## PHYS 20323/60323: Fall 2024 - LaTeX Example

- 1. An electron is found to be in the spin state (in the z-basis):  $\chi = A \begin{pmatrix} 3i \\ 4 \end{pmatrix}$ 
  - (a) (5 points) Determine the possible values of A such that the state is normalized.
  - (b) (5 points) Find the expectation values of the operators  $S_x$ ,  $S_y$ ,  $S_z$  and  $\vec{S}^2$ .

The matrix representations in the z-basis for the components of electron spin operators are given by:

$$\mathbf{S}_{x} = \frac{\hbar}{2} \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}; \qquad \mathbf{S}_{y} = \frac{\hbar}{2} \begin{pmatrix} 0 & -i \\ i & 0 \end{pmatrix}; \qquad \mathbf{S}_{z} = \frac{\hbar}{2} \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$$

2. The average electrostatic field in the earth's atmosphere in fair weather is approximately given:

$$\vec{E} = E_0 \left( A e^{-\alpha z} + B e^{-\beta z} \right) \hat{z},\tag{1}$$

where A, B,  $\alpha$ ,  $\beta$  are positive constants and z is the height above the (locally flat) earth surface.

- (a) (5 points) Find the average charge density in the atmosphere as a function of height
- (b) (5 points) Find the electric potential as a function height above the earth.
- 3. The following questions refer to stars in the Table below.

Note: There may be multiple answers.

Name	Mass	Luminosity	Lifetime	Temperature	Radius
β Cyg.	1.3 <i>M</i> <sub>⊙</sub>	$3.5~L_{\odot}$			
$\alpha$ Cen.	1.0 <i>M</i> <sub>⊙</sub>				1 <i>R</i> ⊙
η Car.	60. <i>M</i> <sub>⊙</sub>	$10^6~L_{\odot}$	$8.0 \times 10^5$ years		
$\varepsilon$ Eri.	$6.0~M_{\odot}$	$10^3~L_{\odot}$		20,000 K	
δ Scu.	2.0 <i>M</i> <sub>⊙</sub>		$5.0 \times 10^8$ years		$2~R_{\odot}$
γ Del.	$0.7~M_{\odot}$		$4.5 \times 10^{10}$ years	5000 K	

- (a) (4 points) Which of these stars will produce a planetary nebula.
- (b) (4 points) Elements heavier than *Carbon* will be produced in which stars.