

# Hierarchical clustering

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```
library(ISLR)
library(readr)
library(tidyverse)

## -- Attaching packages ----- tidyverse 1.2.1 --

## v ggplot2 3.2.1      v purrr  0.3.2
## v tibble  2.1.3      v dplyr  0.8.3
## v tidyr   1.0.0      v stringr 1.4.0
## v ggplot2 3.2.1      v forcats 0.4.0

## -- Conflicts ----- tidyverse_conflicts() --
## x dplyr::filter() masks stats::filter()
## x dplyr::lag()    masks stats::lag()

library(cluster)
library(factoextra)

## Welcome! Related Books: `Practical Guide To Cluster Analysis in R` at
## https://goo.gl/13EFCZ

library(dendextend)

##
## -----
## Welcome to dendextend version 1.12.0
## Type citation('dendextend') for how to cite the package.
##
## Type browseVignettes(package = 'dendextend') for the package vignette.
## The github page is: https://github.com/talgalili/dendextend/
##
## Suggestions and bug-reports can be submitted at:
## https://github.com/talgalili/dendextend/issues
## Or contact: <tal.galili@gmail.com>
##
## To suppress this message use:
## suppressPackageStartupMessages(library(dendextend))
## -----
##
## Attaching package: 'dendextend'
```

```
## The following object is masked from 'package:stats':  
##  
##      cutree
```

```
library(fpc)
```

```
cereals <- read_csv("Cereals.csv")
```

```
## Parsed with column specification:
```

```
## cols(  
##   name = col_character(),  
##   mfr = col_character(),  
##   type = col_character(),  
##   calories = col_double(),  
##   protein = col_double(),  
##   fat = col_double(),  
##   sodium = col_double(),  
##   fiber = col_double(),  
##   carbo = col_double(),  
##   sugars = col_double(),  
##   potass = col_double(),  
##   vitamins = col_double(),  
##   shelf = col_double(),  
##   weight = col_double(),  
##   cups = col_double(),  
##   rating = col_double()  
## )
```

```
View(cereals)
```

```
set.seed(123)
```

```
summary(cereals)
```

```
##      name                mfr                type                calories  
## Length:77          Length:77          Length:77          Min.   : 50.0  
## Class :character    Class :character    Class :character    1st Qu.:100.0  
## Mode  :character    Mode  :character    Mode  :character    Median :110.0  
##                                     Mean   :106.9  
##                                     3rd Qu.:110.0  
##                                     Max.   :160.0  
##  
##      protein            fat            sodium            fiber  
## Min.   :1.000      Min.   :0.000      Min.   : 0.0      Min.   : 0.000  
## 1st Qu.:2.000      1st Qu.:0.000      1st Qu.:130.0     1st Qu.: 1.000  
## Median :3.000      Median :1.000      Median :180.0     Median : 2.000  
## Mean   :2.545      Mean   :1.013      Mean   :159.7     Mean   : 2.152  
## 3rd Qu.:3.000      3rd Qu.:2.000      3rd Qu.:210.0     3rd Qu.: 3.000  
## Max.   :6.000      Max.   :5.000      Max.   :320.0     Max.   :14.000  
##  
##      carbo            sugars            potass            vitamins  
## Min.   : 5.0      Min.   : 0.000      Min.   : 15.00     Min.   : 0.00  
## 1st Qu.:12.0      1st Qu.: 3.000      1st Qu.: 42.50     1st Qu.: 25.00
```

```

## Median :14.5   Median : 7.000   Median : 90.00   Median : 25.00
## Mean    :14.8   Mean     : 7.026   Mean     : 98.67   Mean     : 28.25
## 3rd Qu.:17.0   3rd Qu.:11.000   3rd Qu.:120.00   3rd Qu.: 25.00
## Max.    :23.0   Max.     :15.000   Max.     :330.00   Max.     :100.00
## NA's    :1     NA's     :1     NA's     :2
## shelf           weight           cups           rating
## Min.    :1.000   Min.     :0.50   Min.     :0.250   Min.     :18.04
## 1st Qu.:1.000   1st Qu.:1.00   1st Qu.:0.670   1st Qu.:33.17
## Median :2.000   Median :1.00   Median :0.750   Median :40.40
## Mean    :2.208   Mean     :1.03   Mean     :0.821   Mean     :42.67
## 3rd Qu.:3.000   3rd Qu.:1.00   3rd Qu.:1.000   3rd Qu.:50.83
## Max.    :3.000   Max.     :1.50   Max.     :1.500   Max.     :93.70
##

