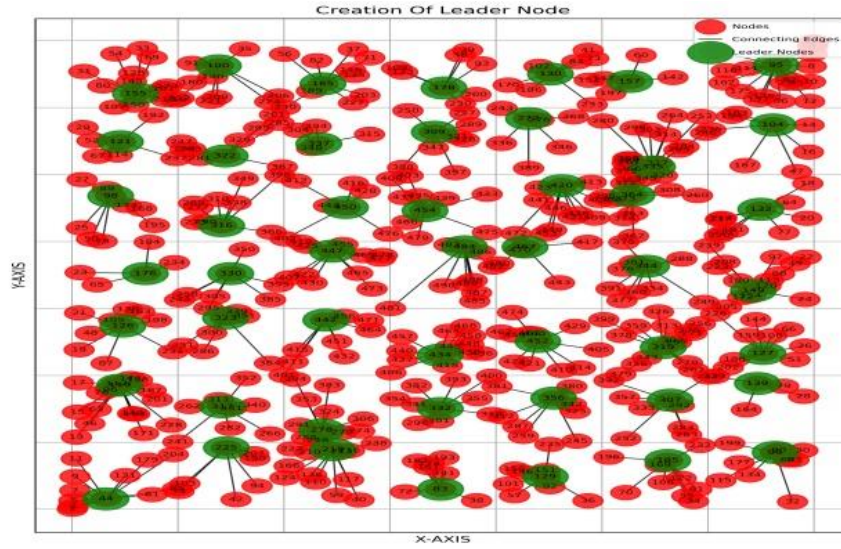


Figure 12: Leader nodes or head nodes of the clusters. The green nodes indicate the leader nodes of the respective clusters.

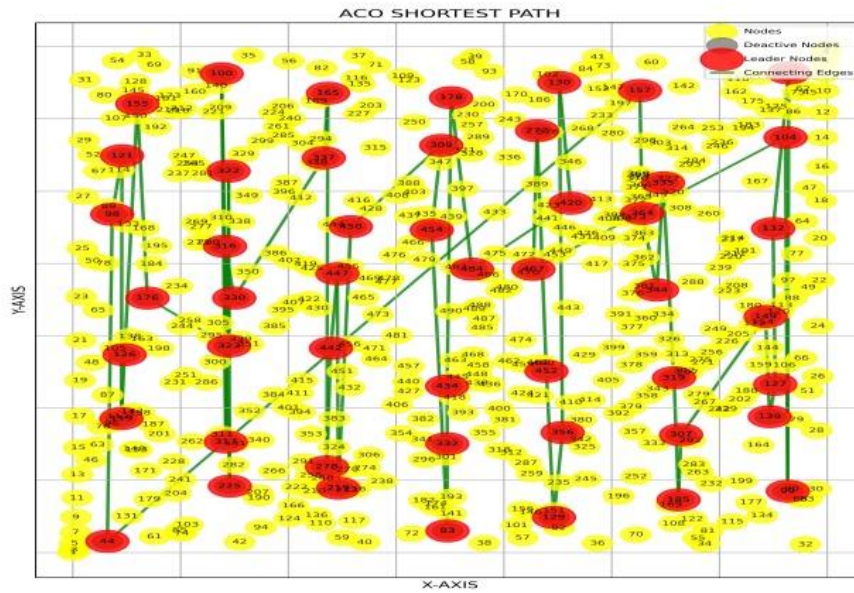


Figure 13: Shortest path obtained after applying ACO denoted by green lines.

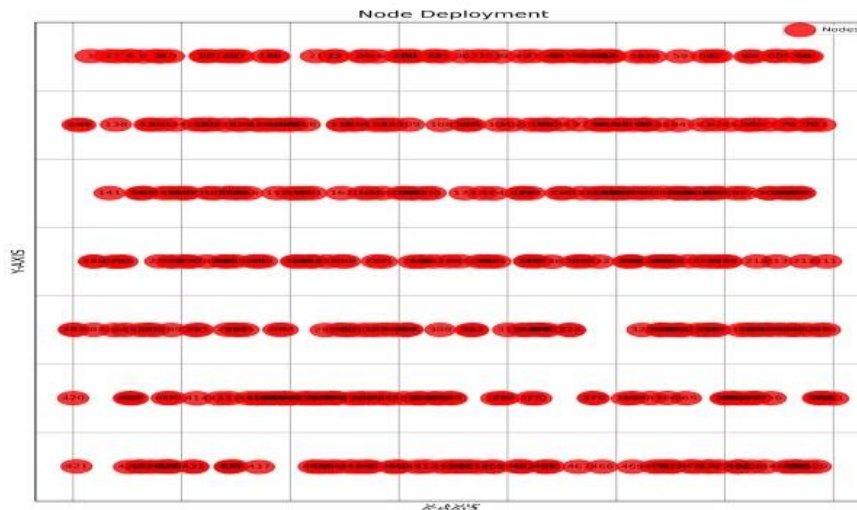


Figure 14: S-pattern Deployment-This above figure shows the deployment of the nodes in a s-pattern fashion.

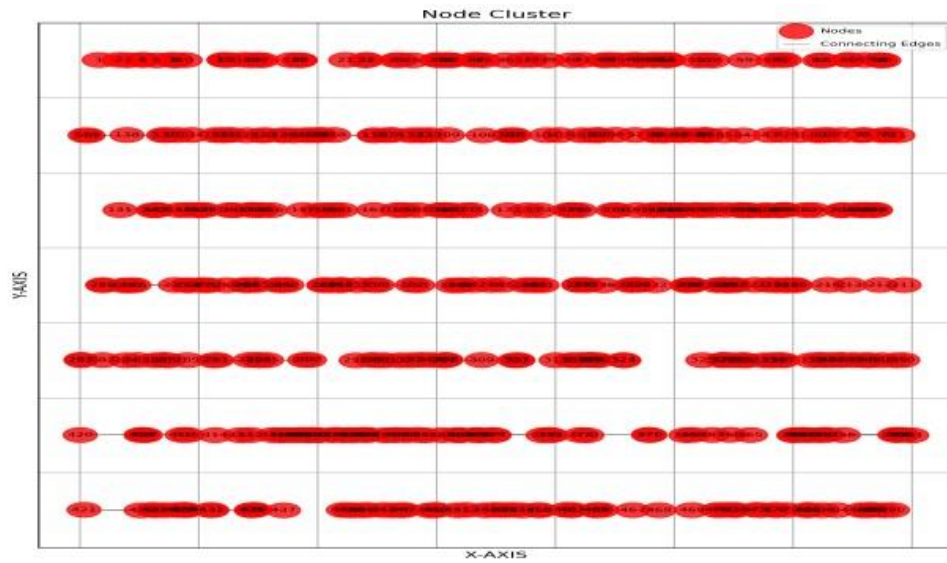


Figure 15: S-pattern Clustering-This figure shows the clustering of the nodes in a s-pattern manner.

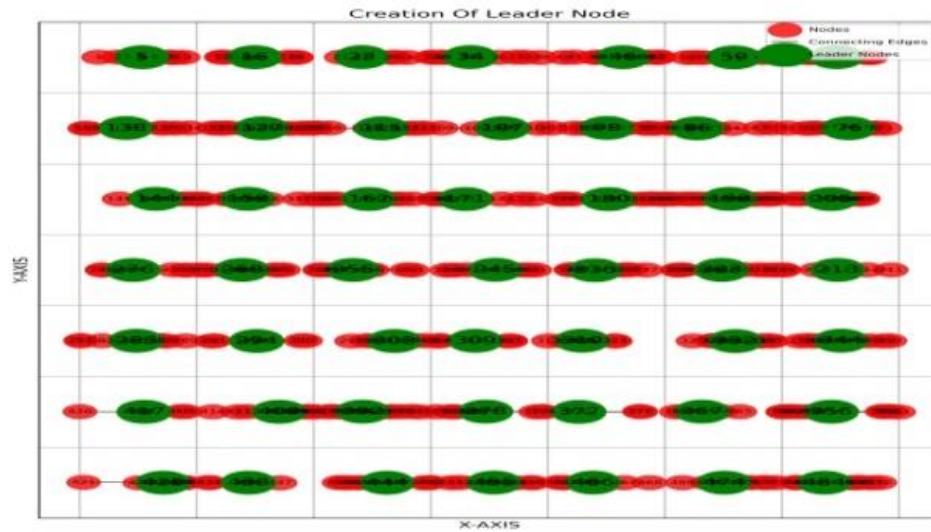


Figure 16: Leader nodes or head nodes of the clusters- The green nodes indicate the leader nodes of the respective cluster

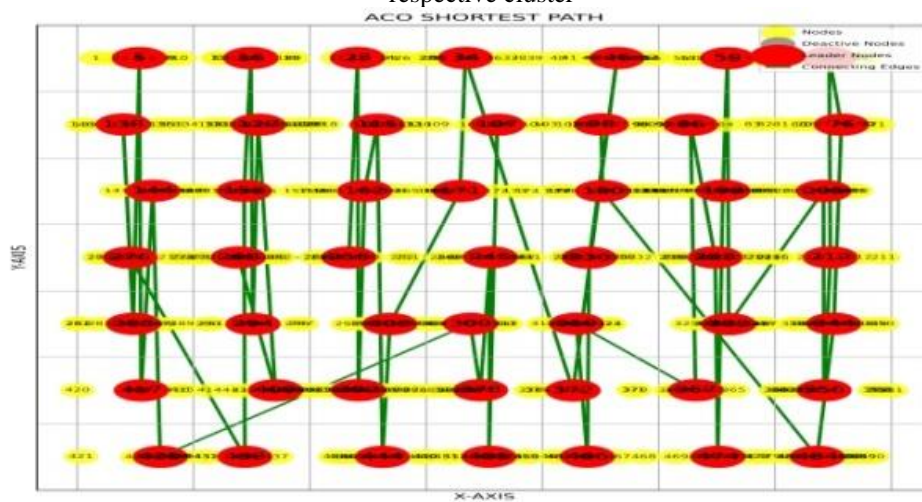


Figure 17: Shortest path after applying the ACO algorithm denoted by green line.

