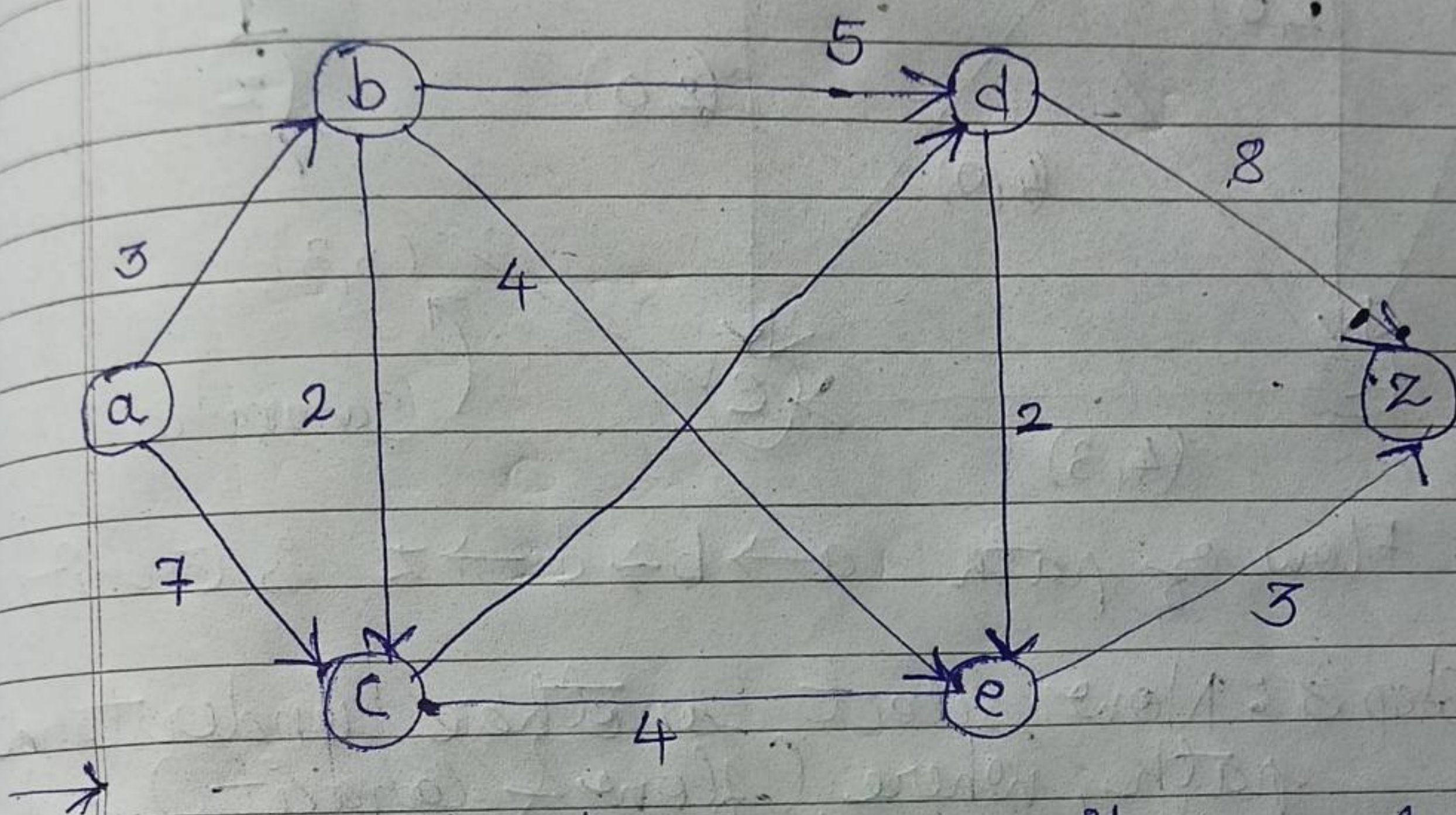


Q3 Using the labelling procedure to find the maximum flow in the transport network in the following figure. Determine the corresponding minimum cut.



Step 1: Select any arbitrary path of given network.

Let's select: $a \rightarrow b \rightarrow e \rightarrow z$

Initially, flow on selected path is zero. Then apply unit flow, till we get any saturated path.