cereals.norm <- cereals[,-c(1:3)]#normaliizing the dataset
cereals.norm <- na.omit(cereals.norm)#Ommiitting na values
cereals.norm <- scale(cereals.norm)
str(cereals.norm)

## num [1:74, 1:13] -1.866 0.654 -1.866 -2.874 0.15 ...
## - attr(*, "dimnames")=List of 2
## ..$ : NULL
## ..$ : chr [1:13] "calories" "protein" "fat" "sodium" ...
## - attr(*, "scaled:center")= Named num [1:13] 107.03 2.51 1 162.36 2.18
## ...
## ..- attr(*, "names")= chr [1:13] "calories" "protein" "fat" "sodium" ...
## - attr(*, "scaled:scale")= Named num [1:13] 19.84 1.08 1.01 82.77 2.42
## ...
## ..- attr(*, "names")= chr [1:13] "calories" "protein" "fat" "sodium" ...

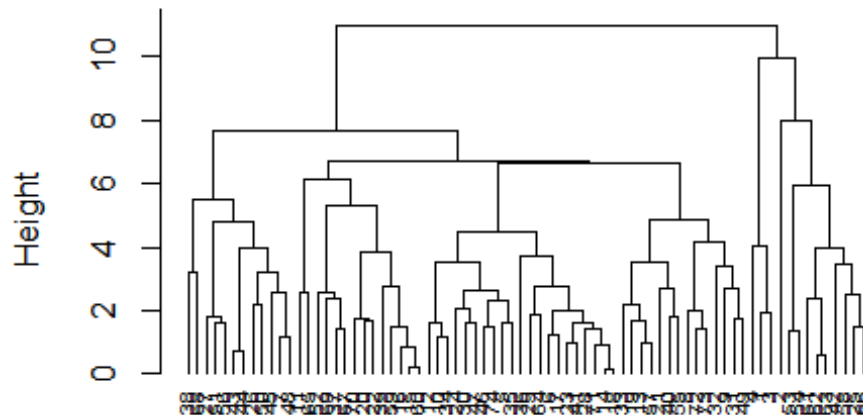
# Dissimilarity matrix
d <- dist(cereals.norm, method = "euclidean")

# Hierarchical clustering using Complete Linkage
hc1 <- hclust(d, method = "complete" )

# Plot the obtained dendrogram
plot(hc1, cex = 0.6, hang = -1)

```

## Cluster Dendrogram



hclust (\*, "complete")

```
# Dissimilarity matrix
d <- dist(cereals.norm, method = "euclidean")

# Compute with agnes and with different Linkage methods
hc_single <- agnes(cereals.norm, method = "single")
hc_complete <- agnes(cereals.norm, method = "complete")
hc_average <- agnes(cereals.norm, method = "average")
hc_ward <- agnes(cereals.norm, method = "ward")

