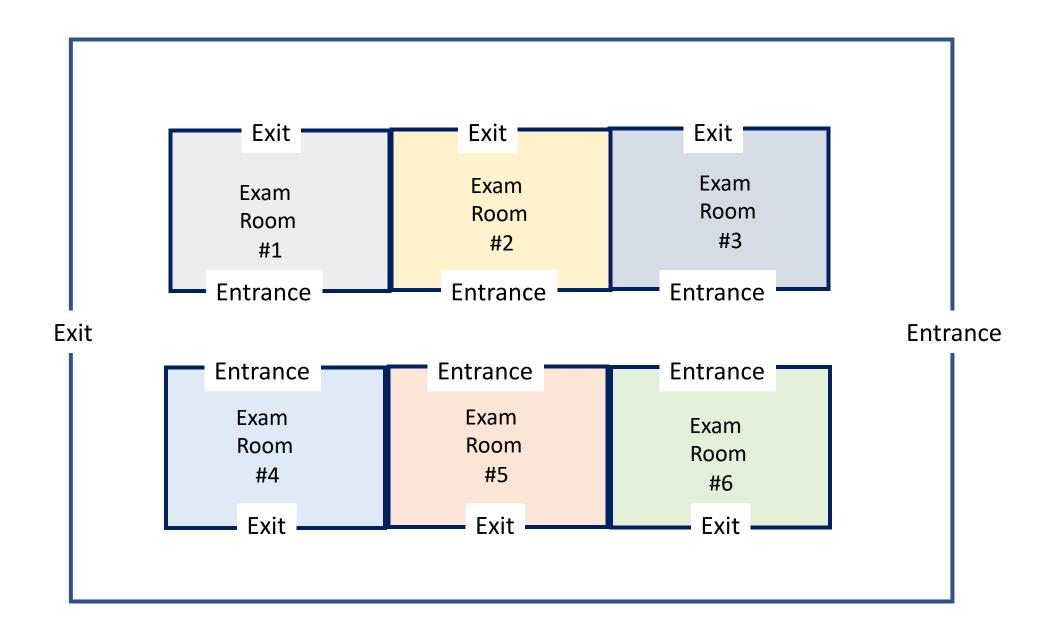
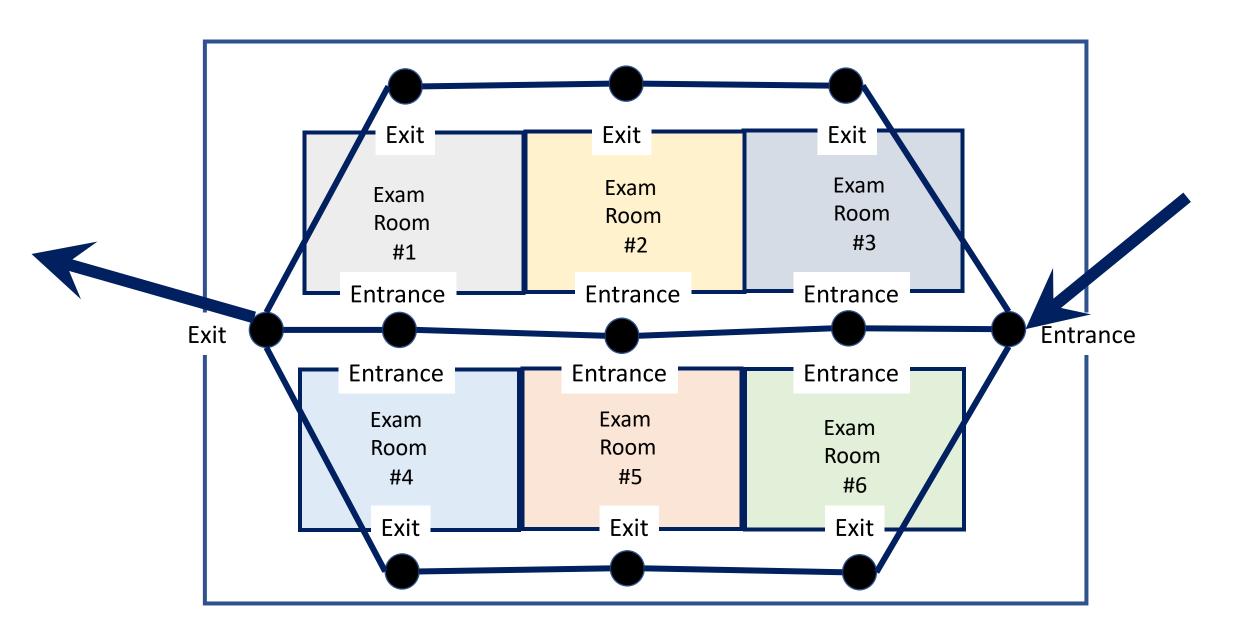
