

# Census Pay Predictions

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## Preface

This document and the associated code is based on the Capstone HarvardX Professional Certificate in Data Science (PH125.9x) course work, and additional reading material provided in the course.

The following files (3 types) are included in the upload:

- **CensusPay.rmd** - Markdown for the main summary report file
- **CensusPay.R** - Main R code for the project
- **DatasetProcessingCode.R** - The R code for downloading, cleaning and converting the dataset into tidy form to be used in the project
- **CensusPaySummaryReport.pdf** - Main summary report containing analysis
- **CensusPayExecutionReport.pdf** - Main execution report containing output of the runs

This document does not describe various machine learning terminologies in detail. The appendix has more information on how to get to that information and more.

The code in this project is memory and CPU intensive. The minimum requirements are at least 8 CPU core, 64 GB RAM, and 1 TB of disk space. Anything lower will take excessively long time.

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## Introduction to Census income level predictions

The Current Population Survey (CPS), sponsored jointly by the U.S. Census Bureau and the U.S. Bureau of Labor Statistics (BLS), is the primary source of labor force statistics for the population of the United States. The adult census income data was extracted from the 1994 Census bureau database by Ronny Kohavi and Barry Becker (Data Mining and Visualization, Silicon Graphics).

This machine learning project uses the adult census income data to predict annual money incomes for adults, given a set of 13 employment and demographic attributes. Census money income is defined as income received on a regular basis before payments for personal income taxes, social security, union dues, Medicare deductions, etc. The income levels were categorized into two classes – more than \$50,000, and less than or equal to \$50,000.

More information can be found at <https://www.kaggle.com/uciml/adult-census-income>.

In this project for the Capstone course of the HarvardX Professional Certificate in Data Science (PH125.9x), we will explore the adult census income data set. The objective will be to analyze and model based on the classification of incomes and develop a machine-learning model by creating, training and test sets to predict income levels on a validation set with accuracy of more than 80% and a reasonable sensitivity, and specificity

Here is a glimpse of adultpay dataset. The columns that are of interest are income, age, sex, education.num, education, race, marital.status, relationship, workclass, hours.per.week and occupation. There are 32,561 rows and 13 columns

```
library(tidyverse)
library(caret)
# inspect the out-of-box original dataset
glimpse(adultpay)
```

```
## Rows: 32,561
## Columns: 15
## $ age          <int> 90, 82, 66, 54, 41, 34, 38, 74, 68, 41, 45, 38, 52, 32, ~
## $ workclass    <chr> "?", "Private", "?", "Private", "Private", "Private", "~
## $ fnlwgt       <int> 77053, 132870, 186061, 140359, 264663, 216864, 150601, ~
## $ education    <chr> "HS-grad", "HS-grad", "Some-college", "7th-8th", "Some--
## $ education.num <int> 9, 9, 10, 4, 10, 9, 6, 16, 9, 10, 16, 15, 13, 14, 16, 1~
## $ marital.status <chr> "Widowed", "Widowed", "Widowed", "Divorced", "Separated~
## $ occupation   <chr> "?", "Exec-managerial", "?", "Machine-op-inspct", "Prof~
## $ relationship <chr> "Not-in-family", "Not-in-family", "Unmarried", "Unmarri~
## $ race          <chr> "White", "White", "Black", "White", "White", "White", "~
## $ sex           <chr> "Female", "Female", "Female", "Female", "Female", "Fema~
## $ capital.gain  <int> 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0~
## $ capital.loss  <int> 4356, 4356, 4356, 3900, 3900, 3770, 3770, 3683, 3683, 3~
## $ hours.per.week <int> 40, 18, 40, 40, 40, 45, 40, 20, 40, 60, 35, 45, 20, 55, ~
## $ native.country <chr> "United-States", "United-States", "United-States", "Uni~
## $ income        <chr> "<=50K", "<=50K", "<=50K", "<=50K", "<=50K", "<=50K", "~
```

We will start with data exploration and cleaning unwanted data and processing. Then we will mimic the ultimate evaluation process by splitting the data into two parts - training and validation and act as if we don't know the outcome for the validation set. We will split the dataset once we cleaned and processed the dataset. We want the test set to be large enough so that we obtain a stable prediction without fitting an impractical number of models. We will then progressively apply various algorithms on the training set and test the predictions on the test set and improve on the overall accuracy.