Table 2: Energy saving (Es) calculations applying S-pattern Deployment Strategy and Area Wise Clustering Process

| INO-CL NO. | dmin(d=42mm or 4.2cm) | | | | dmax(d=42mm or 4.2cm) | | | | dis(zero) | dxy(min) | dxy(max) | E_tx0 | E_tx(min) | E_tx(max) | max Eng | min Eng | AvgEng | total0 | totalxy(min) | totalxy(max) |
|------------|-----------------------|----------|----------|----------|-----------------------|----------|----------|----------|-----------|----------|----------|----------|-----------|-----------|----------|----------|----------|----------|--------------|--------------|
| | (x1-d/2) | (y1-d/2) | (x2-d/2) | (y2-d/2) | (x1+d/2) | (y1+d/2) | (x2+d/2) | (y2+d/2) | | | | | | | | | | | | |
| 1-1 | -2.1 | -2.1 | 65.28 | 68.03 | 2.1 | 2.1 | 69.48 | 72.23 | 97.2537 | 91.31526 | 103.1923 | 50418.28 | 49298.48 | 51608.65 | 2310.168 | 1119.804 | 1190.364 | 50418.28 | 49298.48 | 51608.65 |
| 1-2 | 65.28 | 68.03 | 68.28 | 208.3 | 69.48 | 72.23 | 72.48 | 212.5 | 140.3021 | 136.0753 | 144.6493 | 60644.67 | 59476.48 | 61883.42 | 2406.936 | 1168.188 | 1238.748 | 60644.67 | 59476.48 | 61883.42 |
| 1-3 | 68.28 | 208.3 | 73.42 | 348.04 | 72.48 | 212.5 | 77.62 | 352.24 | 139.8345 | 135.5433 | 144.2427 | 60513.69 | 59331.98 | 61765.96 | 2433.984 | 1181.712 | 1252.272 | 60513.69 | 59331.98 | 61765.96 |
| 1-4 | 73.42 | 348.04 | 96.92 | 488.73 | 77.62 | 352.24 | 101.12 | 492.93 | 142.6391 | 137.8478 | 147.5141 | 61305.93 | 59962.01 | 62720.4 | 2758.392 | 1343.916 | 1414.476 | 61305.93 | 59962.01 | 62720.4 |
| 1-5 | 96.92 | 488.73 | 89.81 | 628.26 | 101.12 | 492.93 | 94.01 | 632.46 | 139.711 | 135.8018 | 143.7595 | 60479.17 | 59402.13 | 61626.78 | 2224.656 | 1077.048 | 1147.608 | 60479.17 | 59402.13 | 61626.78 |
| 1-6 | 89.81 | 628.26 | 83.93 | 768.45 | 94.01 | 632.46 | 88.13 | 772.65 | 140.3133 | 136.3631 | 144.3998 | 60647.81 | 59554.89 | 61811.29 | 2256.408 | 1092.924 | 1163.484 | 60647.81 | 59554.89 | 61811.29 |
| 1-7 | 83.93 | 768.45 | 34.85 | 908.48 | 88.13 | 772.65 | 39.05 | 912.68 | 148.3821 | 145.906 | 151.0513 | 62977.25 | 62248.55 | 63776.51 | 1527.96 | 728.7 | 799.26 | 62977.25 | 62248.55 | 63776.51 |
| 1-8 | 34.85 | 908.48 | 215.44 | 68.65 | 39.05 | 912.68 | 219.64 | 72.85 | 859.0269 | 862.2645 | 855.8182 | 778887.2 | 784460.1 | 773384.8 | 11075.23 | 5572.896 | 5502.336 | 778887.2 | 784460.1 | 773384.8 |
| 1-9 | 215.44 | 68.65 | 188.95 | 208.48 | 219.64 | 72.85 | 193.15 | 212.68 | 142.3171 | 139.0589 | 145.7446 | 61214.15 | 60297.37 | 62201.49 | 1904.112 | 916.776 | 987.336 | 61214.15 | 60297.37 | 62201.49 |
| 1-10 | 188.95 | 208.48 | 190.93 | 348.65 | 193.15 | 212.68 | 195.13 | 352.85 | 140.184 | 135.9881 | 144.5022 | 60611.55 | 59452.77 | 61840.89 | 2388.12 | 1158.78 | 1229.34 | 60611.55 | 59452.77 | 61840.89 |
| 1-11 | 190.93 | 348.65 | 210.24 | 487.91 | 195.13 | 352.85 | 214.44 | 492.11 | 140.5924 | 135.9026 | 145.3736 | 60726.22 | 59429.52 | 62093.49 | 2663.976 | 1296.708 | 1367.268 | 60726.22 | 59429.52 | 62093.49 |
| 1-12 | 210.24 | 487.91 | 212.45 | 628.13 | 214.44 | 492.11 | 216.65 | 632.33 | 140.2374 | 136.0346 | 144.5622 | 60626.53 | 59465.4 | 61858.22 | 2392.824 | 1161.132 | 1231.692 | 60626.53 | 59465.4 | 61858.22 |
| 1-13 | 212.45 | 628.13 | 189.03 | 768.52 | 216.65 | 632.33 | 193.23 | 772.72 | 142.3301 | 138.9625 | 145.8618 | 61217.85 | 60270.58 | 62235.68 | 1965.096 | 947.268 | 1017.828 | 61217.85 | 60270.58 | 62235.68 |
| 1-14 | 189.03 | 768.52 | 175.03 | 908.36 | 193.23 | 772.72 | 179.23 | 912.56 | 140.5391 | 136.8556 | 144.373 | 60711.23 | 59689.45 | 61803.56 | 2114.112 | 1021.776 | 1092.336 | 60711.23 | 59689.45 | 61803.56 |
| 1-15 | 175.03 | 908.36 | 342.97 | 68.55 | 179.23 | 912.56 | 347.17 | 72.75 | 856.4372 | 859.7463 | 853.1566 | 774444.7 | 780123.7 | 768836.3 | 11287.42 | 5678.988 | 5608.428 | 774444.7 | 780123.7 | 768836.3 |
| 1-16 | 342.97 | 68.55 | 322.61 | 208.3 | 347.17 | 72.75 | 326.81 | 212.5 | 141.2253 | 137.757 | 144.8542 | 60904.59 | 59937 | 61942.75 | 2005.752 | 967.596 | 1038.156 | 60904.59 | 59937 | 61942.75 |
| 1-17 | 322.61 | 208.3 | 366.29 | 348.78 | 326.81 | 212.5 | 370.49 | 352.98 | 147.1141 | 141.8834 | 152.3968 | 62602.57 | 61090.91 | 64184.8 | 3093.888 | 1511.664 | 1582.224 | 62602.57 | 61090.91 | 64184.8 |
| 1-18 | 366.29 | 348.78 | 350.87 | 488.58 | 370.49 | 352.98 | 355.07 | 492.78 | 140.6478 | 137.0121 | 144.4365 | 60741.82 | 59732.3 | 61821.89 | 2089.584 | 1009.512 | 1080.072 | 60741.82 | 59732.3 | 61821.89 |
| 1-19 | 350.87 | 488.58 | 326.85 | 628.51 | 355.07 | 492.78 | 331.05 | 632.71 | 141.9766 | 138.6326 | 145.4864 | 61117.37 | 60179 | 62126.29 | 1947.288 | 938.364 | 1008.924 | 61117.37 | 60179 | 62126.29 |
| 1-20 | 326.85 | 628.51 | 324.74 | 768.58 | 331.05 | 632.71 | 328.94 | 772.78 | 140.0859 | 136.0164 | 144.2851 | 60584.06 | 59460.47 | 61778.2 | 2317.728 | 1123.584 | 1194.144 | 60584.06 | 59460.47 | 61778.2 |
| 1-21 | 324.74 | 768.58 | 297.27 | 907.99 | 328.94 | 772.78 | 301.47 | 912.19 | 142.0906 | 138.8695 | 145.4831 | 61149.75 | 60244.73 | 62125.33 | 1880.592 | 905.016 | 975.576 | 61149.75 | 60244.73 | 62125.33 |
| 1-22 | 297.27 | 907.99 | 499.05 | 68.71 | 301.47 | 912.19 | 503.25 | 72.91 | 863.1953 | 866.3119 | 860.1083 | 786066.1 | 791456.4 | 780746.4 | 10710 | 5390.28 | 5319.72 | 786066.1 | 791456.4 | 780746.4 |
| 1-23 | 499.05 | 68.71 | 486.83 | 208.24 | 503.25 | 72.91 | 491.03 | 212.44 | 140.0641 | 136.3225 | 143.9536 | 60577.95 | 59543.83 | 61682.63 | 2138.808 | 1034.124 | 1104.684 | 60577.95 | 59543.83 | 61682.63 |
| 1-24 | 486.83 | 208.24 | 483.81 | 348.56 | 491.03 | 212.44 | 488.01 | 352.76 | 140.3525 | 136.3113 | 144.5248 | 60658.82 | 59540.78 | 61847.42 | 2306.64 | 1118.04 | 1188.6 | 60658.82 | 59540.78 | 61847.42 |
| 1-25 | 483.81 | 348.56 | 511.25 | 488.31 | 488.01 | 352.76 | 515.45 | 492.51 | 142.4185 | 137.5278 | 147.3862 | 61243.02 | 59873.9 | 62682.69 | 2808.792 | 1369.116 | 1439.676 | 61243.02 | 59873.9 | 62682.69 |
| 1-26 | 511.25 | 488.31 | 460.9 | 628.36 | 515.45 | 492.51 | 465.1 | 632.56 | 148.8258 | 146.393 | 151.4526 | 63109.13 | 62390.93 | 63897.89 | 1506.96 | 718.2 | 788.76 | 63109.13 | 62390.93 | 63897.89 |
| 1-27 | 460.9 | 628.36 | 490.01 | 768.47 | 465.1 | 632.56 | 494.21 | 772.67 | 143.1021 | 138.1739 | 148.1045 | 61438.2 | 60052.04 | 62894.93 | 2842.896 | 1386.168 | 1456.728 | 61438.2 | 60052.04 | 62894.93 |
| 1-28 | 490.01 | 768.47 | 483.42 | 908.79 | 494.21 | 772.67 | 487.62 | 912.99 | 140.4747 | 136.547 | 144.5398 | 60693.13 | 59605.08 | 61851.74 | 2246.664 | 1088.052 | 1158.612 | 60693.13 | 59605.08 | 61851.74 |
| 1-29 | 483.42 | 908.79 | 636.31 | 67.96 | 487.62 | 912.99 | 640.51 | 72.16 | 854.6171 | 858.0119 | 851.2503 | 771330.4 | 777144.4 | 765587 | 11557.39 | 5813.976 | 5743.416 | 771330.4 | 777144.4 | 765587 |
| 1-30 | 636.31 | 67.96 | 648.55 | 208.78 | 640.51 | 72.16 | 652.75 | 212.98 | 141.3509 | 136.8564 | 145.9489 | 60940.09 | 59689.67 | 62261.07 | 2571.408 | 1250.424 | 1320.984 | 60940.09 | 59689.67 | 62261.07 |
| 1-31 | 648.55 | 208.78 | 639.6 | 348.39 | 652.75 | 212.98 | 643.8 | 352.59 | 139.8966 | 136.047 | 143.8884 | 60531.05 | 59468.79 | 61663.88 | 2195.088 | 1062.264 | 1132.824 | 60531.05 | 59468.79 | 61663.88 |
| 1-32 | 639.6 | 348.39 | 622.27 | 488.64 | 643.8 | 352.59 | 626.47 | 492.84 | 141.3166 | 137.743 | 145.0455 | 60930.39 | 59933.14 | 61998.2 | 2065.056 | 997.248 | 1067.808 | 60930.39 | 59933.14 | 61998.2 |
| 1-33 | 622.27 | 488.64 | 643.26 | 627.95 | 626.47 | 492.84 | 647.46 | 632.15 | 140.8824 | 136.1492 | 145.704 | 60807.86 | 59496.62 | 62189.66 | 2693.04 | 1311.24 | 1381.8 | 60807.86 | 59496.62 | 62189.66 |
| 1-34 | 643.26 | 627.95 | 668.26 | 768.21 | 647.46 | 632.15 | 672.46 | 772.41 | 142.4706 | 137.6407 | 147.3816 | 61257.87 | 59904.96 | 62681.33 | 2776.368 | 1352.904 | 1423.464 | 61257.87 | 59904.96 | 62681.33 |
| 1-35 | 668.26 | 768.21 | 627.62 | 907.92 | 672.46 | 772.41 | 631.82 | 912.12 | 145.5008 | 142.7361 | 148.4519 | 62130.49 | 61333.59 | 62997.96 | 1664.376 | 796.908 | 867.468 | 62130.49 | 61333.59 | 62997.96 |
| 1-36 | 627.62 | 907.92 | 786.64 | 68.37 | 631.82 | 912.12 | 790.84 | 72.57 | 854.4774 | 857.8364 | 851.1465 | 771091.6 | 776843.3 | 765410.4 | 11432.9 | 5751.732 | 5681.172 | 776843.3 | 771091.6 | 765410.4 |
| 1-37 | 786.64 | 68.37 | 754.28 | 208.44 | 790.84 | 72.57 | 758.48 | 212.64 | 143.7594 | 146.9926 | 146.9926 | 61626.77 | 60757.29 | 62566.82 | 1809.528 | 869.484 | 940.044 | 61626.77 | 60757.29 | 62566.82 |
| 1-38 | 754.28 | 208.44 | 762.36 | 348.65 | 758.48 | 212.64 | 766.56 | 352.85 | 140.4426 | | | | | | | | | | | |

