## Sum of Natural Numbers

How does the formula 
$$n * (n + 1) / 2$$
 work?  
 $S_n = 1 + 2 + 3 + 4 + \dots + n$   
 $S_n = n + (n - 1) + (n - 2) + (n - 3) + \dots + 1$   
 $2S_n = (n + 1) + (n + 1) + (n + 1) + \dots + (n + 1)$   
 $2S_n = n * (n + 1)$   
 $3S_n = n * (n + 1) / 2$