We will choose 13 attributes, income being the outcome and the rest 12 attributes being the predictors or features. After perusing the dimensions, we will randomly choose 10% of the dataset to be the test set and remaining 90% will be the training set. 90% is sizable enough to run various algorithms like lm, glm,nb, knn, rpart, and random forest with some tuning.

```
library(tidyverse)
library(gridExtra)
library(kableExtra)
# inspect dimensions for the cleaned, training and validation datasets
dim(adultpayclean)
```

```
## [1] 29170    13
```

```
dim(adultpayclean_train)
```

```
## [1] 26252    13
```

```
dim(adultpayclean_validation)
```

```
## [1] 2918    13
```

```
# check for NAs and verify there aren't any in the cleaned dataset
colSums(is.na(adultpayclean))
```

```
##          age          fnlwgt          education          eduyears maritalstatus
```

```
##           0           0           0           0           0
##  occupation  relationship      race      sex  hoursperweek
##           0           0           0           0           0
##      native      income      class
##           0           0           0
```

This is a classification problem and the outcome is binary (income above-50K or at-or-below-50K). On reviewing the summary of the dataset we have a choice of predictors. We will keep only USA specific data. Almost all of the predictors have data spread out. There are no NAs in the dataset. There is sufficient degree of variability.

```
# statistics for the clean dataset
summary(adultpayclean)
```

```
##           age           fnlwgt           education           eduyears
##  Min.      :17.00   Min.      : 12285   HSgrad      :9702   Min.      : 1.00
##  1st Qu.:28.00   1st Qu.: 115895   Somecollege:6740   1st Qu.: 9.00
##  Median :37.00   Median : 176730   Bachelors   :4766   Median :10.00
##  Mean   :38.66   Mean   : 187069   Masters     :1527   Mean   :10.17
##  3rd Qu.:48.00   3rd Qu.: 234139   Assocvoc    :1289   3rd Qu.:12.00
##  Max.    :90.00   Max.    :1484705   11th        :1067   Max.    :16.00
##                                     (Other)    :4079
##           maritalstatus           occupation           relationship
##  Divorced      : 4162   Profspecialty :5359   Husband       :11861
##  MarriedAFspouse : 23   Execmanagerial:3735   Notinfamily    : 7528
##  Marriedcivspouse :13368   Craftrepair   :3685   Otherrelative : 696
##  Marriedspouseabsent: 253   Admclerical   :3449   Ownchild      : 4691
##  Nevermarried    : 9579   Sales         :3364   Unmarried     : 3033
##  Separated       : 883   Otherservice   :2777   Wife          : 1361
##  Widowed        : 902   (Other)       :6801
##           race           sex           hoursperweek           native
##  AmerIndianEskimo: 296   Female: 9682   Min.      : 1.00   Length:29170
##  AsianPacIslander: 292   Male   :19488   1st Qu.:40.00   Class :character
##  Black           : 2832   Mean   :40.45   Median :40.00   Mode  :character
##  Other           : 129   3rd Qu.:45.00
##  White           :25621   Max.    :99.00
##
##           income           class
##  Above50K : 7171   Private :21794
##  AtBelow50K:21999   Selfempnotinc: 2313
##                                     Localgov      : 1956
##                                     Stategov      : 1210
##                                     Selfempinc    : 991
##                                     Federalgov    : 886
##                                     (Other)      : 20
```

We can also see the number or above-50K income is significantly less than (25%) the at-or-below-50K income. This implies that there is prevalence of at-or-below-50K group in the dataset.

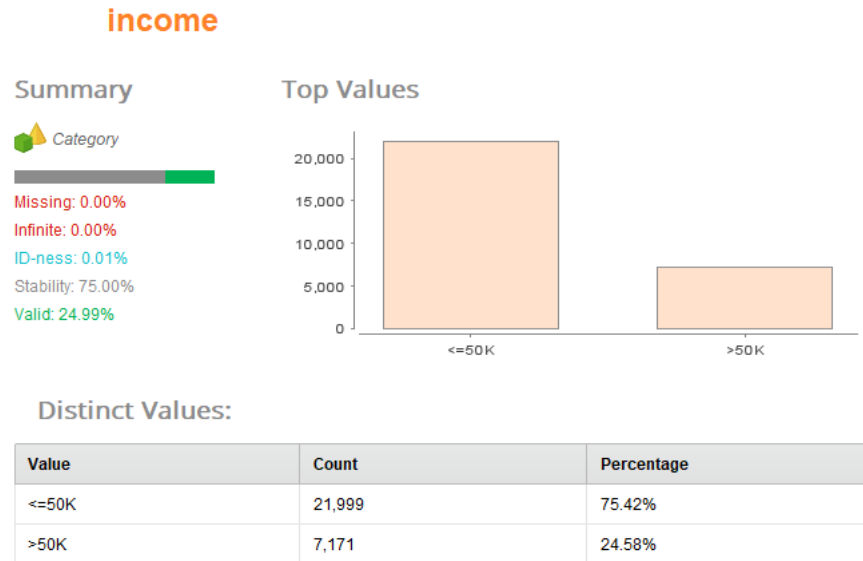


Figure 1: Income distribution

So we begin...