| | | | | | | | | | | | | | | | | | | | | |
|------|--------|--------|--------|--------|--------|--------|--------|---------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|
| 2-15 | 174.42 | 908.54 | 317.74 | 68.09 | 178.62 | 912.74 | 321.94 | 72.29 | 852.5824 | 856.0304 | 849.1621 | 767856.8 | 773748 | 762036.2 | 11711.78 | 5891.172 | 5820.612 | 767856.8 | 773748 | 762036.2 |
| 2-16 | 317.74 | 68.09 | 319.57 | 208.02 | 321.94 | 72.29 | 323.77 | 212.22 | 139.942 | 135.7507 | 144.2561 | 60543.75 | 59388.25 | 61769.82 | 2381.568 | 1155.504 | 1226.064 | 60543.75 | 59388.25 | 61769.82 |
| 2-17 | 319.57 | 208.02 | 371.63 | 348 | 323.77 | 212.22 | 375.83 | 352.2 | 149.3474 | 143.968 | 154.7678 | 63264.64 | 61686.79 | 64913.06 | 2326.272 | 1577.856 | 1648.416 | 63264.64 | 61686.79 | 64913.06 |
| 2-18 | 371.63 | 348 | 347.91 | 488.66 | 375.83 | 352.2 | 492.86 | 142.646 | 139.287 | 146.1693 | 61307.87 | 60360.86 | 63235.45 | 1964.592 | 947.016 | 1017.576 | 61307.87 | 60360.86 | 63235.45 | |
| 2-19 | 347.91 | 488.66 | 353.28 | 628.47 | 352.11 | 492.86 | 357.48 | 632.67 | 139.9131 | 135.615 | 144.3276 | 60535.67 | 59351.44 | 61790.47 | 2439.024 | 1184.232 | 1254.792 | 60535.67 | 59351.44 | 61790.47 |
| 2-20 | 353.28 | 628.47 | 324.68 | 768.55 | 357.48 | 632.67 | 328.88 | 772.75 | 142.9698 | 139.7827 | 146.3287 | 61400.37 | 60499.21 | 62372.08 | 1872.864 | 901.152 | 971.712 | 61400.37 | 60499.21 | 62372.08 |
| 2-21 | 324.68 | 768.55 | 292.36 | 908.62 | 328.88 | 772.75 | 296.56 | 912.82 | 143.7504 | 140.6925 | 146.9849 | 61624.19 | 60754.37 | 62564.57 | 1810.2 | 869.82 | 940.38 | 61624.19 | 60754.37 | 62564.57 |
| 2-22 | 292.36 | 908.62 | 505.33 | 68.41 | 296.56 | 912.82 | 509.53 | 72.61 | 866.7809 | 869.8351 | 863.7566 | 792269.1 | 797573.2 | 787035.5 | 10537.63 | 5304.096 | 5233.536 | 792269.1 | 797573.2 | 787035.5 |
| 2-23 | 505.33 | 68.41 | 496.47 | 208.2 | 509.53 | 72.61 | 500.67 | 212.4 | 140.0705 | 136.2175 | 144.0654 | 60579.74 | 59515.21 | 61714.84 | 2199.624 | 1064.532 | 1135.092 | 60579.74 | 59515.21 | 61714.84 |
| 2-24 | 496.47 | 208.2 | 494.96 | 348.56 | 500.67 | 212.4 | 499.16 | 352.76 | 140.3681 | 136.2797 | 144.585 | 60663.21 | 59532.15 | 61864.83 | 2332.68 | 1131.06 | 1201.62 | 60663.21 | 59532.15 | 61864.83 |
| 2-25 | 494.96 | 348.56 | 477.66 | 488.56 | 499.16 | 352.76 | 481.86 | 492.76 | 141.0648 | 137.4914 | 144.7938 | 60859.29 | 59863.89 | 61925.25 | 2061.36 | 995.4 | 1065.96 | 60859.29 | 59863.89 | 61925.25 |
| 2-26 | 477.66 | 488.56 | 498.41 | 628.86 | 481.86 | 492.76 | 502.61 | 633.06 | 141.8261 | 137.1026 | 146.6382 | 61074.65 | 59757.11 | 62462.75 | 2705.64 | 1317.54 | 1388.1 | 61074.65 | 59757.11 | 62462.75 |
| 2-27 | 498.41 | 628.86 | 477.24 | 768.04 | 502.61 | 633.06 | 481.44 | 772.24 | 140.7808 | 137.3435 | 144.3808 | 60779.24 | 59823.24 | 61805.81 | 1982.568 | 956.004 | 1026.564 | 60779.24 | 59823.24 | 61805.81 |
| 2-28 | 477.24 | 768.04 | 496.46 | 908.08 | 481.44 | 772.24 | 500.66 | 912.28 | 141.3528 | 136.6679 | 146.129 | 60940.61 | 59638.11 | 62313.67 | 2675.568 | 1302.504 | 1373.064 | 60940.61 | 59638.11 | 62313.67 |
| 2-29 | 496.46 | 908.08 | 647.58 | 68.89 | 500.66 | 912.28 | 651.78 | 73.09 | 852.6882 | 856.0912 | 849.313 | 768037.1 | 773852.2 | 762292.6 | 11559.58 | 5815.068 | 5744.508 | 768037.1 | 773852.2 | 762292.6 |
| 2-30 | 647.58 | 68.89 | 677.69 | 208.46 | 651.78 | 73.09 | 681.89 | 212.66 | 142.7809 | 137.8273 | 147.8073 | 61346.4 | 59956.37 | 62806.99 | 2850.624 | 1390.032 | 1460.592 | 61346.4 | 59956.37 | 62806.99 |
| 2-31 | 677.69 | 208.46 | 644.94 | 348.17 | 681.89 | 212.66 | 649.14 | 352.37 | 143.4972 | 140.4573 | 146.7147 | 61551.45 | 60688.26 | 62485.19 | 1796.928 | 863.184 | 933.744 | 61551.45 | 60688.26 | 62485.19 |
| 2-32 | 644.94 | 348.17 | 646.18 | 488.81 | 649.14 | 352.37 | 650.38 | 493.01 | 146.4555 | 136.4721 | 144.9421 | 60741.15 | 59584.64 | 61968.22 | 2383.584 | 1156.512 | 1227.072 | 60741.15 | 59584.64 | 61968.22 |
| 2-33 | 646.18 | 488.81 | 685.68 | 628.77 | 650.38 | 493.01 | 689.88 | 632.97 | 145.4271 | 140.2743 | 150.638 | 62109.05 | 60636.87 | 63651.8 | 3014.928 | 1472.184 | 1542.744 | 62109.05 | 60636.87 | 63651.8 |
| 2-34 | 685.68 | 628.77 | 673.84 | 768.22 | 689.88 | 632.97 | 678.04 | 772.42 | 139.9517 | 136.1978 | 143.853 | 60546.49 | 59509.84 | 61653.69 | 2143.848 | 1036.644 | 1107.204 | 60546.49 | 59509.84 | 61653.69 |
| 2-35 | 673.84 | 768.22 | 628.52 | 908.01 | 678.04 | 772.42 | 632.72 | 912.21 | 146.9529 | 144.3498 | 149.7464 | 62555.15 | 61796.88 | 63383.97 | 1587.096 | 758.268 | 828.828 | 62555.15 | 61796.88 | 63383.97 |
| 2-36 | 628.52 | 908.01 | 790.49 | 68.78 | 632.72 | 912.21 | 794.69 | 72.98 | 854.7171 | 858.0592 | 851.4033 | 771501.3 | 777225.5 | 765847.6 | 11377.97 | 5724.264 | 5653.704 | 771501.3 | 777225.5 | 765847.6 |
| 2-37 | 790.49 | 68.78 | 782.43 | 208.61 | 794.69 | 72.98 | 786.63 | 212.81 | 140.0621 | 136.183 | 144.0817 | 60577.39 | 59505.8 | 61719.54 | 2213.736 | 1071.588 | 1142.148 | 60577.39 | 59505.8 | 61719.54 |
| 2-38 | 782.43 | 208.61 | 744.1 | 348.8 | 786.63 | 212.81 | 748.3 | 353 | 145.3356 | 142.4854 | 148.3689 | 62082.43 | 61262.08 | 62973.33 | 1711.248 | 820.344 | 890.904 | 62082.43 | 61262.08 | 62973.33 |
