ASSIGNMENT 11

APPLIED COMPUTATIONAL METHODS IN MECHANICAL SCIENCES

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Answer

- Grid Independence was done by comparing rod-centre temperature at t=9s for explicit scheme. Result was 90 element grid.
- Time step was chosen as 0.01 s based on stability criteria.

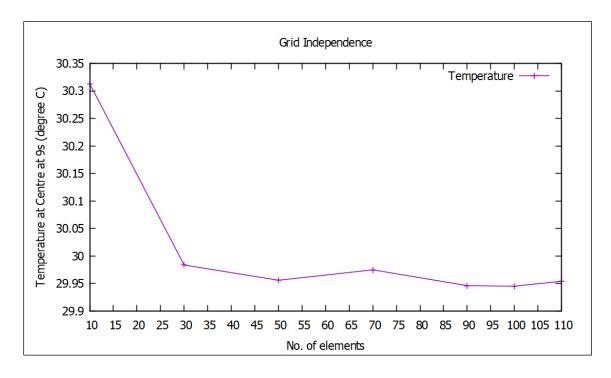
Code(C++)

```
#include<iostream>
     #include<conio.h>
     #include<fstream>
    #include<time.h>
  5 using namespace std;
  6 main()
  7
          clock_t start=clock();
  8
  9
         fstream f;
         f.open("DATA.txt",ios::out);
 10
 11
         int i, n=91, choice=1;
 12
         float 1=0.05, total_time=9, current_time=0, dx=1/(n-1), k=54, rho=7800, cp=490,
alpha=k/(rho*cp), T[n], Told[n], dt=0.01, a, b, c, diag[n-2], B[n-2], factor;
 13
         if(alpha*dt/(dx*dx)>0.5)
 14
 15
              cout<<"Improper time step";</pre>
 16
              getch();
 17
 18
 19
         for (i=1;i<n-1;++i)</pre>
 20
             T[i]=20;
 21
         T[0]=100;
 22
 23
         T[n-1]=25;
 24
         f<<"Grid\n";
 25
 26
         for (i=0; i<n; ++i)</pre>
              f<<i**dx<<" ";
 27
         f<<"\nTime=0s\n";
 28
 29
         for (i=0;i<n;++i)</pre>
              f<<T[i]<<" ";
 30
         if(choice==1) //EXPLICIT
 31
 32
          {
 33
              do
 34
 35
                   for (i=0;i<n;++i)</pre>
 36
                      Told[i]=T[i];
 37
                   current_time+=dt;
 38
                   for (i=1; i<n-1;++i)
                       T[i]=alpha*dt/(dx*dx)*(Told[i+1]-2*Told[i]+Told[i-1])+Told[i];
 39
 40
                   f<<"\nTime="<<current time<<"s\n";
                   for (i=0;i<n;++i)</pre>
 41
                       f<<T[i]<<" ";
 42
 43
              }while (current time < total time);</pre>
 44
 45
         else if(choice==2) //IMPLICIT
 46
 47
              a=-alpha*dt/(dx*dx);
 48
              b=-2*a+1;
 49
              c=a;
 50
              do
 51
 52
                   for (i=0;i<n;++i)</pre>
 53
                       Told[i]=T[i];
 54
                   current time+=dt;
 55
                   for (i=0; i< n-2; ++i)
 56
                       diag[i]=b;
```

