Assignment 2

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Download all python codes from

https://github.com/grajanarsavva/Matrix-theory/codes

and latex-tikz codes from

https://github.com/grajanarsavva/Matrix-theory

1 Question No. 2.45

Can you construct a Rhombus ABCD with AC=6 and BD=7 ?

2 Explanation

- 1) Assume vertices of given rhombus:-Let the vertices of rhombus *ABCD* be **A,B,C** and **D**.
- 2) List out give data in form vectors :- According to given data:

$$||\mathbf{A} - \mathbf{C}|| = 6 \tag{2.0.1}$$

$$\|\mathbf{B} - \mathbf{D}\| = 7 \tag{2.0.2}$$

3) Find out two triangles of given rhombus having same base

Rhombus ABCD is made of two triangles $\triangle ABC$ and $\triangle ACD$ placed on base AC.

From $\triangle ACD$, Consider another $\triangle AOB$ and $\triangle BOD$, both are right angled triangle.

By pythagorean theorem:

$$\|\mathbf{A} - \mathbf{B}\|^2 = \|\mathbf{A} - \mathbf{O}\|^2 + \|\mathbf{O} - \mathbf{B}\|^2$$

= $(3)^2 + (3.5)^2$

= 21.25

$$\|\mathbf{A} - \mathbf{B}\| = \pm 4.6$$

Similarly

$$\|\mathbf{B} - \mathbf{C}\| = 4.6$$

$$\|\mathbf{C} - \mathbf{D}\| = 4.6$$

$$\|\mathbf{D} - \mathbf{A}\| = 4.6$$

By the property of Rhombus, Allsides of rhombus are equal. The opposite sides of rhombus are parallel.

therefore the vertices of rhombus:

$$\mathbf{O} = \begin{pmatrix} 0 \\ 0 \end{pmatrix} \tag{2.0.3}$$

$$\mathbf{A} = \begin{pmatrix} 0 \\ -4.6 \end{pmatrix} \tag{2.0.4}$$

$$\mathbf{B} = \begin{pmatrix} 3.5\\0 \end{pmatrix} \tag{2.0.5}$$

$$\mathbf{C} = \begin{pmatrix} 4.6 \\ 0 \end{pmatrix} \tag{2.0.6}$$

$$\mathbf{D} = \begin{pmatrix} 0 \\ -3.5 \end{pmatrix} \tag{2.0.7}$$

Plot the Rhombus ABCD is as follows:

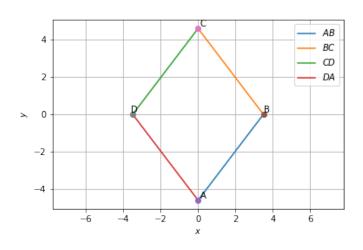


Fig. 2.1: Rhombus ABCD