| 2-39 | 744.1 | 348.8 | 804.78 | 488.12 | 748.3 | 353 | 808.98 | 492.32 | 151.9609 | 146.4493 | 157.5037 | 62502.12 | 62407.4 | 65767.4 | 3360 | 1644.72 | 1715.28 | 64052.12 | 62407.4 | 65767.4 |
| 2-40 | 804.78 | 488.12 | 780.18 | 628.22 | 808.98 | 492.32 | 784.38 | 632.42 | 142.2433 | 138.9181 | 145.7349 | 61193.17 | 60258.25 | 62198.65 | 1940.4 | 934.92 | 1005.48 | 61193.17 | 60258.25 | 62198.65 |
| 2-41 | 780.18 | 628.22 | 751.2 | 768.67 | 784.38 | 632.42 | 755.4 | 772.87 | 143.4087 | 140.2319 | 146.7572 | 61526.04 | 60624.97 | 62497.67 | 1872.696 | 901.068 | 971.628 | 61526.04 | 60624.97 | 62497.67 |
| 2-42 | 751.2 | 768.67 | 799.8 | 908.09 | 755.4 | 772.87 | 804 | 912.29 | 147.6479 | 142.3229 | 153.0181 | 62759.9 | 61215.81 | 64374.54 | 3158.736 | 1544.088 | 1614.648 | 62759.9 | 61215.81 | 64374.54 |
| 2-43 | 799.8 | 908.09 | 881.7 | 68.39 | 804 | 912.29 | 885.9 | 72.59 | 843.6846 | 847.4695 | 839.9247 | 752763.7 | 759164.5 | 746433.5 | 12731.04 | 6400.8 | 6330.24 | 752763.7 | 759164.5 | 746433.5 |
| 2-44 | 881.7 | 68.39 | 908.58 | 208.45 | 885.9 | 72.59 | 912.78 | 212.65 | 142.6161 | 137.7401 | 147.57 | 61299.34 | 59932.32 | 62736.91 | 2804.592 | 1367.016 | 1437.576 | 61299.34 | 59932.32 | 62736.91 |
| 2-45 | 908.58 | 208.45 | 938.78 | 348.35 | 912.78 | 212.65 | 942.98 | 352.55 | 143.1225 | 138.1683 | 148.1491 | 61444.05 | 60050.49 | 62908.17 | 2857.68 | 1393.56 | 1464.12 | 61444.05 | 60050.49 | 62908.17 |
| 2-46 | 938.78 | 348.35 | 891.03 | 488.12 | 942.98 | 352.55 | 895.23 | 492.32 | 147.7014 | 145.1827 | 150.4126 | 62775.72 | 62038.03 | 63583.96 | 1545.936 | 737.688 | 808.248 | 62775.72 | 62038.03 | 63583.96 |
| 2-47 | 891.03 | 488.12 | 894.28 | 628.51 | 895.23 | 492.32 | 898.48 | 632.71 | 140.4276 | 136.1933 | 144.7818 | 60679.91 | 59508.62 | 61921.77 | 2413.152 | 1171.296 | 1241.856 | 60679.91 | 59508.62 | 61921.77 |
| 2-48 | 894.28 | 628.51 | 892.76 | 767.92 | 898.48 | 632.71 | 896.96 | 772.12 | 139.4183 | 135.3309 | 143.635 | 60397.46 | 59274.46 | 61591.01 | 2316.552 | 1122.996 | 1193.556 | 60397.46 | 59274.46 | 61591.01 |
| 2-49 | 892.76 | 767.92 | 909.63 | 908.12 | 896.96 | 772.12 | 913.83 | 912.32 | 141.213 | 136.5889 | 145.9291 | 60900.64 | 59616.53 | 62255.3 | 2638.776 | 1284.108 | 1354.668 | 60900.64 | 59616.53 | 62255.3 |
| 3-1 | -2.1 | -2.1 | 73.84 | 68.23 | 2.1 | 2.1 | 78.04 | 72.43 | 103.5046 | 97.56949 | 109.4401 | 51673.19 | 50479.8 | 52937.14 | 2457.336 | 1193.388 | 1263.948 | 51673.19 | 50479.8 | 52937.14 |
| 3-2 | 73.84 | 68.23 | 54.66 | 208.35 | 78.04 | 72.43 | 58.86 | 212.55 | 141.4266 | 137.9162 | 145.0954 | 60961.49 | 59980.87 | 62012.66 | 2031.792 | 980.616 | 1051.176 | 60961.49 | 59980.87 | 62012.66 |
| 3-3 | 54.66 | 208.35 | 102.51 | 348.87 | 58.86 | 212.55 | 106.71 | 353.07 | 148.4436 | 143.1379 | 153.7956 | 62995.49 | 61448.46 | 64613.08 | 3164.616 | 1547.028 | 1617.588 | 62995.49 | 61448.46 | 64613.08 |
| 3-4 | 102.51 | 348.87 | 50.45 | 488.05 | 106.71 | 353.07 | 54.65 | 492.25 | 148.5978 | 146.2354 | 151.1569 | 63041.32 | 62344.79 | 63808.4 | 1463.616 | 696.528 | 767.088 | 63041.32 | 62344.79 | 63808.4 |
| 3-5 | 50.45 | 488.05 | 105.56 | 628.72 | 54.65 | 492.25 | 109.76 | 632.92 | 151.08 | 145.6568 | 156.5407 | 63785.16 | 62175.89 | 65464.99 | 3289.104 | 1609.272 | 1679.832 | 63785.16 | 62175.89 | 65464.99 |
| 3-6 | 105.56 | 628.72 | 93.09 | 768.08 | 109.76 | 632.92 | 97.29 | 772.28 | 139.9168 | 136.1841 | 143.798 | 60536.71 | 59506.11 | 61637.87 | 2131.752 | 1030.596 | 1101.156 | 60536.71 | 59506.11 | 61637.87 |
| 3-7 | 93.09 | 768.08 | 30.07 | 908.38 | 97.29 | 772.28 | 34.27 | 912.58 | 153.8038 | 151.7951 | 156.013 | 64615.61 | 64001.74 | 65300.04 | 1298.304 | 613.872 | 684.432 | 64615.61 | 64001.74 | 65300.04 |
| 3-8 | 30.07 | 908.38 | 242.13 | 68.18 | 34.27 | 912.58 | 246.33 | 72.38 | 866.548 | 869.6075 | 863.5186 | 791865.5 | 797177.1 | 786624.4 | 10552.75 | 5311.656 | 5241.096 | 791865.5 | 797177.1 | 786624.4 |
| 3-9 | 242.13 | 68.18 | 196.58 | 208.78 | 246.33 | 72.38 | 200.78 | 212.98 | 147.7943 | 145.1896 | 150.5884 | 62803.16 | 62040.02 | 63636.86 | 1596.84 | 763.14 | 833.7 | 62803.16 | 62040.02 | 63636.86 |
| 3-10 | 196.58 | 208.78 | 202.9 | 348.73 | 200.78 | 212.98 | 207.1 | 352.93 | 140.0926 | 135.7666 | 144.5334 | 60585.94 | 59392.56 | 61849.89 | 2457.336 | 1193.388 | 1263.948 | 60585.94 | 59392.56 | 61849.89 |
| 3-11 | 202.9 | 348.73 | 246.56 | 488.18 | 207.1 | 352.93 | 250.76 | 492.38 | 146.1249 | 140.8888 | 151.413 | 62312.5 | 60809.65 | 63885.9 | 3076.248 | 1502.844 | 1573.404 | 62312.5 | 60809.65 | 63885.9 |
| 3-12 | 246.56 | 488.18 | 247.76 | 628.07 | 250.76 | 492.38 | 251.96 | 632.27 | 139.8951 | 135.7232 | 144.1912 | 60530.65 | 59380.78 | 61751.09 | 2370.312 | 1149.876 | 1220.436 | 60530.65 | 59380.78 | 61751.09 |
| 3-13 | 247.76 | 628.07 | 200.58 | 768.43 | 251.96 | 632.27 | 204.78 | 772.63 | 148.0773 | 145.5316 | 150.814 | 62886.88 | 62139.45 | 63704.87 | 1565.424 | 747.432 | 817.992 | 62886.88 | 62139.45 | 63704.87 |
| 3-14 | 200.58 | 768.43 | 173.32 | 908.74 | 204.78 | 772.63 | 177.52 | 912.94 | 142.9336 | 139.6985 | 146.3383 | 61390 | 60475.66 | 62374.9 | 1899.24 | 914.34 | 984.9 | | | |