Edge $e \rightarrow z$ will get saturated first so on unit flow of $e \rightarrow z$.

Here,

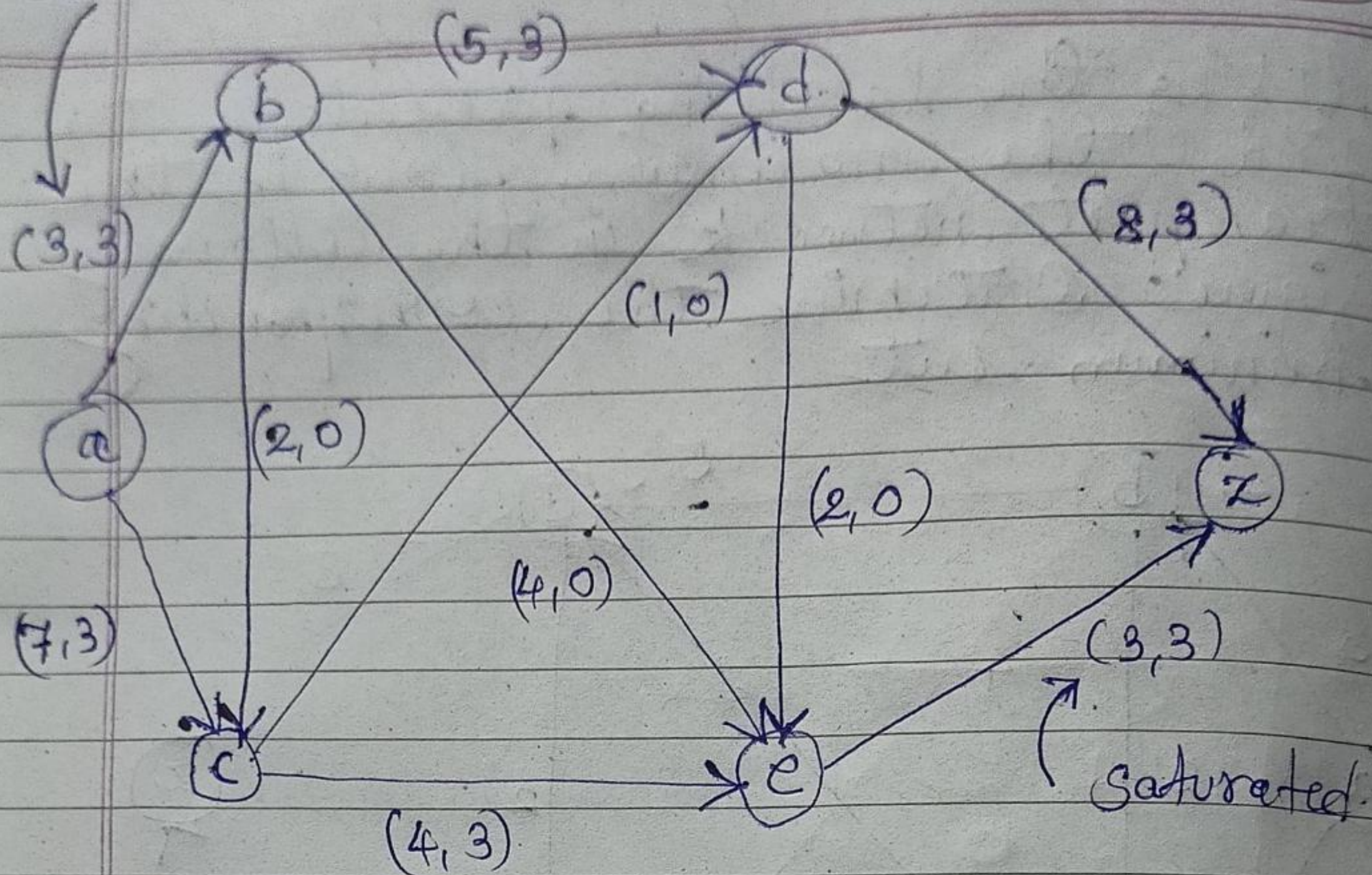
The flow of path

$a \rightarrow c \rightarrow e \rightarrow z = 3$ unit.

