

AI1103 - Assignment 4

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Download all python codes from

<https://github.com/rajasekhar156/assignment-4/blob/main/untitled2.py>

and latex-tikz codes from

<https://github.com/rajasekhar156/assignment-4/blob/main/main.tex>

QUESTION:GATE 2001 (EC), Q. 1.20

The PDF of a Gaussian random variable X is given

by $P_X(x) = \frac{1}{3\sqrt{2\pi}} e^{\frac{-(x-4)^2}{18}}$. The probability of the event $X = 4$ is

- 1) $\frac{1}{2}$
- 2) $\frac{1}{3\sqrt{2\pi}}$
- 3) 0
- 4) $\frac{1}{4}$

ANSWER:

Compare the given PDF function with

$$P_X(x) = \frac{1}{\sigma\sqrt{2\pi}} e^{\frac{-(x-\mu)^2}{2\sigma^2}} \quad (0.0.1)$$

$$P_X(x) = \frac{1}{3\sqrt{2\pi}} e^{\frac{-(x-4)^2}{18}} \quad (0.0.2)$$

We get σ and μ as

$$\sigma = 3 \quad (0.0.3)$$

$$\mu = 4 \quad (0.0.4)$$

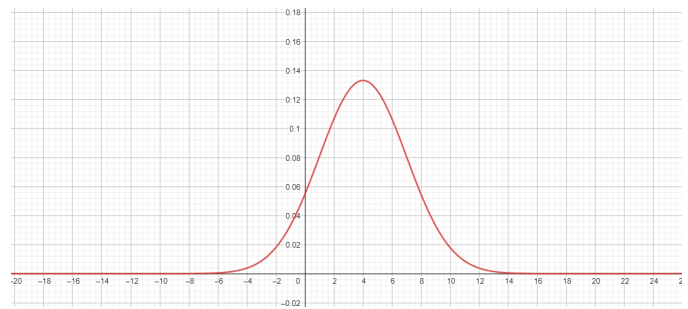
The probability of the event $X = 4$ is

$$\Pr(X = 4) = \frac{1}{3\sqrt{2\pi}} e^{\frac{-(4-4)^2}{18}} \quad (0.0.5)$$

$$= \frac{1}{3\sqrt{2\pi}} e^0 \quad (0.0.6)$$

$$= \frac{1}{3\sqrt{2\pi}} \quad (0.0.7)$$

Hence the probability is $\frac{1}{3\sqrt{2\pi}}$.



Graph of PDF function.