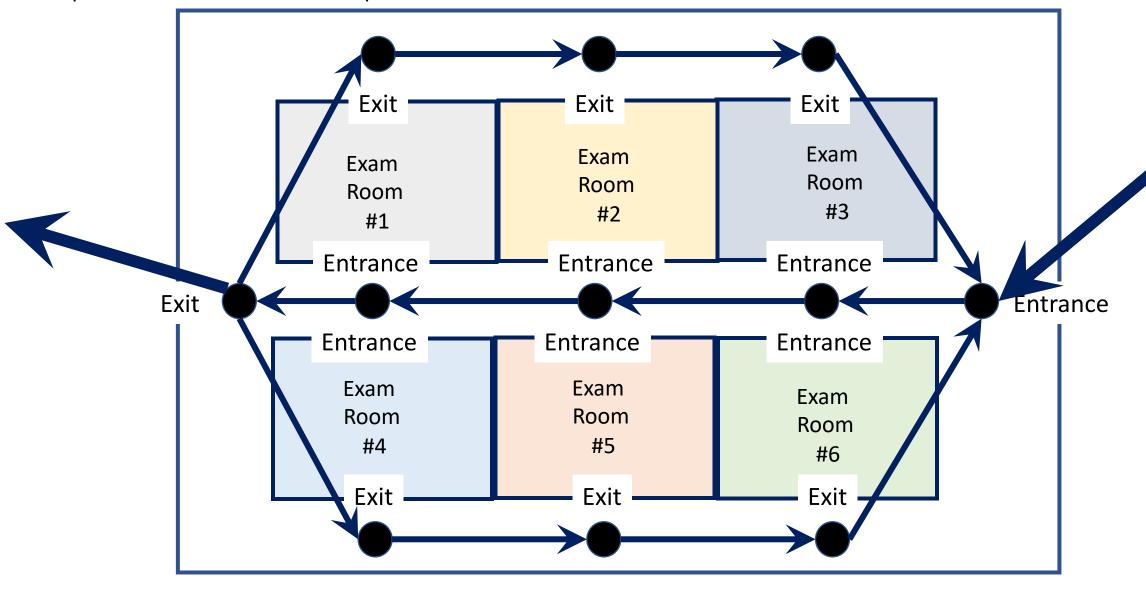
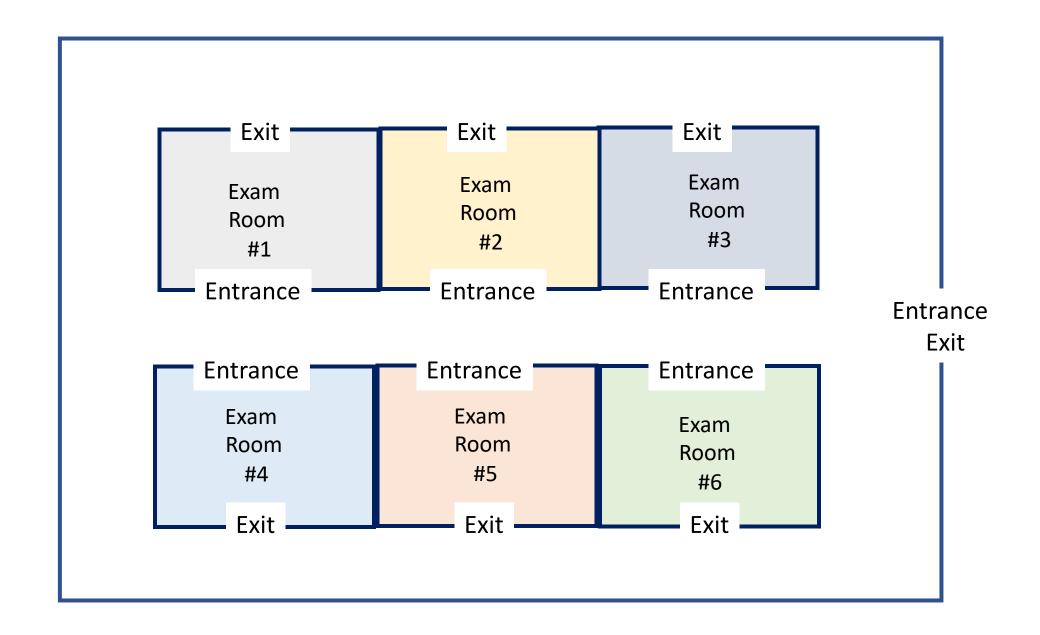
# Project – Part I