# Compare Agglomerative coefficients
print(hc_single$ac)
## [1] 0.6067859

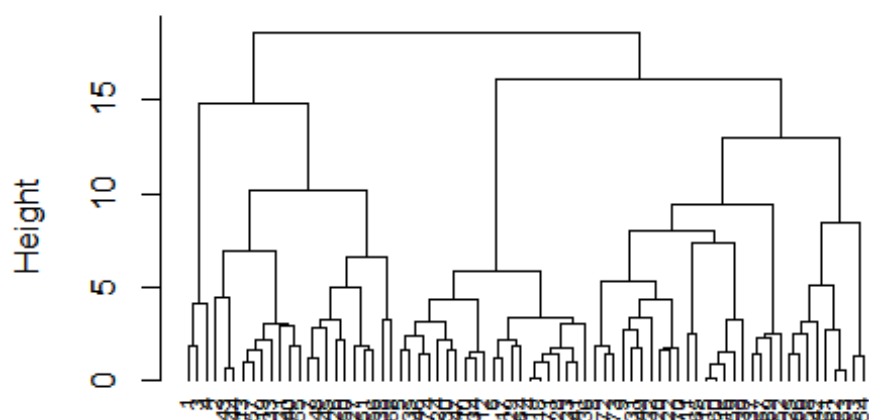
print(hc_complete$ac)
## [1] 0.8353712

print(hc_average$ac)
## [1] 0.7766075

print(hc_ward$ac)
## [1] 0.9046042

hc2 <- agnes(cereals.norm, method = "ward")
pltree(hc2, cex = 0.6, hang = -1, main = "Dendrogram of agnes")
```

## Dendrogram of agnes

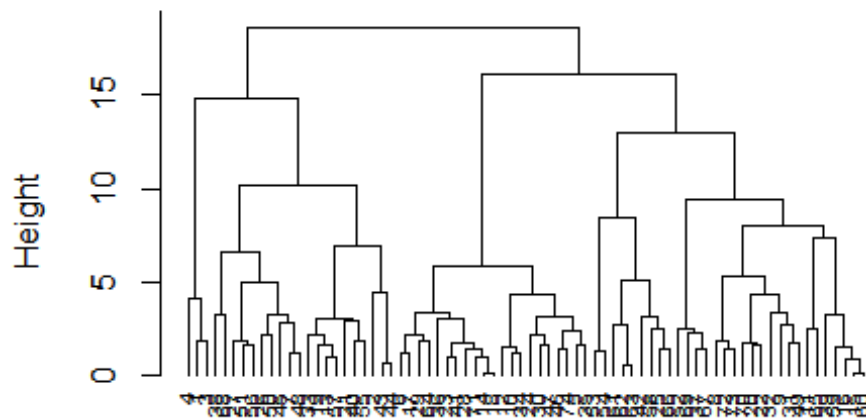


```
d <- dist(cereals.norm, method = "euclidean")
```

```
# Hierarchical clustering using Ward Linkage  
hc3 <- hclust(d, method = "ward.D2" )
```

```
# Plot the obtained dendrogram  
plot(hc3, cex = 0.6, hang = -1)
```

## Cluster Dendrogram

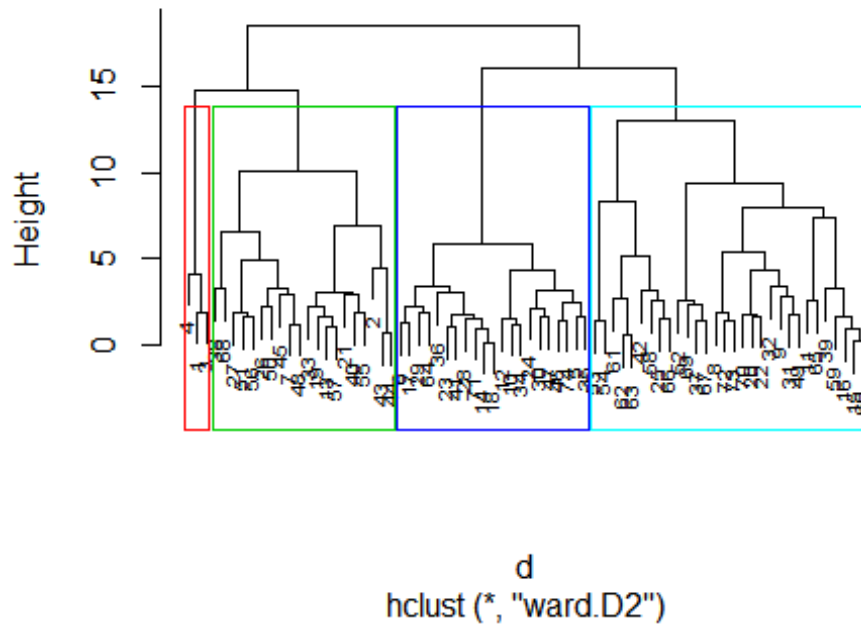


d  
hclust (\*, "ward.D2")

*#From the dendrogram,when we cut the longest length we are obtaining the optimal number of clusters as 6*

