Euclid's Elements

all thirteen books complete in one volume

The Thomas L. Heath Translation

Dana Densmore, Editor



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Cover design by Dana Densmore and William H. Donahue with help from Nadine Shea. Adapted from a detail in Raphael's School of Athens, the illustration focuses on a young student being shown a proof by Euclid while friends and mentors offer supportive encouragement.

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Proposition 1

On a given finite straight line to construct an equilateral triangle.

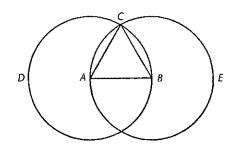
Let AB be the given finite straight line.

Thus it is required to construct an equilateral triangle on the straight line *AB*.

With centre A and distance AB let the circle BCD be described; [Post. 3]

again, with centre B and distance BA

let the circle *ACE* be described; [Post. 3] and from the point *C*, in which the circles cut one another, to the points *A*, *B* let the straight lines *CA*, *CB* be joined. [Post. 1]



Now, since the point A is the centre of the circle CDB,

AC is equal to AB.

[Def. 15]

Again, since the point *B* is the centre of the circle *CAE*, *BC* is equal to *BA*.

[Def. 15]

But CA was also proved equal to AB;

therefore each of the straight lines CA, CB is equal to AB.

And things which are equal to the same thing are also equal to one another;
[C.N. 1]

therefore CA is also equal to CB.

Therefore the three straight lines CA, AB, BC are equal to one another.

Therefore the triangle ABC is equilateral; and it has been constructed on the given finite straight line AB.

Being what it was required to do.

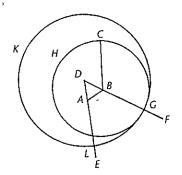
Proposition 2

To place at a given point [as an extremity]¹ a straight line equal to a given straight line.

Let *A* be the given point, and *BC* the given straight line.

Thus it is required to place at the point A [as an extremity] a straight line equal to the given straight line BC.

From the point A to the point B let the straight line AB be joined; [Post. 1] and on it let the equilateral triangle DAB be constructed. [I. 1]



^{1.} Square brackets indicate material which Heath identified as having been supplied by him, adding clarification but not literally present in the Greek text. —Ed.