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|------|--------|--------|--------|--------|--------|--------|--------|--------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|
| 3-38 | 738.23 | 208.12 | 727.71 | 348.52 | 742.43 | 212.32 | 731.91 | 352.72 | 140.7936 | 136.9931 | 144.738 | 60782.83 | 59727.12 | 61909.1 | 2181.984 | 1055.712 | 1126.272 | 60782.83 | 59727.12 | 61909.1 |
| 3-39 | 727.71 | 348.52 | 739.83 | 488.03 | 731.91 | 352.72 | 744.03 | 492.23 | 140.0355 | 135.5416 | 144.6337 | 60569.93 | 59331.52 | 61878.91 | 2547.384 | 1238.412 | 1308.972 | 60569.93 | 59331.52 | 61878.91 |
| 3-40 | 739.83 | 488.03 | 801.77 | 628.65 | 744.03 | 492.23 | 805.97 | 632.85 | 153.6572 | 148.1362 | 159.2085 | 64570.55 | 62904.32 | 66307.33 | 3403.008 | 1666.224 | 1736.784 | 64570.55 | 62904.32 | 66307.33 |
| 3-41 | 801.77 | 628.65 | 743.48 | 768.17 | 805.97 | 632.85 | 747.68 | 772.37 | 151.207 | 149.052 | 153.5616 | 63823.55 | 63176.5 | 64541.17 | 1364.664 | 647.052 | 717.612 | 63823.55 | 63176.5 | 64541.17 |
| 3-42 | 743.48 | 768.17 | 752.08 | 908.86 | 747.68 | 772.37 | 756.28 | 913.06 | 140.9526 | 136.5609 | 145.4543 | 60827.64 | 59608.88 | 62116.95 | 1208.072 | 1218.756 | 1289.316 | 60827.64 | 59608.88 | 62116.95 |
| 3-43 | 752.08 | 908.86 | 864.04 | 68.63 | 756.28 | 913.06 | 868.24 | 72.83 | 847.6565 | 851.278 | 844.0612 | 759481.5 | 765634.2 | 753399.3 | 12234.94 | 6152.748 | 6082.188 | 759481.5 | 765634.2 | 753399.3 |
| 3-44 | 864.04 | 68.63 | 896.96 | 208.44 | 868.24 | 72.83 | 901.16 | 212.64 | 143.6334 | 138.6179 | 148.7171 | 61590.56 | 60174.91 | 63076.77 | 2901.864 | 1415.652 | 1486.212 | 61590.56 | 60174.91 | 63076.77 |
| 3-45 | 896.96 | 208.44 | 950.79 | 348.81 | 901.16 | 212.64 | 954.99 | 353.01 | 150.3376 | 144.9324 | 155.7818 | 63561.41 | 61965.41 | 65227.97 | 3262.56 | 1596 | 1666.56 | 63561.41 | 61965.41 | 65227.97 |
| 3-46 | 950.79 | 348.81 | 916.88 | 488.21 | 954.99 | 353.01 | 921.08 | 492.41 | 143.4651 | 140.4685 | 146.6412 | 61542.25 | 60691.41 | 62463.64 | 1772.232 | 850.836 | 921.396 | 61542.25 | 60691.41 | 62463.64 |
| 3-47 | 916.88 | 488.21 | 892.85 | 628.44 | 921.08 | 492.41 | 897.05 | 632.64 | 142.274 | 138.9284 | 145.785 | 61201.89 | 60261.09 | 62213.25 | 1952.16 | 940.8 | 1011.36 | 61201.89 | 60261.09 | 62213.25 |
| 3-48 | 892.85 | 628.44 | 901.89 | 768.68 | 897.05 | 632.64 | 906.09 | 772.88 | 140.5311 | 136.1261 | 145.0455 | 60708.98 | 59490.31 | 61998.21 | 2507.904 | 1218.672 | 1289.232 | 60708.98 | 59490.31 | 61998.21 |
| 3-49 | 901.89 | 768.68 | 917.32 | 907.97 | 906.09 | 772.88 | 921.52 | 912.17 | 140.142 | 135.556 | 144.8265 | 60599.79 | 59335.42 | 61934.72 | 2599.296 | 1264.368 | 1334.928 | 60599.79 | 59335.42 | 61934.72 |
| 4-1 | -2.1 | -2.1 | 95.37 | 68.02 | 2.1 | 2.1 | 99.57 | 72.22 | 120.0717 | 114.2136 | 125.9375 | 55377.22 | 54004.74 | 56820.25 | 2815.512 | 1372.476 | 1443.036 | 55377.22 | 54004.74 | 56820.25 |
| 4-2 | 95.37 | 68.02 | 84.3 | 208.18 | 99.57 | 72.22 | 88.5 | 212.38 | 140.5965 | 136.8148 | 144.5234 | 60727.37 | 59678.29 | 61847.01 | 2168.712 | 1049.076 | 1119.636 | 60727.37 | 59678.29 | 61847.01 |
| 4-3 | 84.3 | 208.18 | 63.99 | 348.69 | 88.5 | 212.38 | 68.19 | 352.89 | 141.9703 | 138.4961 | 145.604 | 61115.56 | 60141.16 | 62160.52 | 2019.36 | 974.4 | 1044.96 | 61115.56 | 60141.16 | 62160.52 |
| 4-4 | 63.99 | 348.69 | 101.22 | 488.57 | 68.19 | 352.89 | 105.42 | 492.77 | 144.7497 | 139.6426 | 149.9183 | 61912.49 | 60460.04 | 63435.49 | 2975.448 | 1452.444 | 1523.004 | 61912.49 | 60460.04 | 63435.49 |
| 4-5 | 101.22 | 488.57 | 110.64 | 628.59 | 105.42 | 492.77 | 114.84 | 632.79 | 140.3365 | 135.9203 | 144.8617 | 60654.34 | 59434.32 | 61944.91 | 2510.592 | 1220.016 | 1290.576 | 60654.34 | 59434.32 | 61944.91 |
| 4-6 | 110.64 | 628.59 | 63.11 | 768.25 | 114.84 | 632.79 | 67.31 | 772.45 | 147.5263 | 145.0014 | 150.2438 | 62724.02 | 61985.4 | 63533.19 | 1547.784 | 738.612 | 809.172 | 62724.02 | 61985.4 | 63533.19 |
| 4-7 | 63.11 | 768.25 | 66.85 | 908.2 | 67.31 | 772.45 | 71.05 | 912.4 | 140 | 135.7508 | 144.3685 | 60559.99 | 59388.27 | 61802.27 | 2413.992 | 1171.716 | 1242.276 | 60559.99 | 59388.27 | 61802.27 |
| 4-8 | 66.85 | 908.2 | 194.35 | 68.04 | 71.05 | 912.4 | 198.55 | 72.24 | 849.7794 | 853.3151 | 846.2706 | 763085.1 | 769106.7 | 7571.34 | 11972.69 | 6021.624 | 5951.064 | 763085.1 | 769106.7 | 7571.34 |
| 4-9 | 194.35 | 68.04 | 203.29 | 208.21 | 198.55 | 72.24 | 207.49 | 212.41 | 140.4548 | 136.0526 | 144.9667 | 60687.55 | 59470.31 | 61975.36 | 2505.048 | 1217.244 | 1287.804 | 60687.55 | 59470.31 | 61975.36 |
| 4-10 | 203.29 | 208.21 | 165.27 | 348.31 | 207.49 | 212.41 | 169.47 | 352.51 | 145.1672 | 142.3072 | 148.2103 | 62033.53 | 61211.34 | 62926.28 | 1714.944 | 822.192 | 892.752 | 62033.53 | 61211.34 | 62926.28 |
| 4-11 | 165.27 | 348.31 | 177.93 | 488.81 | 169.47 | 352.51 | 182.13 | 493.01 | 141.0692 | 136.5623 | 145.6789 | 60860.53 | 59609.26 | 62182.35 | 2573.088 | 1251.264 | 1321.824 | 60860.53 | 59609.26 | 62182.35 |
| 4-12 | 177.93 | 488.81 | 168.91 | 628.48 | 182.13 | 493.01 | 173.11 | 632.68 | 139.961 | 136.1135 | 143.9507 | 60549.07 | 59486.89 | 61681.81 | 2194.92 | 1062.18 | 1132.74 | 60549.07 | 59486.89 | 61681.81 |
