

# Three-Sum — Complete Notes & Step-by-Step Logic

## Problem (exactly as provided):

Given an integer array `nums`, return all the triplets `[nums[i], nums[j], nums[k]]` such that  $i \neq j$ ,  $i \neq k$ , and  $j \neq k$ , and  $nums[i] + nums[j] + nums[k] == 0$ . The solution set must not contain duplicate triplets.

## Examples (exact as provided):

Example 1:

Input: `nums = [-1,0,1,2,-1,-4]`

Output: `[[-1,-1,2],[-1,0,1]]`

Example 2:

Input: `nums = [0,1,1]`

Output: `[]`

Example 3:

Input: `nums = [0,0,0]`

Output: `[[0,0,0]]`

## Constraints (exact as provided):

-  $3 \leq \text{nums.length} \leq 3000$

-  $-10^5 \leq \text{nums}[i] \leq 10^5$

## Original code (you provided):

```
class Solution {
public:
    vector<vector<int>> threeSum(vector<int>& nums) {
        int n = nums.size();

        vector<vector<int>> ans;

        sort(nums.begin(), nums.end());

        for(int i=0; i<n; i++) {

            if(i > 0 && nums[i] == nums[i-1]) continue;

            int j=i+1, k = n-1;

            while(j < k) {
                int sum = nums[i] + nums[j] + nums[k];
                if(sum < 0) {
                    j++;
                } else if(sum > 0) {
                    k--;
                } else {
                    ans.push_back({nums[i], nums[j], nums[k]});
                    j++;
                    k--;

                    while(j < k && nums[j] == nums[j-1]) {
                        j++;
                    }
                }
            }
        }

        return ans;
    }
};
```

## Full Step-by-Step Logic (detailed for revision):

- 1 **1. Sort the array (ascending).** This makes it possible to use the two-pointer technique and makes duplicate detection easy.
- 2 **2. Iterate i from 0 to n-3** (fix the first element of a potential triplet):
  - 3 - If  $\text{nums}[i] > 0$ : break. Since array is sorted, all remaining numbers are  $\geq \text{nums}[i]$ , so sum cannot be 0.
  - 4 - If  $i > 0$  and  $\text{nums}[i] == \text{nums}[i-1]$ : continue. Skip duplicates to avoid repeating triplets that start with the same number.
- 5 **3. For each fixed i, use two pointers l and r:** set  $l = i + 1$  and  $r = n - 1$ .
  - 6 - While  $l < r$ : compute  $\text{sum} = \text{nums}[i] + \text{nums}[l] + \text{nums}[r]$ .
    - 7 • If  $\text{sum} < 0$ : move  $l++$  (we need a larger sum because array is sorted).
    - 8 • If  $\text{sum} > 0$ : move  $r--$  (we need a smaller sum).
    - 9 • If  $\text{sum} == 0$ : record the triplet  $\{\text{nums}[i], \text{nums}[l], \text{nums}[r]\}$ . Then move both pointers ( $l++$  and  $r--$ ) *and* skip duplicates on both sides:
  - 10 - while ( $l < r$  &&  $\text{nums}[l] == \text{nums}[l-1]$ )  $l++$ ;
  - 11 - while ( $l < r$  &&  $\text{nums}[r] == \text{nums}[r+1]$ )  $r--$ ;
- 12 **4. Continue until all i values are processed.** Return the collected triplets.

## Pseudocode (concise):

```
sort(nums)
for i in range(0, n-2):
    if nums[i] > 0: break
    if i > 0 and nums[i] == nums[i-1]: continue
    l = i+1
    r = n-1
    while l < r:
        s = nums[i] + nums[l] + nums[r]
        if s < 0: l += 1
        elif s > 0: r -= 1
        else:
            add [nums[i], nums[l], nums[r]] to answer
            l += 1
            r -= 1
            skip duplicates at l and r
```

## Corrected & commented C++ implementation:

```
#include <bits/stdc++.h>
using namespace std;

class Solution {
public:
    vector<vector<int>> threeSum(vector<int>& nums) {
        int n = nums.size();
        vector<vector<int>> ans;
        if (n < 3) return ans;

        sort(nums.begin(), nums.end()); // O(n log n)

        for (int i = 0; i < n - 2; ++i) {
            // Early stop: if the current number > 0, remaining can't sum to 0
            if (nums[i] > 0) break;

            // Skip duplicate 'i' values
            if (i > 0 && nums[i] == nums[i - 1]) continue;

            int l = i + 1, r = n - 1;

            while (l < r) {
                int sum = nums[i] + nums[l] + nums[r];
                if (sum < 0) {
                    ++l; // need a larger sum
                } else if (sum > 0) {
                    --r; // need a smaller sum
                } else {

```

```

        // found a valid triplet
        ans.push_back({nums[l], nums[r], nums[i]});
        ++l;
        --r;
        // skip duplicates for left and right pointers
        while (l < r && nums[l] == nums[l + 1]) ++l;
        while (l < r && nums[r] == nums[r - 1]) --r;
    }
}

return ans;
};

```

## Complexity Analysis (step-wise justification):

- Sorting:  $O(n \log n)$  time.
- Two-pointer search: For each  $i$  ( $O(n)$  iterations), the inner two-pointer loop runs in  $O(n)$  time total (each pointer moves at most  $n$  steps). So combined it's  $O(n^2)$ .
- Total time:  $O(n \log n + n^2) = O(n^2)$ .
- Space:  $O(1)$  extra auxiliary space (only pointers and temporary variables), excluding the space required for the output triplets.

## Example walkthrough (nums = [-1,0,1,2,-1,-4]):

- Sort: [-4, -1, -1, 0, 1, 2]
- $i = 0$  (nums[i] = -4):  $l = 1$  (-1),  $r = 5$  (2)  $\rightarrow$  sum = -3 < 0  $\rightarrow$   $l++$  ... no triplet found for  $i=0$ .
- $i = 1$  (nums[i] = -1):  $l = 2$  (-1),  $r = 5$  (2)  $\rightarrow$  sum = 0  $\rightarrow$  record [-1, -1, 2]. Move  $l \rightarrow 3$  (0),  $r \rightarrow 4$  (1).
- Now sum = -1 + 0 + 1 = 0  $\rightarrow$  record [-1, 0, 1]. Move  $l \rightarrow 4$ ,  $r \rightarrow 3$  (stop).
- $i = 2$  is duplicate of  $i = 1$ , so skip. Remaining  $i$  values don't produce new triplets. Final: [[-1,-1,2], [-1,0,1]].

## Revision checklist & common pitfalls:

- Always sort the array first.
- Skip duplicate values for 'i' to avoid duplicate triplets.
- After finding a triplet, advance both  $l$  and  $r$  and skip duplicates on both sides.
- Use early break if  $nums[i] > 0$  (micro-optimization).
- Be careful with arrays of many identical values (e.g., [0,0,0,...]).
- Don't forget to handle small  $n$  (e.g.,  $n < 3$ ) by returning empty result.

## Memory aid (one-line):

Sort  $\rightarrow$  Fix  $i \rightarrow$  Two-pointer for  $-nums[i] \rightarrow$  Skip duplicates  $\rightarrow O(n^2)$

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