```
hcluster <- cutree(hc3, k = 4)
plot(hc3, cex = 0.6)
rect.hclust(hc3, k = 4, border = 2:5)
```

## Cluster Dendrogram



```
fviz_cluster(list(data = cereals.norm, cluster = hcluster))
```

## Cluster plot



```

#cluster stabilities of all 4 clusters
hclust_stability <- clusterboot(cereals.norm, clustermethod=hclustCBI,
method="ward.D2", k=4, count = FALSE)
hclust_stability

## * Cluster stability assessment *
## Cluster method: hclust/cutree
## Full clustering results are given as parameter result
## of the clusterboot object, which also provides further statistics
## of the resampling results.
## Number of resampling runs: 100
##
## Number of clusters found in data: 4
##
## Clusterwise Jaccard bootstrap (omitting multiple points) mean:
## [1] 0.5651665 0.7875223 0.8663548 0.6777744
## dissolved:
## [1] 49 7 5 27
## recovered:
## [1] 51 61 79 43

#Analyze the clustering results
clusters <- hclust_stability$result$partition

#Cluster stability values
hclust_stability$bootmean

## [1] 0.5651665 0.7875223 0.8663548 0.6777744

library(caret)

## Loading required package: lattice

##
## Attaching package: 'caret'

## The following object is masked from 'package:purrr':
##
## lift

set.seed(123)
C<-cereals
C1<-na.omit(C)

C_index<-createDataPartition(C1$calories,p=0.5,list=FALSE)
train_data<-C1[C_index,]
test_data<-C1[-C_index,]
train_data<-scale(train_data[, -c(1:3)])
test_data<-scale(test_data[, -c(1:3)])

# Compute with agnes and with different Linkage methods

```



```

hc_single <- agnes(train_data, method = "single")
hc_complete <- agnes(train_data, method = "complete")
hc_average <- agnes(train_data, method = "average")
hc_ward <- agnes(train_data, method = "ward")

# Compare Agglomerative coefficients
print(hc_single$ac)

## [1] 0.6482111

print(hc_complete$ac)

## [1] 0.7717234

print(hc_average$ac)

## [1] 0.7358853

print(hc_ward$ac)

## [1] 0.8199919

# Compute with agnes and with different linkage methods
hc_single1 <- agnes(test_data, method = "single")
hc_complete1 <- agnes(test_data, method = "complete")
hc_average1 <- agnes(test_data, method = "average")
hc_ward1 <- agnes(test_data, method = "ward")

# Compare Agglomerative coefficients
print(hc_single1$ac)

## [1] 0.6713887

print(hc_complete1$ac)

## [1] 0.8142103

print(hc_average1$ac)

## [1] 0.7402693

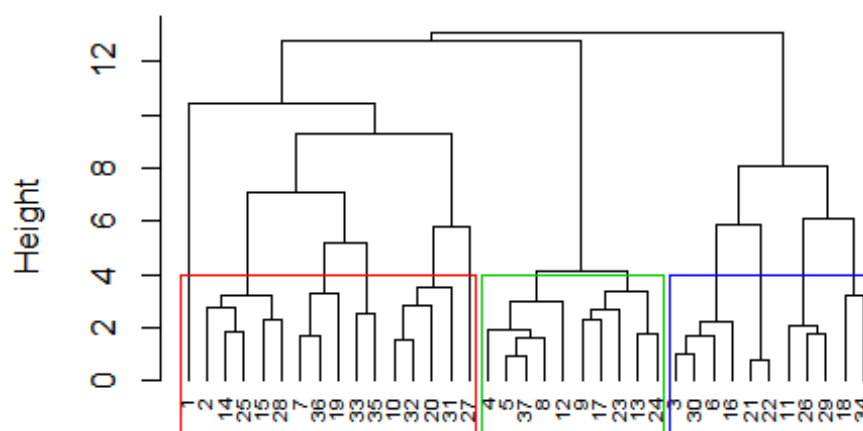
print(hc_ward1$ac)

