

Please show all your work. Answers without supporting comments will not be given credit.

1. (a) Determine the piecewise quadratic of piecewise cubic interpolating polynomials for the function

$$f(x) = \frac{1}{\sqrt{1+x^2}}$$

with nodes at  $-\frac{3}{2}, -1, -\frac{1}{2}, 0, \frac{1}{2}, \frac{3}{2}$ .

- (b) Obtain also a divided difference interpolating polynomial for the above data.
- (c) Find the approximate value of  $f(\frac{-1}{4})$  and by using the above obtained polynomials.
- (d) Find the exact value of  $\frac{-1}{4}$  and  $\frac{3}{4}$ .
- (e) Compare the above three polynomials.
- (f) Which one is giving more accurate result?