AI1103 - Assignment 3

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Download all latex-tikz codes from

https://github.com/rajasekhar156/assignment-3/blob/main/main.tex

QUESTION:

If A and B are two events and the probability $Pr(B) \neq 1$, then $\frac{Pr(A) - Pr(AB)}{1 - Pr(B)}$ equals

- 1) $Pr(A|\bar{B})$
- 2) Pr(A|B)
- 3) $Pr(\bar{A}|B)$
- 4) $Pr(\bar{A}|\bar{B})$

ANSWER:

From Laws of complimentary of Boolean algebra

$$B + \bar{B} = 1 \tag{0.0.1}$$

$$Pr(B) + Pr(\bar{B}) = 1 \qquad (0.0.2)$$

$$1 - \Pr(B) = \Pr(\bar{B}) \tag{0.0.3}$$

And also as

$$A - AB = A(1 - B) \tag{0.0.4}$$

$$A - AB = A(\bar{B}) \tag{0.0.5}$$

$$Pr(A) - Pr(AB) = Pr(A\bar{B})$$
 (0.0.6)

Truth table					
A	В	AB	\bar{B}	A-AB	$Aar{B}$
1	1	1	0	0	0
1	0	0	1	1	1
0	1	0	0	0	0
0	0	0	1	0	0

Using the above equations (0.0.3) and (0.0.6)

$$\frac{\Pr(A) - \Pr(AB)}{1 - \Pr(B)} = \frac{\Pr(A\bar{B})}{\Pr(\bar{B})}$$
(0.0.7)

$$= \Pr(A|\bar{B}) \tag{0.0.8}$$

Hence, option (1) is correct.