## [1] 0.8457967

pltree(hc_ward, cex=0.6, hang=-1, main="Dendrogram of agnes")
rect.hclust(hc_ward, k = 3, border = 2:5)

```

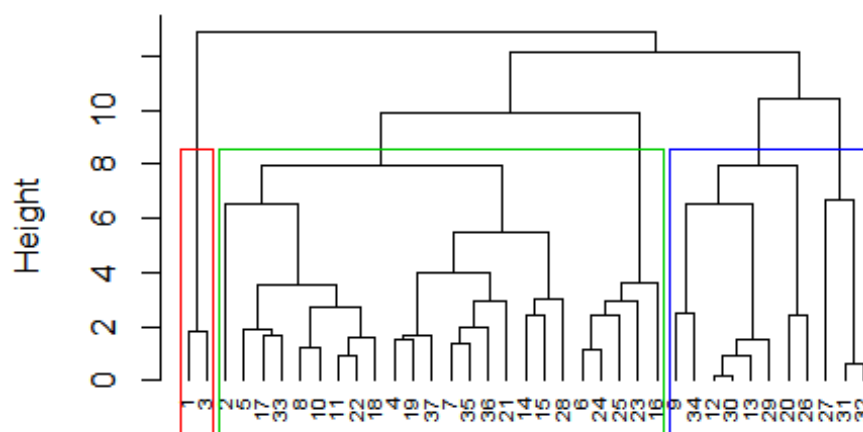
**Dendrogram of agnes**



train\_data  
agnes (\*, "ward")

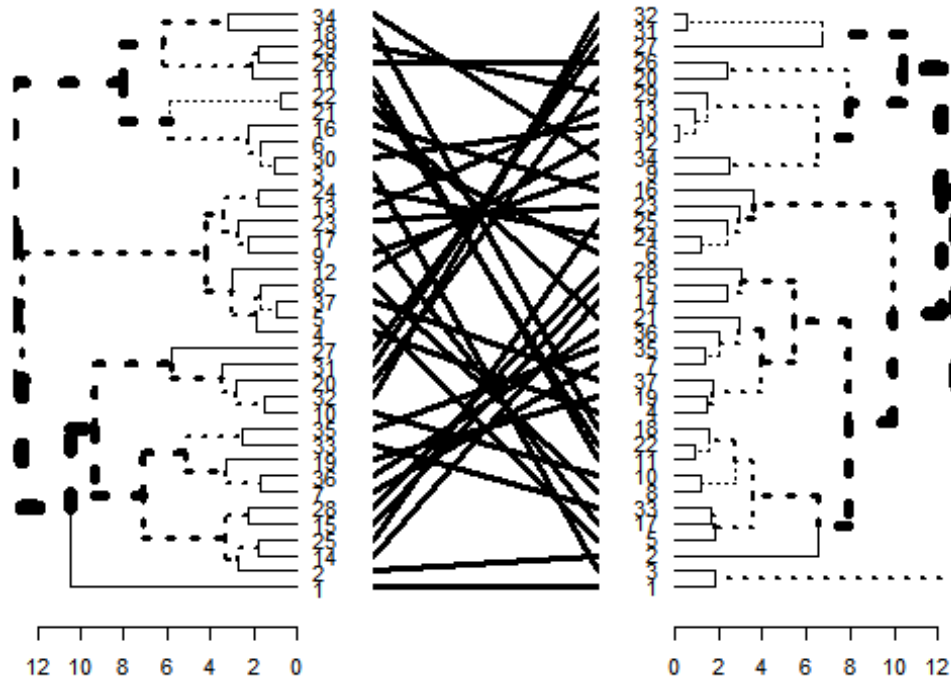
```
pltree(hc_ward1,cex=0.6,hang=-1,main="Dendrogram of agnes")
rect.hclust(hc_ward1, k = 3, border = 2:5)
```

**Dendrogram of agnes**



test\_data  
agnes (\*, "ward")