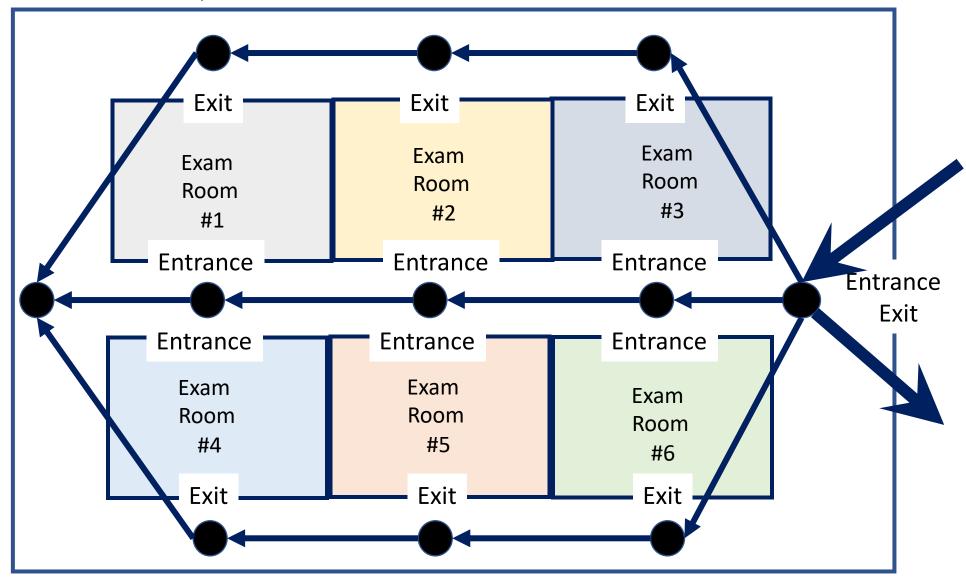


#### One possible solution: it is not unique



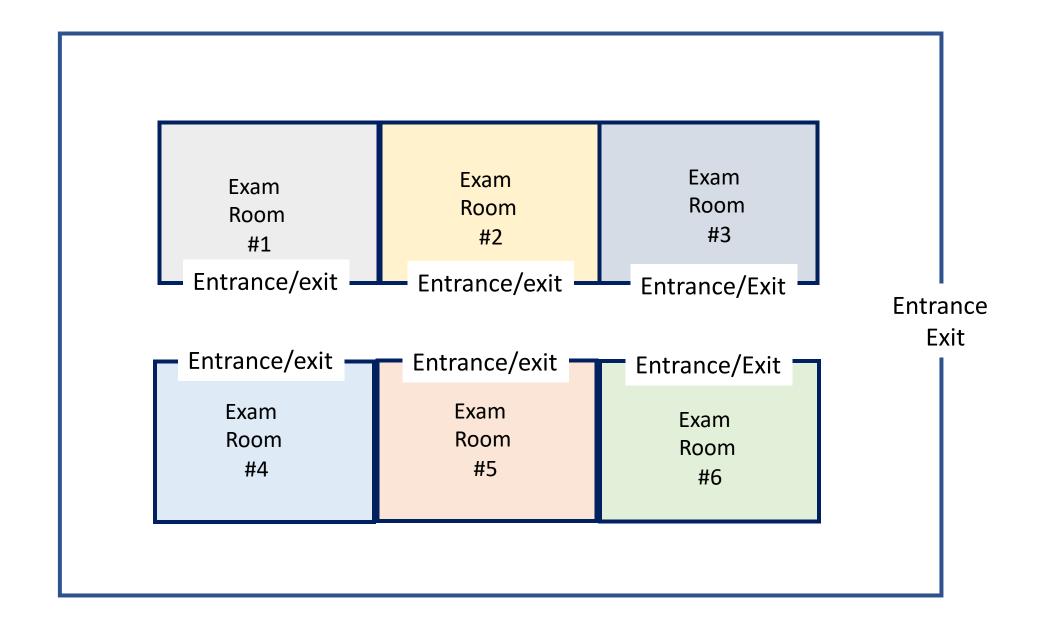


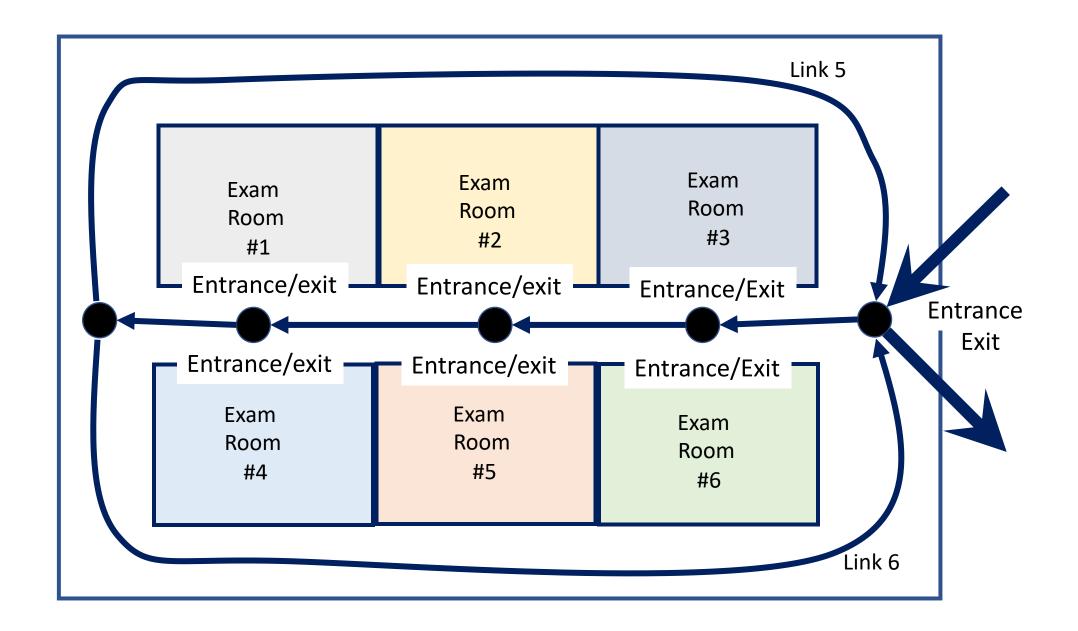
#### One possible solution: it is not unique

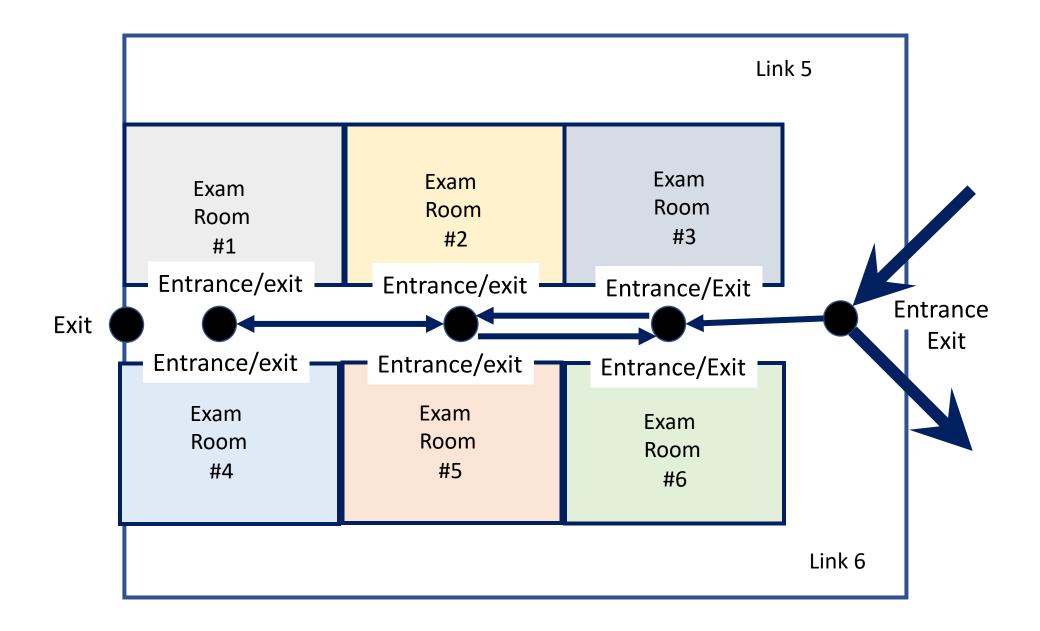


#### Comments

- You can see different link directions on slides 5 and 2: both are valid, but one is better than the other one.
- How can you make sure you will get solution of slide 2 rather than the solution of slide 5?