## Analysis

### Data Exploration, Processing and, Feature engineering

The adult pay dataset from census bureau is a ML ready database. For convenience, I have downloaded it from kaggle and stored in the same github repository as this code and markdown. The dataset is in zip format and is downloaded from <https://github.com/rajeshharidas/havardxwork2/blob/main/adult.csv.zip>. Then it is read into a data frame. The data is ML ready for the most part. However, there are some additional cleaning tasks needed before using the dataset. This processing is done in DatasetProcessingCode.R file. Code fragment is shown below. We perform the following cleaning tasks

- 1) Filter to keep only USA data
- 2) Remove all ? marks data from all the columns. Impute ? values to the modes in categorical columns like class, and occupation
- 3) Remove intermediate columns and columns that are not used in the project
- 4) Rename column names and column values to exclude non-alphanumeric characters
- 5) convert character labels to factors

```
# dataset wrangling and tidying

adultpayclean <- adultpay %>%
  filter(native.country == "United-States") %>%
  mutate(class = ifelse(workclass == "?", getmode(adultpay$workclass),
    ↪ str_replace_all(workclass,
      ↪ "_", ""))) %>%
  dplyr::select(-workclass, -capital.gain, -capital.loss) %>%
  rename(c(eduyears = education.num, maritalstatus = marital.status, hoursperweek =
    ↪ hours.per.week,
```

```

    native = native.country)) %>%
mutate(maritalstatus = ifelse(maritalstatus == "?", getmode(adultpay$maritalstatus),
    str_replace_all(maritalstatus, "-", ""))) %>%
mutate(occupation = ifelse(occupation == "?", getmode(adultpay$occupation),
    ↪ str_replace_all(occupation,
    "-", ""))) %>%
mutate(education = ifelse(education == "?", getmode(adultpay$education),
    ↪ str_replace_all(education,
    "-", ""))) %>%
mutate(relationship = ifelse(relationship == "?", getmode(adultpay$relationship),
    str_replace_all(relationship, "-", ""))) %>%
mutate(native = ifelse(native == "?", "Unknown", str_replace_all(native, "-",
    ""))) %>%
mutate(income = ifelse(income == "?", getmode(adultpay$income),
    ↪ str_replace_all(income,
    "<=50K", "AtBelow50K"))) %>%
mutate(income = ifelse(income == "?", "Unknown", str_replace_all(income, ">50K",
    "Above50K")))

```

After performing this cleaning we see 29170 rows and 13 columns. We further analyze the makeup of the categorical columns.

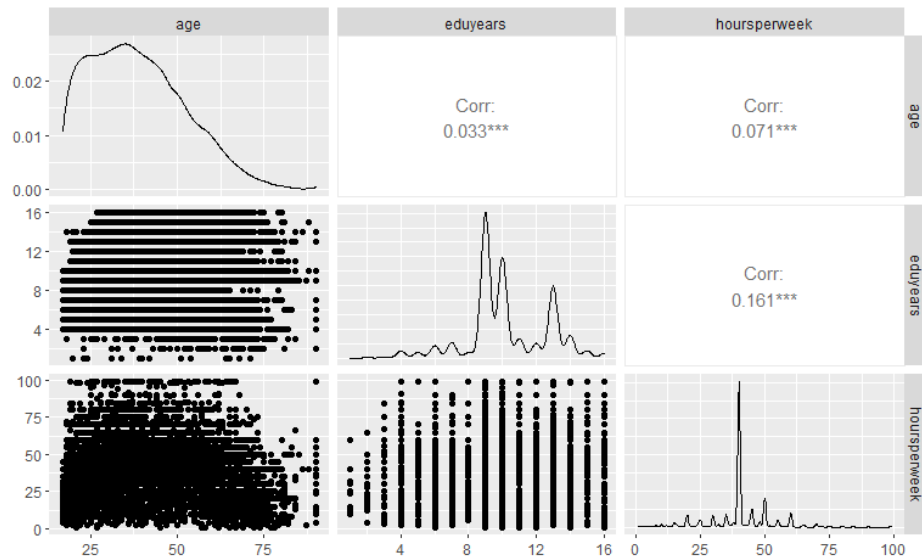


Figure 2: Comparison plots for numerical variables

Here are the comparison plots (generated by GGally package) for the numerical variables like age, edueyears and hoursperweek. There are very less people who have less than 4 years of education. Most people complete at least 9-10 years of education between 25-80 years age. Significant group of people stopped at elementary school. Significant group of people put in more than 40 hours per week past their retirement age. People who have 8-10 years of education put in more hours per week than others.

