## Decision tree classifier

Prof. E.P.Ephzibah

## General Approach to Classification

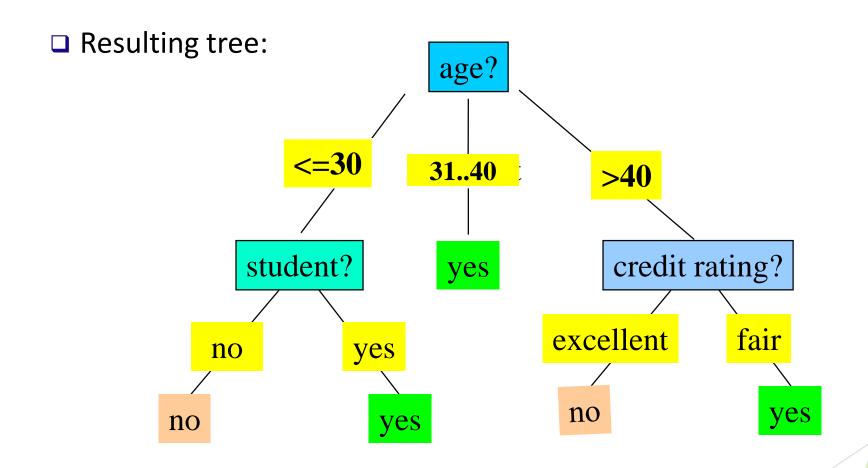
- ► The data classification process:
- ▶ (a) Learning: Training data are analyzed by a classification algorithm. The learned model or classifier is represented in the form of classification rules (if -then rules).
- ▶ (b) <u>Classification:</u> Test data are used to estimate the accuracy of the classification rules. If the accuracy is considered acceptable, the rules can be applied to the classification of new data tuples.

#### Decision Tree Induction: An Example

□Training data set: Buys\_computer

age	income	student	credit_rating	buys_computer
<=30	high	no	fair	no
<=30	high	no	excellent	no
3140	high	no	fair	yes
>40	medium	no	fair	yes
>40	low	yes	fair	yes
>40	low	yes	excellent	no
3140	low	yes	excellent	yes
<=30	medium	no	fair	no
<=30	low	yes	fair	yes
>40	medium	yes	fair	yes
<=30	medium	yes	excellent	yes
3140	medium	no	excellent	yes
3140	high	yes	fair	yes
>40	medium	no	excellent	no

## Decision Tree Induction: An Example



## Algorithm for Decision Tree Induction

- Basic algorithm (a greedy algorithm)
  - ► Tree is constructed in a top-down recursive divide-andconquer manner
  - ► At start, all the training examples are at the root
  - ► Attributes are categorical (if continuous-valued, they are discretized in advance)
  - Examples are partitioned recursively based on selected attributes
  - ► Test attributes are selected on the basis of a heuristic or statistical measure (e.g., information gain)
- Conditions for stopping partitioning
  - ► All samples for a given node belong to the same class
  - ► There are no remaining attributes for further partitioning majority voting is employed for classifying the leaf
  - ► There are no samples left

# Attribute Selection Measure: Information Gain (ID3)

- ID3 uses information gain as its attribute selection measure.
- Select the attribute with the highest information gain
- Let  $p_i$  be the probability that an arbitrary tuple in D belongs to class  $C_i$ , estimated by  $|C_{i,D}|/|D|$  Info $(D) = -\sum_{i}^{m} p_i \log_2(p_i)$
- **Expected information (entropy)** needed to classify a tuple in D:

$$Info_A(D) = \sum_{j=1}^{\nu} \frac{|D_j|}{|D|} \times Info(D_j)$$

Information needed (after using A to split D into v partitions) to classify D:

$$Gain(A) = Info(D) - Info_A(D)$$

The information gained by branching on attribute A

#### Attribute Selection: Information Gain

- Class P: buys\_computer = "yes"
- Class N: buys\_computer = "no"

$$Info(D) = -\sum_{i=1}^{m} p_i \log_2(p_i)$$

$$Info(D) = I(9,5) = -\frac{9}{14} \log_2(\frac{9}{14}) - \frac{5}{14} \log_2(\frac{5}{14}) = 0.940$$

