# Stack (abstract data type)

In computer science, a **stack** is an <u>abstract data type</u> that serves as a collection of elements, with two main principal operations:

- Push, which adds an element to the collection, and
- **Pop**, which removes the most recently added element that was not yet removed.

The order in which elements come off a stack gives rise to its alternative name, **LIFO** (**last in, first out**). Additionally, a peek operation may give access to the top without modifying the stack. The name "stack" for this type of structure comes from the analogy to a set of physical items stacked on top of each other. This structure makes it easy to take an item off the top of the stack, while getting to an item deeper in the stack may require taking off multiple other items first. [2]

Considered as a <u>linear data structure</u>, or more abstractly a sequential collection, the push and pop operations occur only at one end of the structure, referred to as the *top* of the stack. This data structure makes it possible to implement a stack as a singly linked list and a pointer to

the top element. A stack may be implemented to have a bounded capacity. If the stack is full and does not contain enough space to accept an entity to be pushed, the stack is then considered to be in an <u>overflow</u> state. The pop operation removes an item from the top of the stack.

A stack is needed to implement <u>depth-first</u> <u>search</u>.

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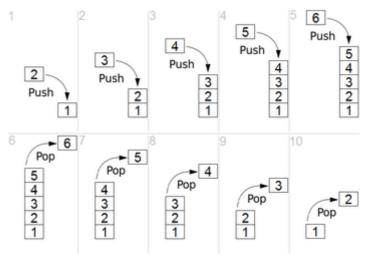
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Similar to a stack of plates, adding or removing is only possible at the top.



Simple representation of a stack runtime with *push* and *pop* operations.

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# History

Stacks entered the computer science literature in 1946, when Alan M. Turing used the terms "bury" and "unbury" as a means of calling and returning from subroutines.  $\frac{[3][4]}{Subroutines}$  had already been implemented in Konrad Zuse's Z4 in 1945.

Klaus Samelson and Friedrich L. Bauer of Technical University Munich proposed the idea of a stack in  $1955^{[5][6]}$  and filed a patent in  $1957.^{[7][8][9][10]}$  In March 1988, by which time Samelson was deceased, Bauer received the IEEE Computer Pioneer Award for the invention of the stack principle. Similar concepts were developed, independently, by Charles Leonard Hamblin in the first half of  $1954^{[12]}$  and by Wilhelm Kämmerer in  $1958.^{[13][14]}$ 

Stacks are often described using the analogy of a spring-loaded stack of plates in a cafeteria. [15][2][16] Clean plates are placed on top of the stack, pushing down any already there. When a plate is removed from the stack, the one below it pops up to become the new top plate.

# **Non-essential operations**

In many implementations, a stack has more operations than the essential "push" and "pop" operations. An example of a non-essential operation is "top of stack", or "peek", which observes the top element without removing it from the stack. [17] This could be done with a "pop" followed by a "push" to return the same data to the stack, so it is not considered an essential operation. If the stack is empty, an underflow condition will occur upon execution of either the "stack top" or "pop" operations. Also, implementations often have a function which just returns whether the stack is empty.

# Software stacks

# **Implementation**

A stack can be easily implemented either through an <u>array</u> or a <u>linked list</u>. What identifies the data structure as a stack, in either case, is not the implementation but the interface: the user is only allowed to pop or push items onto the array or linked list, with few other helper operations. The following will demonstrate both implementations, using pseudocode.

#### **Array**

An array can be used to implement a (bounded) stack, as follows. The first element, usually at the <u>zero offset</u>, is the bottom, resulting in <code>array[0]</code> being the first element pushed onto the stack and the last element popped off. The program must keep track of the size (length) of the stack, using a variable *top* that records the number of items pushed so far, therefore pointing to the place in the array where the next element is to be inserted (assuming a zero-based index convention). Thus, the stack itself can be effectively implemented as a three-element structure:

```
structure stack:
   maxsize : integer
   top : integer
   items : array of item

procedure initialize(stk : stack, size : integer):
   stk.items ← new array of size items, initially empty
   stk.maxsize ← size
   stk.top ← 0
```