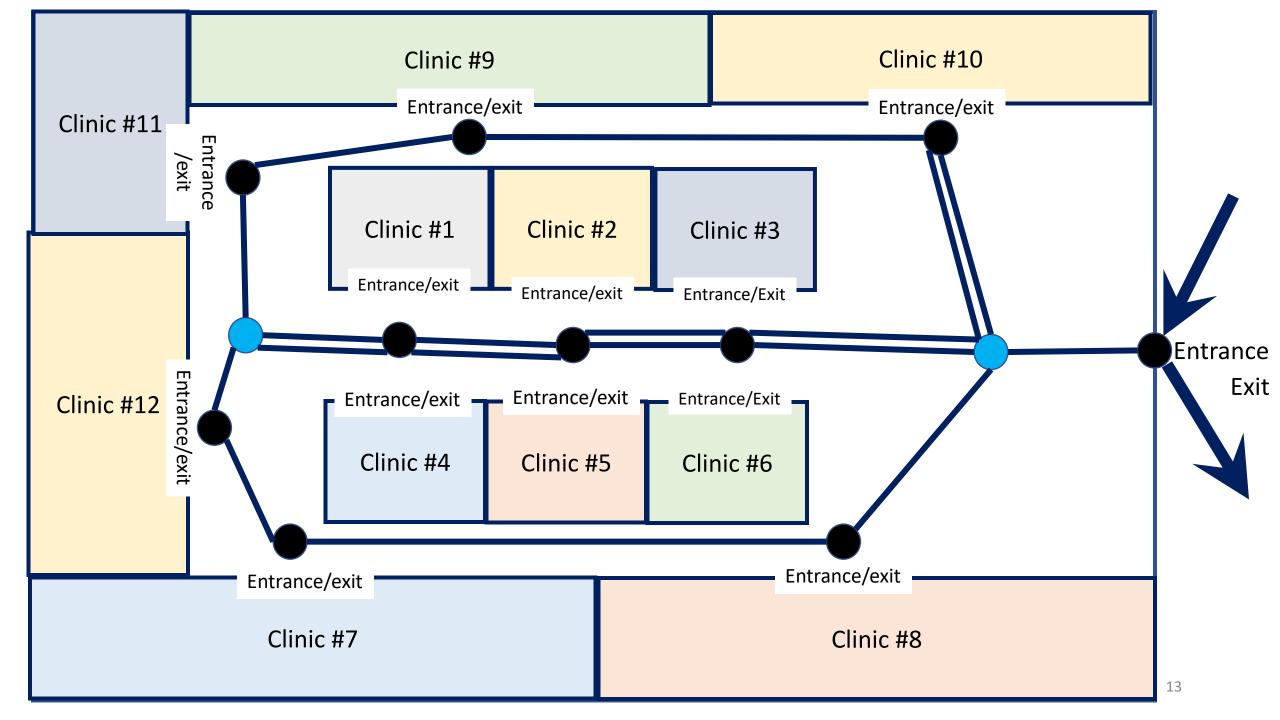




#### Comments

• What is the interest of keeping both links 5 and 6?

# Project – Part II



### Paper #1

ARTICLE

#### Finding paths with minimum shared edges



Authors: Masoud T. Omran, Jörg-Rüdiger Sack, Hamid Zarrabi-Zadeh Authors Info & Claims

COCOON'11: Proceedings of the 17th annual international conference on Computing and combinatorics • August 2011

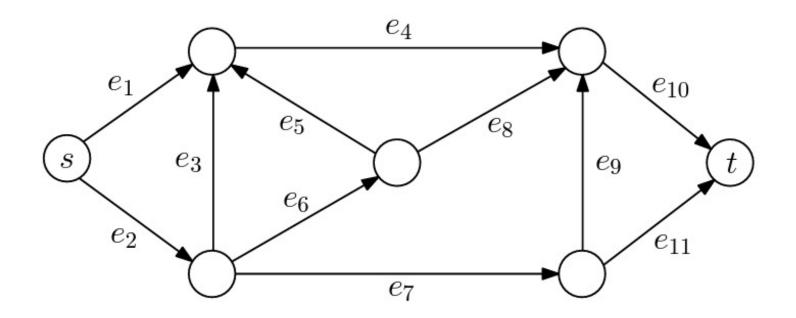
• Pages 567-578

#### Shared Link

• Given a graph G, two special nodes  $v_{SRC}$  and  $v_{DST}$  in G, and a number k, find k paths from  $v_{SRC}$  to  $v_{DST}$  in G so as to minimize the number of links shared among the paths.