```
tanglegram(as.dendrogram(hc_ward),as.dendrogram(hc_ward1))
```



```
cor_cophenetic(as.dendrogram(hc_ward),as.dendrogram(hc_ward1))
```

```
## [1] 0.09342934
```

```
cor_bakers_gamma(as.dendrogram(hc_ward),as.dendrogram(hc_ward1))
```

```
## [1] 0.07586184
```

*#Since the stability values are near to zero the above model is not stable*

```
result<-cbind(C1,hcluster)
result[result$hcluster==1,]
```

```
##           name mfr type calories protein fat sodium fiber
## 1      100%_Bran   N    C       70        4   1    130    10
## 3          All-Bran   K    C       70        4   1    260     9
## 4 All-Bran_with_Extra_Fiber K    C       50        4   0    140    14
##   carbo sugars potass vitamins shelf weight cups  rating hcluster
## 1     5      6     280      25    3      1 0.33 68.40297        1
## 3     7      5     320      25    3      1 0.33 59.42551        1
## 4     8      0     330      25    3      1 0.50 93.70491        1
```

```
result[result$hcluster==2,]
```

```
##           name mfr type calories protein fat
## 2      100%_Natural_Bran   Q    C      120        3   5
## 7          Basic_4       G    C      130        3   2
```

```

## 13                Clusters      G      C      110      3      2
## 19      Cracklin'_Oat_Bran      K      C      110      3      3
## 21      Crispy_Wheat_&_Raisins  G      C      100      2      1
## 26 Fruit_&_Fibre_Dates,_Walnuts,_and_Oats P      C      120      3      2
## 27                Fruitful_Bran  K      C      120      3      0
## 33                Great_Grains_Pecan P      C      120      3      3
## 38                Just_Right_Fruit_&_Nut K      C      140      3      1
## 40                Life           Q      C      100      4      2
## 43      Muesli_Raisins,_Dates,_&_Almonds R      C      150      4      3
## 44      Muesli_Raisins,_Peaches,_&_Pecans R      C      150      4      3
## 45                Mueslix_Crispy_Blend K      C      160      3      2
## 48      Nutri-Grain_Almond-Raisin K      C      140      3      2
## 50                Oatmeal_Raisin_Crisp G      C      130      3      2
## 51                Post_Nat._Raisin_Bran P      C      120      3      1
## 55                Quaker_Oat_Squares   Q      C      100      4      1
## 56                Raisin_Bran          K      C      120      3      1
## 57                Raisin_Nut_Bran      G      C      100      3      2
## 68                Total_Raisin_Bran    G      C      140      3      1
##      sodium fiber carbo sugars potass vitamins shelf weight cups rating
## 2          15   2.0   8.0      8    135        0     3   1.00 1.00 33.98368
## 7          210   2.0  18.0      8    100       25     3   1.33 0.75 37.03856
## 13         140   2.0  13.0      7    105       25     3   1.00 0.50 40.40021
## 19         140   4.0  10.0      7    160       25     3   1.00 0.50 40.44877
## 21         140   2.0  11.0     10    120       25     3   1.00 0.75 36.17620
## 26         160   5.0  12.0     10    200       25     3   1.25 0.67 40.91705
## 27         240   5.0  14.0     12    190       25     3   1.33 0.67 41.01549
## 33          75   3.0  13.0      4    100       25     3   1.00 0.33 45.81172
## 38         170   2.0  20.0      9     95      100     3   1.30 0.75 36.47151
## 40         150   2.0  12.0      6     95       25     2   1.00 0.67 45.32807
## 43          95   3.0  16.0     11    170       25     3   1.00 1.00 37.13686
## 44         150   3.0  16.0     11    170       25     3   1.00 1.00 34.13976
## 45         150   3.0  17.0     13    160       25     3   1.50 0.67 30.31335
## 48         220   3.0  21.0      7    130       25     3   1.33 0.67 40.69232
## 50         170   1.5  13.5     10    120       25     3   1.25 0.50 30.45084
## 51         200   6.0  11.0     14    260       25     3   1.33 0.67 37.84059
## 55         135   2.0  14.0      6    110       25     3   1.00 0.50 49.51187
## 56         210   5.0  14.0     12    240       25     2   1.33 0.75 39.25920
## 57         140   2.5  10.5      8    140       25     3   1.00 0.50 39.70340
## 68         190   4.0  15.0     14    230      100     3   1.50 1.00 28.59278
##      hcluster
## 2           2
## 7           2
## 13          2
## 19          2
## 21          2
## 26          2
## 27          2
## 33          2
## 38          2
## 40          2

```