The *push* operation adds an element and increments the *top* index, after checking for overflow:

```
procedure push(stk : stack, x : item):
   if stk.top = stk.maxsize:
      report overflow error
   else:
      stk.items[stk.top] ← x
      stk.top ← stk.top + 1
```

Similarly, *pop* decrements the *top* index after checking for underflow, and returns the item that was previously the top one:

```
procedure pop(stk : stack):
    if stk.top = 0:
        report underflow error
    else:
        stk.top ← stk.top − 1
        r ← stk.items[stk.top]
    return r
```

Using a <u>dynamic array</u>, it is possible to implement a stack that can grow or shrink as much as needed. The size of the stack is simply the size of the dynamic array, which is a very efficient implementation of a stack since adding items to or removing items from the end of a dynamic array requires amortized O(1) time.

#### Linked list

Another option for implementing stacks is to use a <u>singly linked list</u>. A stack is then a pointer to the "head" of the list, with perhaps a counter to keep track of the size of the list:

```
structure frame:
data : item
next : frame or nil

structure stack:
head : frame or nil
size : integer
```

```
procedure initialize(stk : stack):

stk.head ← nil

stk.size ← 0
```

Pushing and popping items happens at the head of the list; overflow is not possible in this implementation (unless memory is exhausted):

```
procedure push(stk : stack, x : item):
    newhead ← new frame
    newhead.data ← x
    newhead.next ← stk.head
    stk.head ← newhead
    stk.size ← stk.size + 1

procedure pop(stk : stack):
    if stk.head = nil:
        report underflow error
    r ← stk.head.data
    stk.head ← stk.head.next
    stk.size ← stk.size - 1
    return r
```

### Stacks and programming languages

Some languages, such as <u>Perl</u>, <u>LISP</u>, <u>JavaScript</u> and <u>Python</u>, make the stack operations push and pop available on their standard list/array types. Some languages, notably those in the <u>Forth</u> family (including <u>PostScript</u>), are designed around language-defined stacks that are directly visible to and manipulated by the programmer.

The following is an example of manipulating a stack in <u>Common Lisp</u> (">" is the Lisp interpreter's prompt; lines not starting with ">" are the interpreter's responses to expressions):

```
> (setf stack (list 'a 'b 'c)) ;; set the variable "stack"
(A B C)
> (pop stack) ;; get top (leftmost) element, should modify the stack
A
> stack ;; check the value of stack
(B C)
> (push 'new stack) ;; push a new top onto the stack
(NEW B C)
```

Several of the C++ Standard Library container types have push\_back and pop\_back operations with LIFO semantics; additionally, the stack template class adapts existing containers to provide a restricted API with only push/pop operations. PHP has an SplStack (http://www.php.net/manual/en/class.splstack.php) class. Java's library contains a Stack (https://docs.oracle.com/javase/10/docs/api/java/util/Stack.html) class that is a specialization of Vector (https://docs.oracle.com/javase/10/docs/api/java/util/Vector.html). Following is an example program in Java language, using that class.

```
stack.pop();  // removing the top ("D")
stack.pop();  // removing the next top ("C")
}
}
```

### Hardware stack

A common use of stacks at the architecture level is as a means of allocating and accessing memory.

#### Basic architecture of a stack

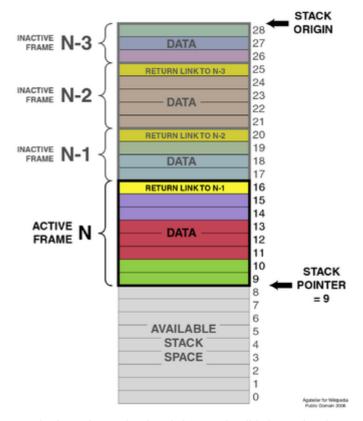
A typical stack is an area of computer memory with a fixed origin and a variable size. Initially the size of the stack is zero. A *stack pointer*, usually in the form of a hardware register, points to the most recently referenced location on the stack; when the stack has a size of zero, the stack pointer points to the origin of the stack.

