

AI1103 - Assignment 1

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Download all python codes from

<https://github.com/rajasekhar156/AI1103/blob/main/assignment--1.py> \\ \\

and latex-tikz codes from

<https://github.com/rajasekhar156/AI1103/edit/main/assignment-1.tex> \\ \\ \\

QUESTION:

A manufacturer has three machine operators A, B and C. The first operator A produces 1% defective items, where as the other two operators B and C produce 5% and 7% defective items respectively. A is on the job for 50% of the time, B is on the job for 30% of the time and C is on the job for 20% of the time. A defective item is produced, what is the probability that it was produced by A?

ANSWER:

Let $X \in \{0, 1, 2\}$ be the random variable denoting that item was produced by operator A when $X=0$, $X=1$ denoting that item was produced by operator B, $X=2$ denoting that item was produced by operator C, and random variable $Y \in \{0, 1\}$ be the random variable denoting that item produced was defective when $Y=1$.

From conditional probability we say that

$$\begin{aligned} \Pr(X = 0/Y = 1) &= \frac{\Pr(Y = 1/X = 0) \Pr(X = 0)}{\sum_{i=0}^2 \Pr(Y = 1/X = i) \Pr(X = i)} \\ &= \frac{(0.01)(0.5)}{(0.01)(0.5) + (0.05)(0.3) + (0.07)(0.2)} \\ &= \frac{5}{34} \\ &= 0.147058 \end{aligned}$$

Probability that defective item is produced by operator A is 0.147058

$$\Pr(X = 0) = 0.5 \quad (0.0.1)$$

$$\Pr(X = 1) = 0.3 \quad (0.0.2)$$

$$\Pr(X = 2) = 0.2 \quad (0.0.3)$$

$$\Pr(Y = 1/X = 0) = 0.01 \quad (0.0.4)$$

$$\Pr(Y = 1/X = 1) = 0.05 \quad (0.0.5)$$

$$\Pr(Y = 1/X = 2) = 0.07 \quad (0.0.6)$$