AI1103 - Assignment 4

I.Rajasekhar Reddy – CS20BTECH11020

Download all python codes from

https://github.com/rajasekhar156/assignment-4/ blob/main/untitled2.py

and latex-tikz codes from

https://github.com/rajasekhar156/assignment-4/ blob/main/main.tex

QUESTION:GATE 2001 (EC), Q. 1.20

The PDF of a Gaussian random variable X is given by
$$P_X(x) = \frac{1}{3\sqrt{2\pi}}e^{\frac{-(x-4)^2}{18}}$$
. The probability of the event $X = 4$ is

- 1) $\frac{1}{2}$
- 2) $\frac{1}{3\sqrt{2\pi}}$
- 3) 0

ANSWER:

Compare the given PDF function with

$$P_X(x) = \frac{1}{\sigma \sqrt{2\pi}} e^{\frac{-(x-\mu)^2}{2\sigma^2}}$$
(0.0.1)

$$P_X(x) = \frac{1}{3\sqrt{2\pi}}e^{\frac{-(x-4)^2}{18}}$$
(0.0.2)

We get σ and μ as

$$\sigma = 3 \tag{0.0.3}$$

$$\mu = 4 \tag{0.0.4}$$

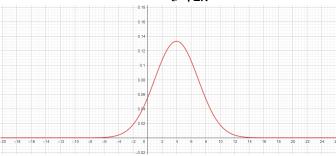
The probability of the event X = 4 is

$$\Pr(X=4) = \frac{1}{3\sqrt{2\pi}}e^{\frac{-(4-4)^2}{18}} \tag{0.0.5}$$

$$= \frac{1}{3\sqrt{2\pi}}e^{0}$$
 (0.0.6)
$$= \frac{1}{3\sqrt{2\pi}}$$
 (0.0.7)

$$=\frac{1}{3\sqrt{2\pi}}\tag{0.0.7}$$

Hence the probability is $\frac{1}{3\sqrt{2\pi}}$.



GraphofPDF function.