The two operations applicable to all stacks are:

- a push operation, in which a data item is placed at the location pointed to by the stack pointer, and the address in the stack pointer is adjusted by the size of the data item;
- a pop or pull operation: a data item at the current location pointed to by the stack pointer is removed, and the stack pointer is adjusted by the size of the data item.

There are many variations on the basic principle of stack operations. Every stack has a fixed location, in memory, at which it begins. As data items are added to the stack, the stack pointer is displaced to indicate the current extent of the stack, which expands away from the origin.

Stack pointers may point to the origin of a stack or to a limited range of addresses either above or below the origin (depending on the direction in which the stack grows); however, the stack pointer cannot cross the origin of the stack. In other words, if the origin of the stack is at address 1000 and the stack grows downwards (towards addresses 999, 998, and so on), the stack pointer



A typical stack, storing local data and call information for nested procedure calls (not necessarily nested procedures). This stack grows downward from its origin. The stack pointer points to the current topmost datum on the stack. A push operation decrements the pointer and copies the data to the stack; a pop operation copies data from the stack and then increments the pointer. Each procedure called in the program stores procedure return information (in yellow) and local data (in other colors) by pushing them onto the stack. This type of stack implementation is extremely common, but it is vulnerable to buffer overflow attacks (see the text).

must never be incremented beyond 1000 (to 1001, 1002, etc.). If a pop operation on the stack causes the stack pointer to move past the origin of the stack, a *stack underflow* occurs. If a push operation causes the stack pointer to increment or decrement beyond the maximum extent of the stack, a *stack overflow* occurs.

Some environments that rely heavily on stacks may provide additional operations, for example:

- *Duplicate*: the top item is popped, and then pushed again (twice), so that an additional copy of the former top item is now on top, with the original below it.
- Peek: the topmost item is inspected (or returned), but the stack pointer and stack size does not change (meaning the item remains on the stack). This is also called top operation in many articles.
- *Swap* or *exchange*: the two topmost items on the stack exchange places.
- Rotate (or Roll): the *n* topmost items are moved on the stack in a rotating fashion. For example, if *n*=3, items 1, 2, and 3 on the stack are moved to positions 2, 3, and 1 on the stack, respectively. Many variants of this operation are possible, with the most common being called *left rotate* and *right rotate*.

Stacks are often visualized growing from the bottom up (like real-world stacks). They may also be visualized growing from left to right, so that "topmost" becomes "rightmost", or even growing from top to bottom. The important feature is that the bottom of the stack is in a fixed position. The illustration in this section is an example of a top-to-bottom growth visualization: the top (28) is the stack "bottom", since the stack "top" (9) is where items are pushed or popped from.

A *right rotate* will move the first element to the third position, the second to the first and the third to the second. Here are two equivalent visualizations of this process:

```
apple banana
banana ===right rotate==> cucumber
cucumber apple

cucumber apple
banana ===left rotate==> cucumber
apple
banana session banana
```

A stack is usually represented in computers by a block of memory cells, with the "bottom" at a fixed location, and the stack pointer holding the address of the current "top" cell in the stack. The top and bottom terminology are used irrespective of whether the stack actually grows towards lower memory addresses or towards higher memory addresses.

Pushing an item on to the stack adjusts the stack pointer by the size of the item (either decrementing or incrementing, depending on the direction in which the stack grows in memory), pointing it to the next cell, and copies the new top item to the stack area. Depending again on the exact implementation, at the end of a push operation, the stack pointer may point to the next unused location in the stack, or it may point to the topmost item in the stack. If the stack points to the current topmost item, the stack pointer will be updated before a new item is pushed onto the stack; if it points to the next available location in the stack, it will be updated *after* the new item is pushed onto the stack.

Popping the stack is simply the inverse of pushing. The topmost item in the stack is removed and the stack pointer is updated, in the opposite order of that used in the push operation.