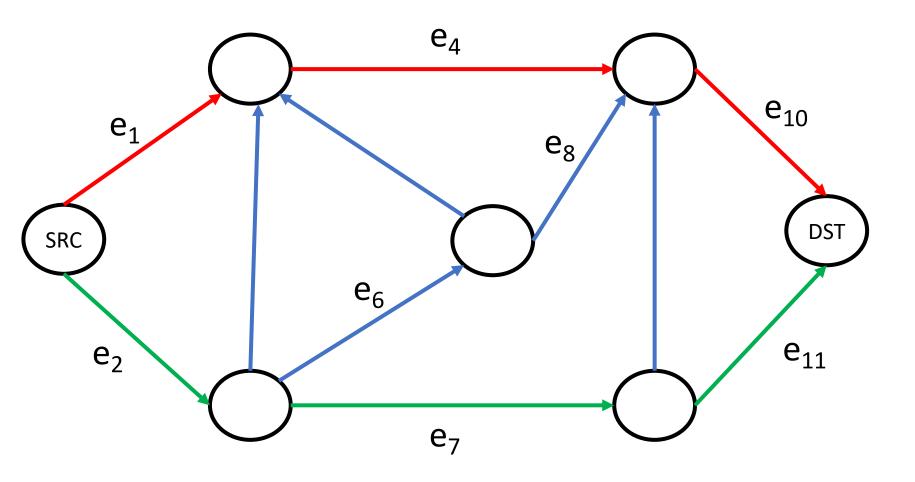
2022-03-10 15

## A graph G with six possible (s,t)-paths, denoted by $\pi_1$ to $\pi_6$



$$\pi_{1} = \langle e_{1}, e_{4}, e_{10} \rangle 
\pi_{2} = \langle e_{2}, e_{7}, e_{11} \rangle 
\pi_{3} = \langle e_{2}, e_{6}, e_{8}, e_{10} \rangle 
\pi_{4} = \langle e_{2}, e_{3}, e_{4}, e_{10} \rangle 
\pi_{5} = \langle e_{2}, e_{7}, e_{9}, e_{10} \rangle 
\pi_{6} = \langle e_{2}, e_{6}, e_{5}, e_{4}, e_{10} \rangle$$

## A graph G with six possible (s,t)-paths, denoted by $\pi_1$ to $\pi_6$



$$\pi_1 = (e_1, e_4, e_{10})$$
 $\pi_2 = (e_2, e_7, e_{11})$ 
 $\pi_6 = (e_2, e_6, e_8, e_{10})$ 
2 shared links

### Paper #2



#### Discrete Applied Mathematics

Volume 116, Issue 3, 15 February 2002, Pages 271-278



Note

### A note on orientations of mixed graphs

Esther M. Arkin <sup>1, a</sup> ○ ☑, Refael Hassin <sup>b</sup> ☑

### Concept of essential edge

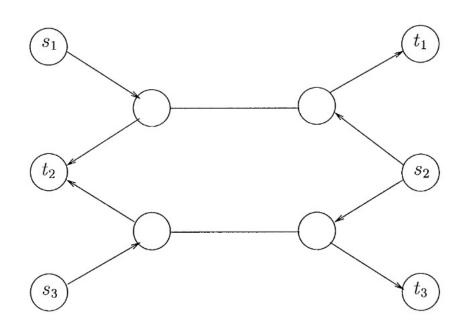


Fig. 2. A graph with no P-orientation and no essential edge.

- In the project: use essential edge for "alternating" edge, i.e., edge used in both directions.
- Since edge cannot be used in both directions at any given time, it slows down the circulation of people in the corridor

### Maximize throughput

- General definition
  - Throughput = rate of production or the rate at which something is processed.
- Often used in the context of networking
  - Rate of successful messages or packets delivery over a communication channel.
- In the context of the project
  - Number of people reaching their destination per time unit

### Maximizing the throughput

- Minimize the number of link sharing as they correspond to merging flows
- Minimize the number of edges with no fixed orientation
- Example of next slide
  - Blue edges are alternating edges

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