| 4-13 | 168.91 | 628.48 | 163.09 | 767.98 | 173.11 | 632.68 | 167.29 | 772.18 | 139.6214 | 135.6705 | 143.7091 | 60454.12 | 59366.49 | 61612.31 | 2245.824 | 1087.632 | 1158.192 | 60454.12 | 59366.49 | 61612.31 |
| 4-14 | 163.09 | 767.98 | 164 | 908.62 | 167.29 | 772.18 | 168.2 | 912.82 | 140.6429 | 136.4797 | 144.9301 | 60740.44 | 59586.7 | 61964.74 | 2378.04 | 1153.74 | 1224.3 | 60740.44 | 59586.7 | 61964.74 |
| 4-15 | 164 | 908.62 | 315.59 | 68 | 168.2 | 912.82 | 319.79 | 72.2 | 854.1789 | 857.5807 | 850.8049 | 770581.5 | 776404.6 | 764828.9 | 11575.7 | 5823.132 | 5752.572 | 770581.5 | 776404.6 | 764828.9 |
| 4-16 | 315.59 | 68 | 368.45 | 208.32 | 319.79 | 72.2 | 372.65 | 212.52 | 149.9463 | 144.556 | 155.3766 | 63443.88 | 61856.45 | 65101.87 | 3245.424 | 1587.432 | 1657.992 | 63443.88 | 61856.45 | 65101.87 |
| 4-17 | 368.45 | 208.32 | 373.25 | 348.53 | 372.65 | 212.52 | 377.45 | 352.73 | 140.2921 | 136.0113 | 144.6902 | 60641.88 | 59459.08 | 61895.25 | 2436.168 | 1182.804 | 1253.364 | 60641.88 | 59459.08 | 61895.25 |
| 4-18 | 373.25 | 348.53 | 359.79 | 488.47 | 377.45 | 352.73 | 363.99 | 492.67 | 140.5858 | 136.884 | 144.4371 | 60724.38 | 59697.22 | 61822.09 | 2124.864 | 1027.152 | 1097.712 | 60724.38 | 59697.22 | 61822.09 |
| 4-19 | 359.79 | 488.47 | 365.7 | 628.56 | 363.99 | 492.67 | 369.9 | 632.76 | 140.2146 | 135.9008 | 144.6438 | 60620.14 | 59429.02 | 61881.82 | 2452.8 | 1191.12 | 1261.68 | 60620.14 | 59429.02 | 61881.82 |
| 4-20 | 365.7 | 628.56 | 318.11 | 768.28 | 369.9 | 632.76 | 322.31 | 772.48 | 147.6025 | 145.0789 | 150.3185 | 62746.49 | 62007.87 | 63555.66 | 1547.784 | 738.612 | 809.172 | 62746.49 | 62007.87 | 63555.66 |
| 4-21 | 318.11 | 768.28 | 278.32 | 907.99 | 322.31 | 772.48 | 282.52 | 912.19 | 145.2657 | 142.4713 | 148.2455 | 62062.13 | 61258.08 | 62936.74 | 1678.656 | 804.048 | 874.608 | 62062.13 | 61258.08 | 62936.74 |
| 4-22 | 278.32 | 907.99 | 512.59 | 68.49 | 282.52 | 912.19 | 516.79 | 72.69 | 871.5748 | 874.5067 | 868.6737 | 800602.7 | 795554 | 10167.86 | 5119.212 | 5048.652 | 800602.7 | 795554 | 10167.86 | |
| 4-23 | 512.59 | 68.49 | 508.3 | 208.29 | 516.79 | 72.69 | 512.5 | 212.49 | 139.8658 | 135.8655 | 144 | 60522.44 | 59419.44 | 61696.01 | 2276.568 | 1103.004 | 1173.564 | 60522.44 | 59419.44 | 61696.01 |
| 4-24 | 508.3 | 208.29 | 457.91 | 348.89 | 516.79 | 72.69 | 462.11 | 353.09 | 149.357 | 146.9184 | 151.9887 | 63267.51 | 62545.03 | 64060.56 | 1515.528 | 722.484 | 793.044 | 63267.51 | 62545.03 | 64060.56 |
| 4-25 | 457.91 | 348.89 | 471.27 | 488.79 | 462.11 | 353.09 | 475.47 | 492.99 | 140.5365 | 136.0088 | 145.166 | 60710.5 | 59458.4 | 62033.16 | 2574.768 | 1252.104 | 1322.664 | 60710.5 | 59458.4 | 62033.16 |
| 4-26 | 471.27 | 488.79 | 513.59 | 628.25 | 475.47 | 492.99 | 517.79 | 632.45 | 145.7397 | 140.5229 | 151.0043 | 62200.07 | 60708.4 | 63762.31 | 3053.904 | 1491.672 | 1562.232 | 62200.07 | 60708.4 | 63762.31 |
| 4-27 | 513.59 | 628.25 | 516.8 | 768.1 | 517.79 | 632.45 | 521 | 772.3 | 139.8868 | 135.6536 | 144.2405 | 60528.33 | 59361.9 | 61765.31 | 2403.408 | 1166.424 | 1236.984 | 60528.33 | 59361.9 | 61765.31 |
| 4-28 | 516.8 | 768.1 | 431.95 | 907.93 | 521 | 772.3 | 436.15 | 912.13 | 163.5602 | 162.251 | 165.0729 | 67711.95 | 67285.4 | 68209.06 | 923.664 | 426.552 | 497.112 | 67711.95 | 67285.4 | 68209.06 |
| 4-29 | 431.95 | 907.93 | 618.8 | 68.69 | 436.15 | 912.13 | 623 | 72.89 | 859.7888 | 862.9902 | 856.6165 | 780196.7 | 785712.1 | 774751.9 | 10960.15 | 5515.356 | 5444.796 | 780196.7 | 785712.1 | 774751.9 |
| 4-30 | 618.8 | 68.69 | 682.38 | 208.58 | 623 | 72.89 | 686.58 | 212.78 | 153.6608 | 148.114 | 159.2359 | 64571.63 | 62897.76 | 66316.06 | 3418.296 | 1673.868 | 1744.428 | 64571.63 | 62897.76 | 66316.06 |
| 4-31 | 682.38 | 208.58 | 652.76 | 348.06 | 686.58 | 212.78 | 656.96 | 352.26 | 142.5904 | 139.4434 | 145.9113 | 61292.01 | 60404.47 | 62250.12 | 1845.648 | 887.544 | 958.104 | 61292.01 | 60404.47 | 62250.12 |
| 4-32 | 652.76 | 348.06 | 655.22 | 487.94 | 656.96 | 352.26 | 659.42 | 492.14 | 139.9016 | 135.6912 | 144.2338 | 60532.47 | 59372.09 | 61763.4 | 2391.312 | 1160.376 | 1230.936 | 60532.47 | 59372.09 | 61763.4 |
| 4-33 | 655.22 | 487.94 | 633.38 | 628.86 | 659.42 | 492.14 | 637.58 | 633.06 | 142.6024 | 139.1777 | 146.1882 | 61295.43 | 60330.44 | 62330.98 | 2000.544 | 964.992 | 1035.552 | 61295.43 | 60330.44 | 62330.98 |
| 4-34 | 633.38 | 628.86 | 686.66 | 768 | 637.58 | 633.06 | 690.86 | 772.2 | 148.9923 | 143.5885 | 154.4354 | 63158.7 | 61577.65 | 64810.31 | 3232.656 | 1581.048 | 1651.608 | 63158.7 | 61577.65 | 64810.31 |
| 4-35 | 686.66 | 768 | 609.82 | 908.85 | 690.86 | 772.2 | 614.02 | 913.05 | 160.4466 | 158.8732 | 162.2223 | 66703.11 | 66200.7 | 67276.07 | 1075.368 | 502.404 | 572.964 | 66703.11 | 66200.7 | 67276.07 |
| 4-36 | 609.82 | 908.85 | 792.12 | 68.57 | 614.02 | 913.05 | 796.32 | 72.77 | 859.8278 | 863.0562 | 856.6283 | 780263.8 | 785826.1 | 774772 | 11054.06 | 5562.312 | 5491.752 | 780263.8 | 785826.1 | 774772 |
| 4-37 | 792.12 | 68.57 | 785.54 | 208.09 | 796.32 | 72.77 | 789.74 | 212.29 | 139.6751 | 135.7487 | 143.7397 | 60469.13 | 59387.71 | 61621.1 | 2233.392 | 1081.416 | 1151.976 | 60469.1 | | |