Step 2: Now select path 'abdz'. When we apply unit flow ~~then~~ and increment one at a time, then edge 'ab' gets saturated, when flow will reach to 5 units.

$$F_{ab} = C_{ab}$$

Saturated

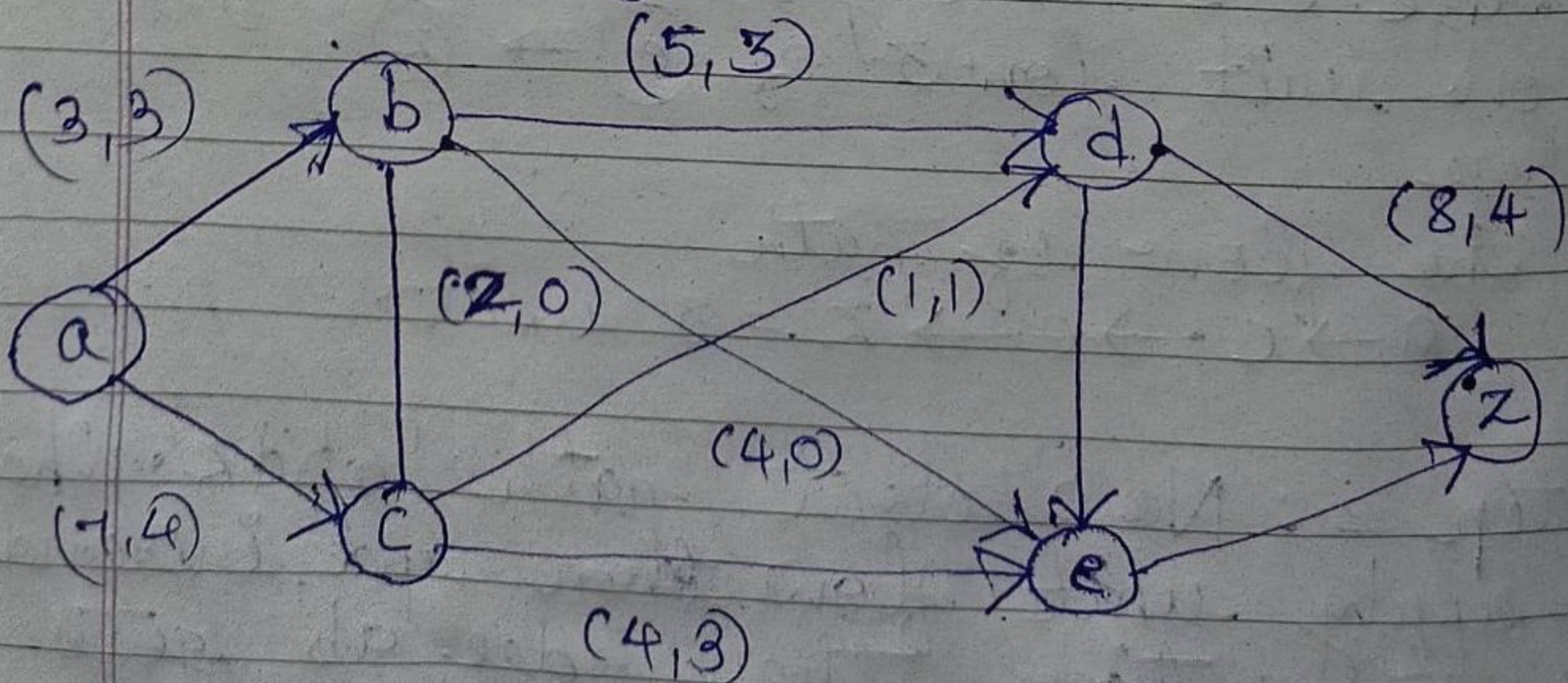


Flow of path $a \rightarrow b \rightarrow d \rightarrow z$ is 3 unit

Step 3: Now select another understand path, where (flow & capacity) and apply unit flow we get saturated path.