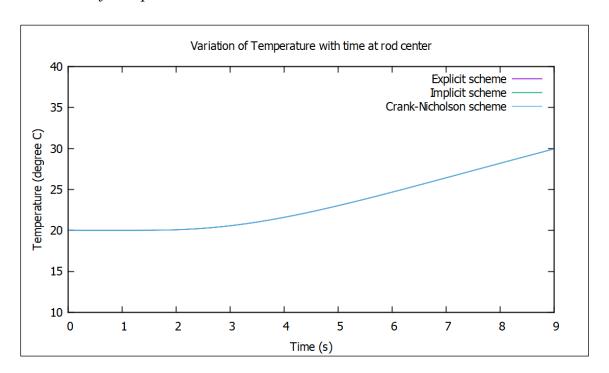
```
57
                   B[0] = Told[1] - c * T[0];
 58
                   B[n-3] = Told[n-2] - a * T[n-1];
 59
                   for (i=1;i<n-3;++i)</pre>
 60
                       B[i]=Told[i+1];
 61
                   for (i=1;i<n-2;++i)</pre>
 62
 63
                       factor=c/diag[i-1];
 64
                        diag[i]=diag[i]-factor*a;
                       B[i]=B[i]-factor*B[i-1];
 6.5
 66
 67
                   T[n-2]=B[n-3]/diag[n-3];
 68
                   for (i=n-3; i>0; --i)
 69
                       T[i] = (B[i-1]-a*T[i+1])/diag[i-1];
                   f<<"\nTime="<<current_time<<"s\n";
 70
 71
                   for (i=0;i<n;++i)</pre>
 72
                        f<<T[i]<<" ";
 73
               }while(current time<total time);</pre>
 74
 75
          else if(choice==3) //CRANK-NICOLSON SCHEME
 76
              a=-alpha*dt/(2*dx*dx);
 77
 78
              b=-2*a+1;
 79
              c=a;
 80
              do
 81
                   for (i=0;i<n;++i)</pre>
 82
 83
                       Told[i]=T[i];
 84
                   current_time+=dt;
 85
                   for (i=0; i< n-2; ++i)
 86
                       diag[i]=b;
                   B[0]=Told[1]-a*Told[2]-(b-1)*Told[1]-2*c*Told[0];
 87
 88
                   B[n-3]=Told[n-2]-2*a*Told[n-1]-(b-1)*Told[n-2]-c*Told[n-3];
 89
                   for (i=1;i<n-3;++i)</pre>
 90
                       B[i] = Told[i+1] - a*Told[i+2] - (b-1)*Told[i+1] - c*Told[i];
 91
                   for (i=1;i<n-2;++i)</pre>
 92
 93
                        factor=c/diag[i-1];
 94
                       diag[i]=diag[i]-factor*a;
 95
                       B[i]=B[i]-factor*B[i-1];
 96
 97
                   T[n-2]=B[n-3]/diag[n-3];
 98
                   for (i=n-3;i>0;--i)
 99
                       T[i] = (B[i-1]-a*T[i+1])/diag[i-1];
                   f<<"\nTime="<<current_time<<"s\n";
100
101
                   for (i=0;i<n;++i)</pre>
                       f<<T[i]<<" ";
102
103
               }while(current time<total time);</pre>
104
105
          clock t stop=clock();
106
          double timespent = (double) (stop-start) / (double) CLOCKS PER SEC;
          cout<<"\nCPU Time:"<<timespent<<" seconds";</pre>
107
108 }
```

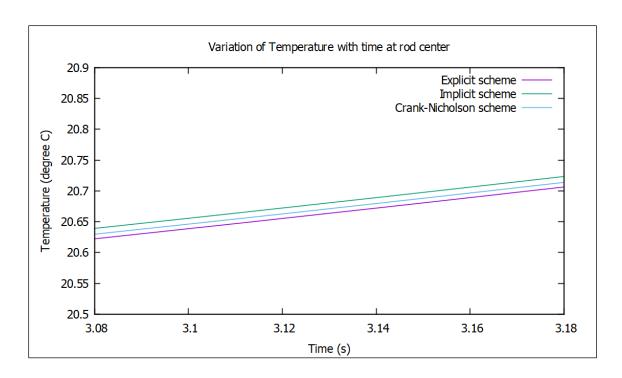
Output

Grid Independence Study: No. of elements = 90



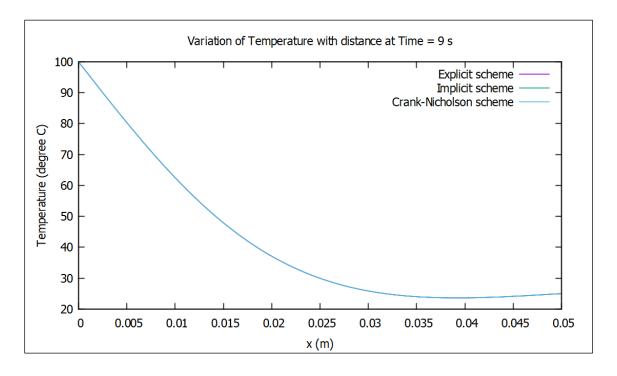
Variation of Temperature with time at rod centre

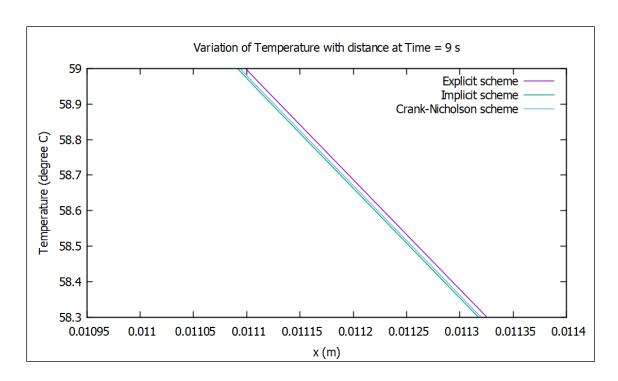




Observation: All schemes seem to give approximately the same answer.

Variation of Temperature along length of rod at 9 s





Observation: Again, all schemes seem to give approximately the same values. The zoomed graph shows that Implicit and Crank-Nicholson are very close compared to explicit with other schemes. This maybe due to usage of all previous time-step values in Explicit in contrast to the other schemes. A few nodes have temperatures below 25°C since all interior nodes were initialized at 20°C and only 9s has passed. When steady state is reached, all interior node temperatures will be above 25°C as expected.

Computational Time taken for different schemes

Scheme	Time (seconds)
Explicit	0.324
Implicit	0.326
Crank-Nicholson	0.329

Observation: Crank-Nicholson takes largest time and Explicit is the quickest since it doesn't involve TDMA.