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|------|--------|--------|--------|--------|--------|--------|--------|--------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|
| 5-12 | 255.97 | 488.38 | 156.86 | 627.97 | 260.17 | 492.58 | 161.06 | 632.17 | 171.1963 | 170.3039 | 172.2889 | 70268.16 | 69963.41 | 70643.47 | 680.064 | 304.752 | 375.312 | 70268.16 | 69963.41 | 70643.47 |
| 5-13 | 156.86 | 627.97 | 225.32 | 768.51 | 161.06 | 632.17 | 229.52 | 772.71 | 156.3274 | 150.7247 | 161.9541 | 65398.26 | 63677.94 | 67189.14 | 3511.2 | 1720.32 | 1790.88 | 65398.26 | 63677.94 | 67189.14 |
| 5-14 | 225.32 | 768.51 | 161.29 | 908.71 | 229.52 | 772.71 | 165.49 | 912.91 | 154.1294 | 152.1556 | 156.3042 | 64715.88 | 64111.33 | 65390.99 | 1279.656 | 604.548 | 675.108 | 64715.88 | 64111.33 | 65390.99 |
| 5-15 | 161.29 | 908.71 | 315.17 | 68.44 | 165.49 | 912.91 | 319.37 | 72.64 | 854.244 | 857.6326 | 850.8833 | 770692.7 | 776493.7 | 764962.3 | 11531.35 | 5800.956 | 5730.396 | 770692.7 | 776493.7 | 764962.3 |
| 5-16 | 315.17 | 68.44 | 305.13 | 208.14 | 319.37 | 72.64 | 309.33 | 212.34 | 140.0603 | 136.2462 | 144.0185 | 60576.89 | 59523.03 | 61701.32 | 2178.288 | 1053.864 | 1124.424 | 60576.89 | 59523.03 | 61701.32 |
| 5-17 | 305.13 | 208.14 | 376.28 | 348.69 | 309.33 | 212.34 | 380.48 | 352.89 | 157.5329 | 151.9 | 163.1876 | 65776.63 | 64033.63 | 67590.19 | 3556.56 | 1743 | 1813.56 | 65776.63 | 64033.63 | 67590.19 |
| 5-18 | 376.28 | 348.69 | 333.47 | 487.97 | 380.48 | 352.89 | 337.67 | 492.17 | 145.7107 | 143.0264 | 148.5841 | 62191.61 | 61416.55 | 63037.24 | 1620.696 | 775.068 | 845.628 | 62191.61 | 61416.55 | 63037.24 |
| 5-19 | 333.47 | 487.97 | 308.2 | 628.01 | 337.67 | 492.17 | 312.4 | 632.21 | 142.3017 | 139 | 145.7708 | 61209.77 | 60280.99 | 62209.12 | 1928.136 | 928.788 | 999.348 | 61209.77 | 60280.99 | 62209.12 |
| 5-20 | 308.2 | 628.01 | 360.32 | 768.86 | 312.4 | 632.21 | 364.52 | 773.06 | 150.1839 | 144.8087 | 155.6003 | 63515.22 | 61929.55 | 65171.44 | 3241.896 | 1585.668 | 1656.228 | 63515.22 | 61929.55 | 65171.44 |
| 5-21 | 360.32 | 768.86 | 327.49 | 908.61 | 364.52 | 773.06 | 331.69 | 912.81 | 143.5544 | 140.517 | 146.7695 | 61567.87 | 60705.02 | 62501.28 | 1796.256 | 862.848 | 933.408 | 61567.87 | 60705.02 | 62501.28 |
| 5-22 | 327.49 | 908.61 | 516.14 | 68.89 | 331.69 | 912.81 | 520.34 | 73.09 | 860.65 | 863.8419 | 857.4875 | 781678.5 | 787182.8 | 776244.8 | 10937.98 | 5504.268 | 5433.708 | 781678.5 | 787182.8 | 776244.8 |
| 5-23 | 516.14 | 68.89 | 457.4 | 208.74 | 520.34 | 73.09 | 461.6 | 212.94 | 151.6852 | 149.5405 | 154.0293 | 63968.41 | 63322.37 | 64685.01 | 1362.648 | 646.044 | 716.604 | 63968.41 | 63322.37 | 64685.01 |
| 5-24 | 457.4 | 208.74 | 456.76 | 348.24 | 461.6 | 212.94 | 460.96 | 352.44 | 139.5015 | 135.3865 | 143.7441 | 60420.66 | 59289.52 | 61622.36 | 2332.848 | 1131.144 | 1201.704 | 60420.66 | 59289.52 | 61622.36 |
| 5-25 | 456.76 | 348.24 | 467.65 | 488.54 | 460.96 | 352.44 | 471.85 | 492.74 | 140.722 | 136.2643 | 145.2858 | 60762.68 | 59527.97 | 62067.96 | 2539.992 | 1234.716 | 1305.276 | 60762.68 | 59527.97 | 62067.96 |
| 5-26 | 467.65 | 488.54 | 423.05 | 628.15 | 471.85 | 492.74 | 427.25 | 632.35 | 146.561 | 143.9351 | 149.377 | 62440.11 | 61677.31 | 63273.48 | 1596.168 | 762.804 | 833.364 | 62440.11 | 61677.31 | 63273.48 |
| 5-27 | 423.05 | 628.15 | 468.36 | 767.99 | 427.25 | 632.35 | 472.56 | 772.19 | 146.9974 | 141.733 | 152.3114 | 62568.22 | 61048.24 | 64158.76 | 3110.52 | 1519.98 | 1590.54 | 62568.22 | 61048.24 | 64158.76 |
| 5-28 | 468.36 | 767.99 | 542.07 | 908.72 | 472.56 | 772.19 | 546.27 | 912.92 | 158.865 | 153.206 | 164.5438 | 66198.1 | 64432.08 | 68034.67 | 3602.592 | 1766.016 | 1836.576 | 66198.1 | 64432.08 | 68034.67 |
| 5-29 | 542.07 | 908.72 | 666.44 | 68.37 | 546.27 | 912.92 | 670.64 | 72.57 | 849.5034 | 853.0566 | 845.977 | 762616 | 768665.5 | 756637.1 | 12028.46 | 6049.512 | 5978.952 | 762616 | 768665.5 | 756637.1 |
| 5-30 | 666.44 | 68.37 | 581.73 | 208.87 | 670.64 | 72.57 | 585.93 | 213.07 | 164.0611 | 162.735 | 165.5897 | 67876.03 | 67442.68 | 68379.95 | 937.272 | 433.356 | 503.916 | 67876.03 | 67442.68 | 68379.95 |
| 5-31 | 581.73 | 208.87 | 652.76 | 348.52 | 585.93 | 213.07 | 656.96 | 352.72 | 156.676 | 151.0396 | 162.3341 | 65507.38 | 63772.95 | 67312.38 | 3539.424 | 1734.432 | 1804.992 | 65507.38 | 63772.95 | 67312.38 |
| 5-32 | 652.76 | 348.52 | 583.94 | 488.84 | 656.96 | 352.72 | 588.14 | 493.04 | 156.2879 | 154.4687 | 158.3091 | 65385.89 | 64820.57 | 66021.77 | 1201.2 | 565.32 | 635.88 | 65385.89 | 64820.57 | 66021.77 |
| 5-33 | 583.94 | 488.84 | 692.05 | 628.06 | 588.14 | 493.04 | 696.25 | 632.26 | 176.2668 | 170.3751 | 182.1616 | 72029.98 | 69987.69 | 74142.83 | 4155.144 | 2042.292 | 2112.852 | 72029.98 | 69987.69 | 74142.83 |
| 5-34 | 692.05 | 628.06 | 578.51 | 768.52 | 696.25 | 632.26 | 582.71 | 772.72 | 180.611 | 180.0819 | 181.3333 | 73580.34 | 73389.5 | 73841.75 | 452.256 | 190.848 | 261.408 | 73580.34 | 73389.5 | 73841.75 |
| 5-35 | 578.51 | 768.52 | 604.39 | 908.05 | 582.71 | 772.72 | 608.59 | 912.25 | 141.9098 | 137.0556 | 146.8439 | 61098.4 | 59744.23 | 62523.12 | 2778.888 | 1354.164 | 1424.724 | 61098.4 | 59744.23 | 62523.12 |
| 5-36 | 604.39 | 908.05 | 767.42 | 68.29 | 608.59 | 912.25 | 771.62 | 72.49 | 855.4389 | 858.7756 | 852.1305 | 772735.6 | 778455.5 | 767086.4 | 11369.06 | 5719.812 | 5649.252 | 772735.6 | 778455.5 | 767086.4 |
| 5-37 | 767.42 | 68.29 | 734.4 | 208.09 | 771.62 | 72.49 | 738.6 | 212.29 | 143.6467 | 140.6154 | 146.8557 | 61594.36 | 60732.69 | 62526.59 | 1793.904 | 861.672 | 932.232 | 61594.36 | 60732.69 | 62526.59 |
| 5-38 | 734.4 | 208.09 | 827.9 | 348.56 | 738.6 | 212.29 | 832.1 | 352.76 | 168.7426 | 162.9233 | 174.57 | 69434.07 | 67504 | 71434.7 | 3930.696 | 1930.068 | 2000.628 | 69434.07 | 67504 | 71434.7 |
| 5-39 | 827.9 | 348.56 | 825.93 | 488.56 | 832.1 | 352.76 | 830.13 | 492.76 | 140.0139 | 135.9401 | 144.2172 | 60563.88 | 59439.71 | 61758.61 | 2318.904 | 1124.172 | 1194.732 | 60563.88 | 59439.71 | 61758.61 |
| 5-40 | 825.93 | 488.56 | 750.27 | 628.84 | 830.13 | 492.76 | 754.47 | 633.04 | 159.3829 | 157.7827 | 161.1862 | 66362.91 | 65855.39 | 66941 | 1085.616 | 507.528 | 578.088 | 66362.91 | 65855.39 | 66941 |
| 5-41 | 750.27 | 628.84 | 733.51 | 768.46 | 754.47 | 633.04 | 737.71 | 772.66 | 140.6223 | 137.0325 | 144.3674 | 60734.64 | 59737.9 | 61801.95 | 2064.048 | 996.744 | 1067.304 | 60734.64 | 59737.9 | 61801.95 |
| 5-42 | 733.51 | 768.46 | 744.5 | 908 | 737.71 | 772.66 | 748.7 | 912.2 | 139.9721 | 135.5102 | 144.5404 | 60552.19 | 59323.02 | 61851.92 | 2528.904 | 1229.172 | 1299.732 | 60552.19 | 59323.02 | 61851.92 |
| 5-43 | 744.5 | 908 | 925.89 | 68.02 | 748.7 | 912.2 | 930.09 | 72.22 | 859.342 | 862.5753 | 856.1378 | 779428.7 | 784996.2 | 773931.9 | 11064.31 | 5567.436 | 5496.876 | 779428.7 | 784996.2 | 773931.9 |
| 5-44 | 925.89 | 68.02 | 933.58 | 208.63 | 930.09 | 72.22 | 937.78 | 212.83 | 140.8201 | 136.4546 | 145.2973 | 60790.31 | 59579.87 | 62071.31 | 2491.44 | 1210.44 | 1281 | 60790.31 | 59579.87 | 62071.31 |
| 5-45 | 933.58 | 208.63 | 861.26 | 347.99 | 937.78 | 212.83 | 865.46 | 352.19 | 157.0076 | 155.3175 | 158.9019 | 65611.39 | 65083.54 | 66209.81 | 1126.272 | 527.856 | 598.416 | 65611.39 | 65083.54 | 66209.81 |
| 5-46 | 861.26 | 347.99 | 922.7 | 488.72 | 865.46 | 352.19 | 926.9 | 492.92 | 153.5572 | 148.0434 | 159.1016 | 64539.81 | 62876.86 | 66273.31 | 3396.456 | 1662.948 | 1733.508 | 64539.81 | 62876.86 | 66273.31 |
| 5-47 | 922.7 | 488.72 | 903.86 | 628.42 | 926.9 | 492.92 | 908.06 | 632.62 | 140.9647 | 137.4449 | 144.6428 | 60831.04 | 59851.09 | 61881.54 | 2030.448 | 979.944 | 1050.504 | 60831.04 | 59851.09 | 61881.54 |
| 5-48 | 903.86 | 628.42 | 883.29 | 768.76 | 908.06 | 632.62 | 887.49 | 772.96 | 141.8395 | 138.375 | 145.464 | 61078.44 | 60107.65 | 62119.79 | 2012.136 | 970.788 | 1041.348 | 61078.44 | 60107.65 | 62119.79 |
| 5-49 | 883.29 | 768.76 | 937.41 | 908.83 | 887.49 | 772.96 | 941.61 | 913.03 | 150.1618 | 144.7503 | 155.6119 | 63508.58 | 61912.66 | 65175.06 | 3262.392 | 1595.916 | 1666.476 | 63508.58 | 61912.66 | 65175.06 |
| | | | | | | | | | | | | | | | 838600.7 | 412773.6 | 425827.2 | | | |