Path $\Rightarrow a \rightarrow c \rightarrow d \rightarrow z$

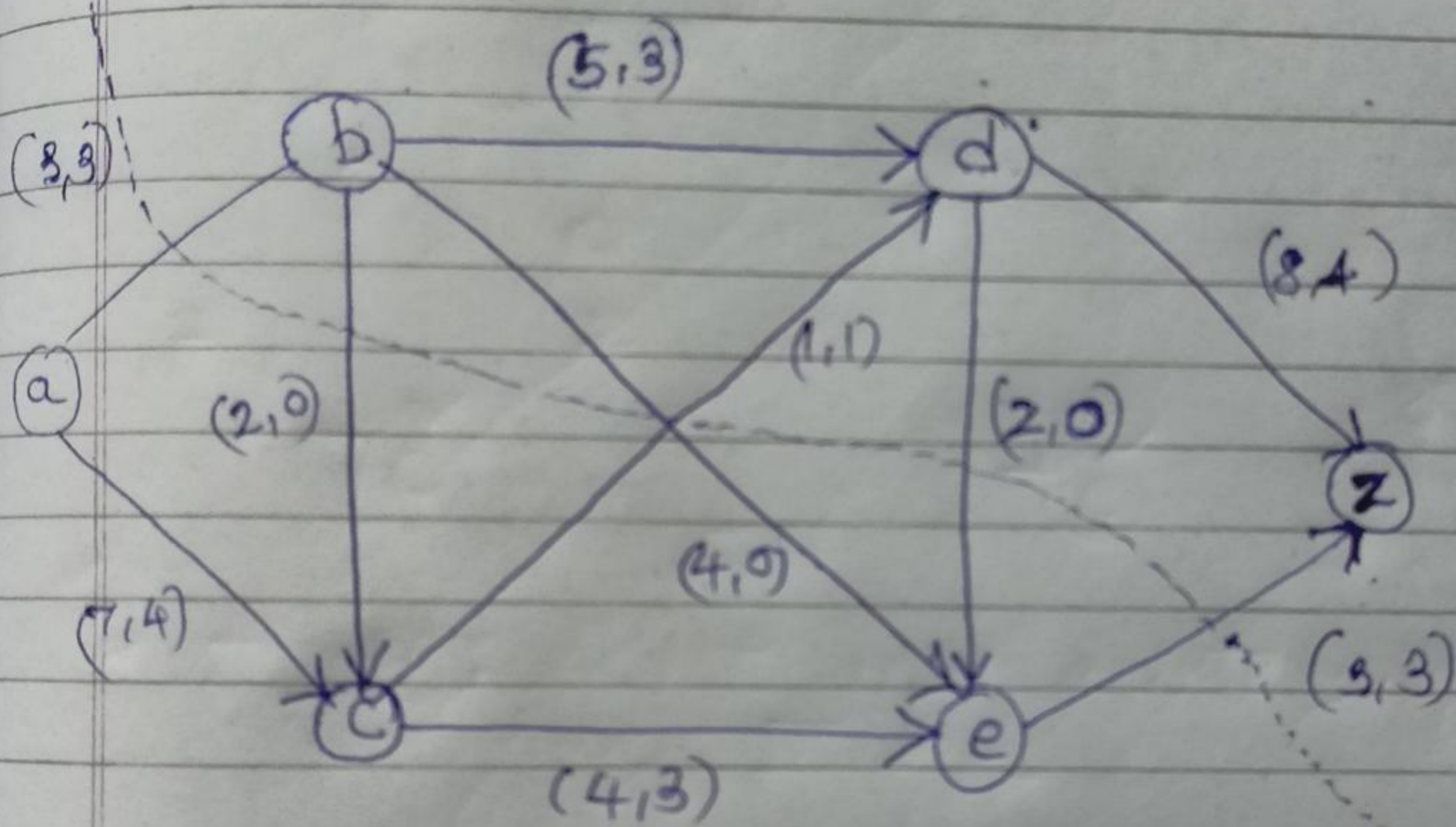
Edge "ed" get saturated when unit flow reached. to "1" unit flow of "cd" of $C_d = \text{Capacity of } cd$.



Flow of path, $a \rightarrow c \rightarrow d \rightarrow z$.
flow = 1 unit.

According to max flow - min cut theorem

Maximum flow in the network = minimum cut.



Maximum flow = $F_{ez} + F_{ab} + F_{cd} = 3 + 3 + 1 = 7$ units
in the network

Capacity of Cut = $C_{ab} + C_{ez} + C_{cd}$
 $= 3 + 1 + 3$
 $= 7$ units.

Minimum Cut = 7