```
## 43      2
## 44      2
## 45      2
## 48      2
## 50      2
## 51      2
## 55      2
## 56      2
## 57      2
## 68      2
```

```
result[result$hcluster==3,]
```

```
##              name mfr type calories protein fat sodium fiber
## 5  Apple_Cinnamon_Cheerios G C 110 2 2 180 1.5
## 6      Apple_Jacks K C 110 2 0 125 1.0
## 10      Cap'n'Crunch Q C 120 1 2 220 0.0
## 12  Cinnamon_Toast_Crunch G C 120 1 3 210 0.0
## 14      Cocoa_Puffs G C 110 1 1 180 0.0
## 17      Corn_Pops K C 110 1 0 90 1.0
## 18      Count_Chocula G C 110 1 1 180 0.0
## 23      Froot_Loops K C 110 2 1 125 1.0
## 24      Frosted_Flakes K C 110 1 0 200 1.0
## 28      Fruity_Pebbles P C 110 1 1 135 0.0
## 29      Golden_Crisp P C 100 2 0 45 0.0
## 30      Golden_Grahams G C 110 1 1 280 0.0
## 34      Honey_Graham_Ohs Q C 120 1 2 220 1.0
## 35      Honey_Nut_Cheerios G C 110 3 1 250 1.5
## 36      Honey-comb P C 110 1 0 180 0.0
## 41      Lucky_Charms G C 110 2 1 180 0.0
## 46  Multi-Grain_Cheerios G C 100 2 1 220 2.0
## 47      Nut&Honey_Crunch K C 120 2 1 190 0.0
## 64      Smacks K C 110 2 1 70 1.0
## 71      Trix G C 110 1 1 140 0.0
## 74      Wheaties_Honey_Gold G C 110 2 1 200 1.0
##      carbo sugars potass vitamins shelf weight cups rating hcluster
## 5  10.5 10 70 25 1 1 0.75 29.50954 3
## 6  11.0 14 30 25 2 1 1.00 33.17409 3
## 10 12.0 12 35 25 2 1 0.75 18.04285 3
## 12 13.0 9 45 25 2 1 0.75 19.82357 3
## 14 12.0 13 55 25 2 1 1.00 22.73645 3
## 17 13.0 12 20 25 2 1 1.00 35.78279 3
## 18 12.0 13 65 25 2 1 1.00 22.39651 3
## 23 11.0 13 30 25 2 1 1.00 32.20758 3
## 24 14.0 11 25 25 1 1 0.75 31.43597 3
## 28 13.0 12 25 25 2 1 0.75 28.02576 3
## 29 11.0 15 40 25 1 1 0.88 35.25244 3
## 30 15.0 9 45 25 2 1 0.75 23.80404 3
## 34 12.0 11 45 25 2 1 1.00 21.87129 3
## 35 11.5 10 90 25 1 1 0.75 31.07222 3
```

```
## 36 14.0      11      35      25      1      1 1.33 28.74241      3
## 41 12.0      12      55      25      2      1 1.00 26.73451      3
## 46 15.0       6      90      25      1      1 1.00 40.10596      3
## 47 15.0       9      40      25      2      1 0.67 29.92429      3
## 64  9.0      15      40      25      2      1 0.75 31.23005      3
## 71 13.0      12      25      25      2      1 1.00 27.75330      3
## 74 16.0       8      60      25      1      1 0.75 36.18756      3
```