The value of R, E_{charge}, E_{ts}, and E_{rx} has been considered 4096 bits, 50000 Pico-Joules, 10 Pico-Joules, and 204800000 Pico-Joules respectively. Similarly, we have calculated the average energy, minimum energy, and maximum energy for random as well as square deployment. The below table shows the comparison of results.

Table 3: Comparison of results of 3 deployments strategies.

| Deployments | Maximum Energy (pJ) | Minimum Energy (pJ) | Average Energy (pJ) |
|-------------|---------------------|---------------------|---------------------|
| S-shaped | 838600.7 | 412773.6 | 425827.2 |
| Random | 864823.7 | 426308.4 | 438525.9 |
| Spiral | 848969 | 418425.9 | 430717.5 |

6. RESULT ANALYSIS

We have used the data from Table 3 for experimental purposes. As it is visible in Table 3 that the S-shaped in performing better than the other 2 deployment strategies. So we have compared the data of S-shaped deployment with the data taken from existing literature [31]. Applying our strategies (deployment strategies and clustering process) we have obtained a large set of results as depicted in Tables 2, 3, and 4.

Applying Random Deployment Strategy and area wise Clustering Process

The calculations of the energy saved are shown in table 2. There are five iterations and the energy saved has been calculated for every node which sums up to 864823.7 Pico-Joules in case of maximum energy saving. Considering the initial energy of nodes as 1 Joule and not taking duty cycle into account we have calculated the number of days by using the formula

$$days = \frac{1 \times 10^{12} \text{ Joules}}{86400 \times E_s} \quad (11)$$

Where E_s=Energy saved and 1day=86400 seconds. Putting the value of E_s as 864823.7 we get 13 days and 3 hours or 315 hours. So this network can save up to 267.75 hours to 362.25 hours or 11.15 days to 15.09 days.

Applying Spiral Deployment Strategy and area wise Clustering Process

The calculations of the energy saved are shown in table 3. There are five iterations and energy saved that have been calculated for every node which sums up to 848969.0 Pico-Joules in case of maximum energy saving. Considering the initial energy of nodes as 1 Joule and not taking duty cycle into account we have calculated the number of days by using the formula

$$days = \frac{1 \times 10^{12} \text{ Joules}}{86400 \times E_s} \quad (12)$$

Where E_s=Energy saved and 1day=86400 seconds. Putting the value of E_s as 864823.7 we get 13 days and 6 hours or 318 hours. So this network can save up to 270.3 hours to 365.7 hours or 11.25 days to 15.23 days.

Applying S-pattern Deployment Strategy and area wise Clustering Process

The calculations of the energy saved are shown in table 2. There are five iterations and energy saved that have been calculated for every node which sums up to 838600.7 Pico-Joules in case of maximum energy saving. Considering the initial energy of nodes as 1 Joule and not taking duty cycle into account we have calculated the number of days by using the formula

$$days = \frac{1 \times 10^{12} \text{ Joules}}{86400 \times E_s} \quad (13)$$

Where E_s=Energy saved and 1day=86400 seconds.

Putting the value of E_s as 864823.7 we get 13 days and 8 hours or 320 hours. So it can be concluded that the concept can save up to 272 hours to 368 hours or 11.33 days to 15.33 days of a lifetime of WSN. Therefore, from the above calculations, we can say that the s-pattern deployment is performing better than the other two deployments as the network will remain active for a longer time in the case of s-pattern deployment. In this research work, the obtained result (the lifetime of WSN) has been compared with the paper of [30] by scaling up the external environmental parameters like covered area size, several nodes deployed, several rounds have

also been compared and it has been seen that the lifesaving can be done 10 to 11 days by applying their method which can be increased 1 to 5 days in case of random deployment strategies using modified ACO. Lifetime saving can be increased.

We have compared our work with other literature [31] to prove that our experiments have yielded better results than other papers.

Table 4. Comparison of results obtained by our proposed algorithm and existing literature [31].

| Parameters | Totalxy (max) | Totalx y (min) | Energy Saved | Days |
|----------------------------------|-----------------------|---------------------------|-----------------|----------|
| Algorithms | | | | |
| ACO (Random Deployment) | 100389425 972.31 | 100389 269395 .97 | 864823.68 | 13.38 |
| ACO (Spiral Deployment) | 100388152 202.95 | 100387 999246 .18 | 848969.01 6 | 13.63 |
| ACO(S- pattern Deployment) | 36589595.8 2 | 364366 18.21 | 838600.72 8 | 13.8 |
| DE-QPSO | 172149605 57260.80 | 172159 303680 00.00 | 96981073 9.2 | 7 |

In this table, we have compared our work to another literature [30] and found out that our experiment has performed better than the existing literature [31]. We have obtained a value of about 13 days which is 6 days more than the value obtained by applying the DE-QPSO algorithm. In our experiment, we have covered a large area (1 km²) than the existing literature [31]. Other than that, we have also deployed more nodes and have more clusters as well.

7. CONCLUSION

In this research, the lifetime of WSN has been increased to a significant margin theoretically. To choose the best result set among all the obtained results some parameters such as equivalent distribution, number of iterations, maximum energy has been set to a permissible range. To decide which type of deployment should be applied to get the maximum amount of energy and increasing the lifetime of the overall network we can use the fuzzy set in future work. In practical life the level may not match with the theoretical result due to physical dependencies like some external environmental factors. In this research work, we have also considered some physical dependencies like different

environmental hazards as well as physical hazards. To implement those hazards in our experiment we have used an allowable tolerance percentage in this experiment. It is expected that the result may reach up to some significant level, if some fuzzy logic is going to be developed to incorporate the uncertainty into the experimental result to make the situation more realistic. In the future, the fuzzy number system can be implemented in this type of research work to adapt to the uncertainty in the experimental environment.

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