#### Stack in main memory

Many <u>CISC</u>-type <u>CPU</u> designs, including the  $\underline{x86}$ ,  $\underline{Z80}$  and  $\underline{6502}$ , have a dedicated register for use as the <u>call stack</u> stack pointer with dedicated call, return, push, and pop instructions that implicitly update the dedicated register, thus increasing <u>code</u> density. Some CISC processors, like the <u>PDP-11</u> and the <u>68000</u>, also have special addressing modes for implementation of stacks, typically with a semi-dedicated stack pointer as well (such as A7 in the 68000). In contrast, most <u>RISC</u> CPU designs do not have dedicated stack instructions and therefore most if not all registers may be used as stack pointers as needed.

#### Stack in registers or dedicated memory

The <u>x87</u> <u>floating point</u> architecture is an example of a set of registers organised as a stack where direct access to individual registers (relative the current top) is also possible. As with stack-based machines in general, having the top-of-stack as an implicit argument allows for a small <u>machine code</u> footprint with a good usage of <u>bus bandwidth</u> and <u>code caches</u>, but it also prevents some types of optimizations possible on processors permitting <u>random access</u> to the <u>register file</u> for all (two or three) operands. A stack structure also makes <u>superscalar</u> implementations with <u>register renaming</u> (for <u>speculative execution</u>) somewhat more complex to implement, although it is still feasible, as exemplified by modern x87 implementations.

<u>Sun SPARC</u>, <u>AMD Am29000</u>, and <u>Intel i960</u> are all examples of architectures using <u>register windows</u> within a register-stack as another strategy to avoid the use of slow main memory for function arguments and return values.

There are also a number of small microprocessors that implements a stack directly in hardware and some microcontrollers have a fixed-depth stack that is not directly accessible. Examples are the PIC microcontrollers, the Computer Cowboys MuP21, the Harris RTX line, and the Novix NC4016. Many stack-based microprocessors were used to implement the programming language Forth at the microcode level. Stacks were also used as a basis of a number of mainframes and mini computers. Such machines were called stack machines, the most famous being the Burroughs B5000.

# **Applications of stacks**

### **Expression evaluation and syntax parsing**

Calculators employing <u>reverse Polish notation</u> use a stack structure to hold values. Expressions can be represented in prefix, postfix or infix notations and conversion from one form to another may be accomplished using a stack. Many compilers use a stack for parsing the syntax of expressions, program blocks etc. before translating into low level code. Most programming languages are <u>context-free languages</u>, allowing them to be parsed with stack based machines.

## **Backtracking**

Another important application of stacks is <u>backtracking</u>. Consider a simple example of finding the correct path in a maze. There are a series of points, from the starting point to the destination. We start from one point. To reach the final destination, there are several paths. Suppose we choose a random path. After following a certain path, we realise that the path we have chosen is wrong. So we need to find a way by which we can return to the beginning of that path. This can be done with the use of stacks. With the help of stacks, we remember the point where we have reached. This is done by pushing that point into the stack. In case we end up on the wrong path, we can pop the last point from the stack and thus return to the last point and continue our quest to find the right path. This is called backtracking.

The prototypical example of a backtracking algorithm is <u>depth-first search</u>, which finds all vertices of a graph that can be reached from a specified starting vertex. Other applications of backtracking involve searching through spaces that represent potential solutions to an optimization problem. <u>Branch and bound</u> is a technique for performing such backtracking searches without exhaustively searching all of the potential solutions in such a space.

# Compile time memory management

A number of programming languages are <u>stack-oriented</u>, meaning they define most basic operations (adding two numbers, printing a character) as taking their arguments from the stack, and placing any return values back on the stack. For example, <u>PostScript</u> has a return stack and an operand stack, and also has a graphics state stack and a dictionary stack. Many <u>virtual machines</u> are also stack-oriented, including the <u>p-code machine</u> and the Java Virtual Machine.

