

Please show all your work. Answers without supporting comments will not be given credit.

1. Perform four iterations of the Newton's method to solve the following system of equation

$$\begin{aligned}x^2 + xy + y^2 &= 7 \\ x^3 + y^3 &= 9\end{aligned}$$

Take the initial values $x_0 = 1.5, y_0 = 0.5$.

Exact solution is $x = 2, y = 1$.

2. Solve the following system of equations by using Jacobi iteration method

$$\begin{aligned}4x_1 + x_2 + x_4 &= 1 \\ x_1 + 4x_2 + x_3 &= -2 \\ x_2 + 4x_3 + x_4 &= 2 \\ x_1 + x_3 + 4x_4 &= -2\end{aligned}$$

Initialization $X_0 = (0, 0, 0, 0)^T$. Perform four iterations.

3. Solve the following system of linear equations using Gaussian Elimination method

$$\begin{aligned}10x_1 - x_2 + 2x_3 &= 4 \\ x_1 + 10x_2 - x_3 &= 3 \\ 2x_1 + 3x_2 + 20x_3 &= 7\end{aligned}$$

Solutions : $x_1 = 0.375, x_2 = 0.289, x_3 = 0.269$.