```
result[result$hcluster==4,]
```

```
##              name mfr type calories protein fat sodium fiber
## 8           Bran_Chex R   C      90        2   1    200      4
## 9           Bran_Flakes P   C      90        3   0    210      5
## 11          Cheerios G   C     110        6   2    290      2
## 15          Corn_Chex R   C     110        2   0    280      0
## 16          Corn_Flakes K   C     100        2   0    290      1
## 20          Crispix K   C     110        2   0    220      1
## 22          Double_Chex R   C     100        2   0    190      1
## 25      Frosted_Mini-Wheats K   C     100        3   0      0      3
## 31      Grape_Nuts_Flakes P   C     100        3   1    140      3
## 32      Grape-Nuts P   C     110        3   0    170      3
## 37 Just_Right_Crunchy__Nuggets K   C     110        2   1    170      1
## 39              Kix G   C     110        2   1    260      0
## 42              Maypo A   H     100        4   1      0      0
## 49      Nutri-grain_Wheat K   C      90        3   0    170      3
## 52      Product_19 K   C     100        3   0    320      1
## 53      Puffed_Rice Q   C      50        1   0      0      0
## 54      Puffed_Wheat Q   C      50        2   0      0      1
## 58      Raisin_Squares K   C      90        2   0      0      2
## 59      Rice_Chex R   C     110        1   0    240      0
## 60      Rice_Krispies K   C     110        2   0    290      0
## 61      Shredded_Wheat N   C      80        2   0      0      3
## 62      Shredded_Wheat_'n'Bran N   C      90        3   0      0      4
## 63      Shredded_Wheat_spoon_size N   C      90        3   0      0      3
## 65      Special_K K   C     110        6   0    230      1
## 66      Strawberry_Fruit_Wheats N   C      90        2   0     15      3
## 67      Total_Corn_Flakes G   C     110        2   1    200      0
## 69      Total_Whole_Grain G   C     100        3   1    200      3
## 70      Triples G   C     110        2   1    250      0
## 72      Wheat_Chex R   C     100        3   1    230      3
## 73      Wheaties G   C     100        3   1    200      3
##      carbo sugars potass vitamins shelf weight cups rating hcluster
## 8       15      6     125      25      1   1.00 0.67 49.12025      4
## 9       13      5     190      25      3   1.00 0.67 53.31381      4
## 11      17      1     105      25      1   1.00 1.25 50.76500      4
## 15      22      3      25      25      1   1.00 1.00 41.44502      4
## 16      21      2      35      25      1   1.00 1.00 45.86332      4
## 20      21      3      30      25      3   1.00 1.00 46.89564      4
## 22      18      5      80      25      3   1.00 0.75 44.33086      4
## 25      14      7     100      25      2   1.00 0.80 58.34514      4
```

## 31	15	5	85	25	3	1.00	0.88	52.07690	4
## 32	17	3	90	25	3	1.00	0.25	53.37101	4
## 37	17	6	60	100	3	1.00	1.00	36.52368	4
## 39	21	3	40	25	2	1.00	1.50	39.24111	4
## 42	16	3	95	25	2	1.00	1.00	54.85092	4
## 49	18	2	90	25	3	1.00	1.00	59.64284	4
## 52	20	3	45	100	3	1.00	1.00	41.50354	4
## 53	13	0	15	0	3	0.50	1.00	60.75611	4
## 54	10	0	50	0	3	0.50	1.00	63.00565	4
## 58	15	6	110	25	3	1.00	0.50	55.33314	4
## 59	23	2	30	25	1	1.00	1.13	41.99893	4
## 60	22	3	35	25	1	1.00	1.00	40.56016	4
## 61	16	0	95	0	1	0.83	1.00	68.23588	4
## 62	19	0	140	0	1	1.00	0.67	74.47295	4
## 63	20	0	120	0	1	1.00	0.67	72.80179	4
## 65	16	3	55	25	1	1.00	1.00	53.13132	4
## 66	15	5	90	25	2	1.00	1.00	59.36399	4
## 67	21	3	35	100	3	1.00	1.00	38.83975	4
## 69	16	3	110	100	3	1.00	1.00	46.65884	4
## 70	21	3	60	25	3	1.00	0.75	39.10617	4
## 72	17	3	115	25	1	1.00	0.67	49.78744	4
## 73	17	3	110	25	1	1.00	1.00	51.59219	4

*#From the above results we can say that elementary public schools belongs to cluster 1 because it has highest rating.We need to normalize the data set because the data set is having different range values.*