Almost all <u>calling conventions</u>—the ways in which <u>subroutines</u> receive their parameters and return results—use a special stack (the "<u>call stack</u>") to hold information about procedure/function calling and nesting in order to switch to the context of the called function and restore to the caller function when the calling finishes. The functions follow a runtime protocol between caller and callee to save arguments and return value on the stack. Stacks are an important way of supporting nested or <u>recursive</u> function calls. This type of stack is used implicitly by the compiler to support CALL and RETURN statements (or their equivalents) and is not manipulated directly by the programmer.

Some programming languages use the stack to store data that is local to a procedure. Space for local data items is allocated from the stack when the procedure is entered, and is deallocated when the procedure exits. The  $\underline{C}$  programming language is typically implemented in this way. Using the same stack for both data and procedure calls has important security implications (see below) of which a programmer must be aware in order to avoid introducing serious security bugs into a program.

### Efficient algorithms

Several <u>algorithms</u> use a stack (separate from the usual function call stack of most programming languages) as the principle <u>data structure</u> with which they organize their information. These include:

- Graham scan, an algorithm for the convex hull of a two-dimensional system of points. A convex hull of a subset of the input is maintained in a stack, which is used to find and remove concavities in the boundary when a new point is added to the hull.
- Part of the SMAWK algorithm for finding the row minima of a monotone matrix uses stacks in a similar way to Graham scan. [19]
- All nearest smaller values, the problem of finding, for each number in an array, the closest preceding number that is smaller than it. One algorithm for this problem uses a stack to maintain a collection of candidates for the nearest smaller value. For each position in the array, the stack is popped until a smaller value is found on its top, and then the value in the new position is pushed onto the stack.
- The nearest-neighbor chain algorithm, a method for agglomerative hierarchical clustering based on maintaining a stack of clusters, each of which is the nearest neighbor of its predecessor on the stack. When this method finds a pair of clusters that are mutual nearest neighbors, they are popped and merged. [21]

# **Security**

Some computing environments use stacks in ways that may make them vulnerable to <u>security breaches</u> and attacks. Programmers working in such environments must take special care to avoid the pitfalls of these implementations.

For example, some programming languages use a common stack to store both data local to a called procedure and the linking information that allows the procedure to return to its caller. This means that the program moves data into and out of the same stack that contains critical return addresses for the procedure calls. If data is moved to the wrong location on the stack, or an oversized data item is moved to a stack location that is not large enough to contain it, return information for procedure calls may be corrupted, causing the program to fail.

Malicious parties may attempt a <u>stack smashing</u> attack that takes advantage of this type of implementation by providing oversized data input to a program that does not check the length of input. Such a program may copy the data in its entirety to a location on the stack, and in so doing it may change the return addresses for procedures that have called it. An attacker can experiment to find a specific type of data that can be provided to such a program such that the return address of the current procedure is reset to point to an area within the stack itself (and within the data provided by the attacker), which in turn contains instructions that carry out unauthorized operations.

This type of attack is a variation on the <u>buffer overflow</u> attack and is an extremely frequent source of security breaches in software, mainly because some of the most popular compilers use a shared stack for both data and procedure calls, and do not verify the length of data items. Frequently programmers do not write code to verify the size of data items, either, and when an oversized or undersized data item is copied to the stack, a security breach may occur.

### See also

- List of data structures
- Queue
- Double-ended gueue
- FIFO (computing and electronics)
- Stack-based memory allocation
- Stack overflow
- Stack-oriented programming language

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Donald Knuth. <u>The Art of Computer Programming</u>, Volume 1: <u>Fundamental Algorithms</u>, Third Edition. Addison-Wesley, 1997. <u>ISBN</u> <u>0-201-89683-4</u>. Section 2.2.1: Stacks, Queues, and Deques, pp. 238–243.

### **External links**

- Stack Machines the new wave (http://www.ece.cmu.edu/~koopman/stack\_computers/index.html)
- Bounding stack depth (http://www.cs.utah.edu/~regehr/stacktool)
- Stack Size Analysis for Interrupt-driven Programs (http://www.cs.ucla.edu/~palsberg/paper/sas 03.pdf) (322 KB)

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