#### Attribute Selection: Information Gain

age	p <sub>i</sub>	n <sub>i</sub>	I(p <sub>i</sub> , n <sub>i</sub> )
<=30	2	3	0.971
3140	4	0	0
>40	3	2	0.971

$$Info_{age}(D) = \frac{5}{14}I(2,3) + \frac{4}{14}I(4,0) + \frac{5}{14}I(3,2) = 0.694$$

$$\frac{5}{14}I(2,3)$$
 means "age <=30" has 5 out of 14 samples, with 2 yes'es and 3 no's. Hence

$$Gain(age) = Info(D) - Info_{age}(D) = 0.246$$

Similarly,

$$Gain(income) = 0.029$$
  
 $Gain(student) = 0.151$   
 $Gain(credit_rating) = 0.048$ 

## Computing Information-Gain for Continuous-Valued Attributes

- Let attribute A be a continuous-valued attribute
- ► Must determine the *best split point* for A
  - ► Sort the value A in increasing order
  - ► Typically, the midpoint between each pair of adjacent values is considered as a possible *split point* 
    - $\triangleright$   $(a_i+a_{i+1})/2$  is the midpoint between the values of  $a_i$  and  $a_{i+1}$
  - ► The point with the *minimum expected information* requirement for A is selected as the split-point for A
- ► Split:
  - D1 is the set of tuples in D satisfying A ≤ split-point, and D2 is the set of tuples in D satisfying A > split-point

## Gain Ratio for Attribute Selection (C4.5)

- Information gain measure is biased towards attributes with a large number of values
- ► C4.5 (a successor of ID3) uses gain ratio to overcome the problem (normalization to information gain)

$$SplitInfo_A(D) = -\sum_{j=1}^{\nu} \frac{|D_j|}{|D|} \times \log_2(\frac{|D_j|}{|D|})$$

- ► GainRatio(A) = Gain(A)/SplitInfo(A)
- EX.  $SplitInfo_{income}(D) = -\frac{4}{14} \times \log_2(\frac{4}{14}) \frac{6}{14} \times \log_2(\frac{6}{14}) \frac{4}{14} \times \log_2(\frac{4}{14}) = 1.557$ 
  - gain\_ratio(income) = 0.029/1.557 = 0.019
- ► The attribute with the maximum gain ratio is selected as the splitting attribute

## Gini Index (CART, IBM IntelligentMiner)

▶ If a data set *D* contains examples from *n* classes, gini index, *gini(D)* is defined as

 $\begin{array}{c}
\text{d as} \\
gini(D) = 1 - \sum_{j=1}^{n} p_j^2
\end{array}$ 

where  $p_j$  is the relative frequency of class j in D

▶ If a data set D is split on A into two subsets  $D_1$  and  $D_2$ , the *gini* index *gini*(D) is defined as

 $gini_A(D) = \frac{|D_1|}{|D|}gini(D_1) + \frac{|D_2|}{|D|}gini(D_2)$ • Reduction in Impurity:

 $\Delta gini(A) = gini(D) - gini_{A}(D)$ The attribute provides the smallest  $gini_{split}(D)$  (or the largest reduction in impurity) is chosen to split the node (need to enumerate all the possible splitting points for each attribute)

## Computation of Gini Index

Ex. D has 9 tuples in buys\_computer = "yes" and 5 in "no"

$$gini(D) = 1 - \left(\frac{9}{14}\right)^2 - \left(\frac{5}{14}\right)^2 = 0.459$$

Suppose the attribute income partitions D into 10 in  $D_1$ : {low,

medium} and 4 in D<sub>2</sub>  $gini_{income \in \{low, medium\}}(D) = \left(\frac{10}{14}\right)Gini(D_1) + \left(\frac{4}{14}\right)Gini(D_2)$ 

$$= \frac{10}{14} \left( 1 - \left( \frac{7}{10} \right)^2 - \left( \frac{3}{10} \right)^2 \right) + \frac{4}{14} \left( 1 - \left( \frac{2}{4} \right)^2 - \left( \frac{2}{4} \right)^2 \right)$$

$$= 0.443$$

$$= Gini_{income} \in \{high\}(D).$$

Gini<sub>{low,high}</sub> is 0.458; Gini<sub>{medium,high}</sub> is 0.450. Thus, split on the {low,medium} (and {high}) since it has the lowest Gini index

- All attributes are assumed continuous-valued
- May need other tools, e.g., clustering, to get the possible split values
- Can be modified for categorical attributes

## Comparing Attribute Selection Measures

- ▶ The three measures, in general, return good results but
  - ► Information gain:
    - biased towards multivalued attributes
  - ► Gain ratio:
    - ► tends to prefer unbalanced splits in which one partition is much smaller than the others
  - ► Gini index:
    - biased to multivalued attributes
    - ▶ has difficulty when # of classes is large
    - tends to favor tests that result in equal-sized partitions and purity in both partitions

age	income	student	Credit rating	Buys computer
<=30	high	no	fair	no
<=30	high	no	excellent	no
3140	high	no	fair	yes
>40	medium	no	fair	yes
>40	low	yes	fair	yes
>40	low	yes	excellent	no
3140	low	yes	excellent	yes
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<=30	medium	yes	excellent	yes
3140	medium	no	excellent	yes
3140	high	yes	fair	yes
>40	medium	no	excellent	no

Build a decision tree for the given training data in the table (Buy Computer data), predict the class of the following new example:

age<=30, income=medium, student=yes, credit-rating=fair

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