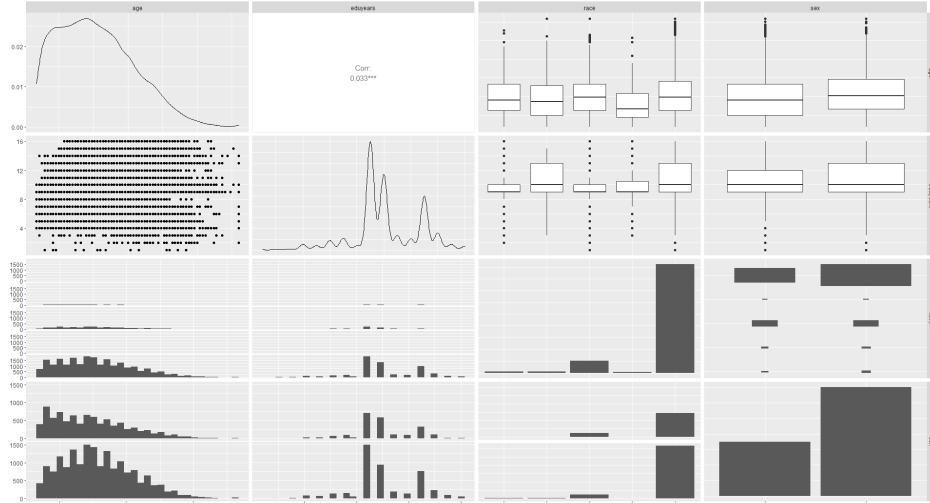


Figure 3: Comparison plots for categorical variables

Here are the comparison plots for the categorical variables. On an average white-Americans and black-Americans are gainfully employed at similar ages. More black and white people are employed past their retirement age when compared to other races. Similarly, more females are employed past their retirement age in comparison to male counterparts (outliers). More white males are employed than white females, however, the number of black males and females are about the same. There are more middle-aged men and younger females in the labor force.

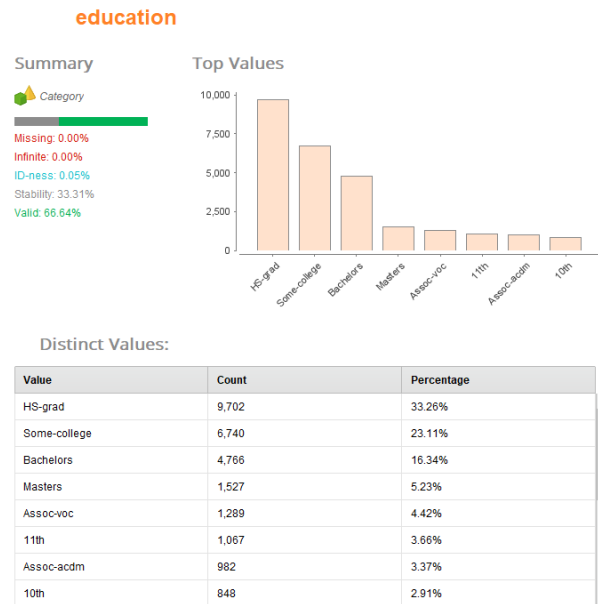


Figure 4: Education statistics

The number of high-school graduates are most frequent than other groups. There are 2 income distributions for education. One by the level of education and one by the number of years spent in education. Sure enough, most of the above-50K earners have at least high-school education. Bachelors and some college have more above-50K earners than other categories.



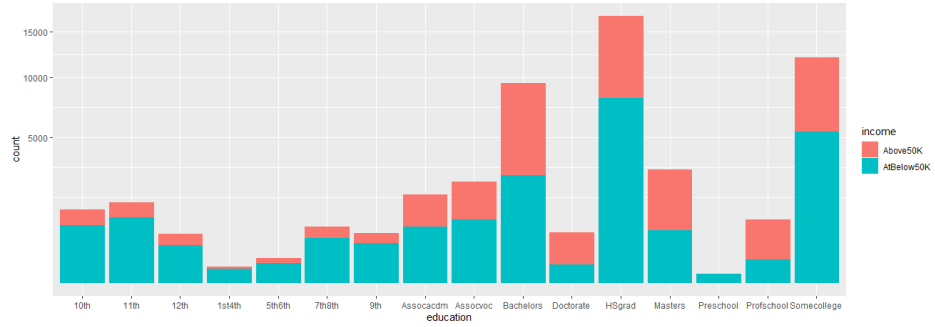


Figure 5: Education income distribution

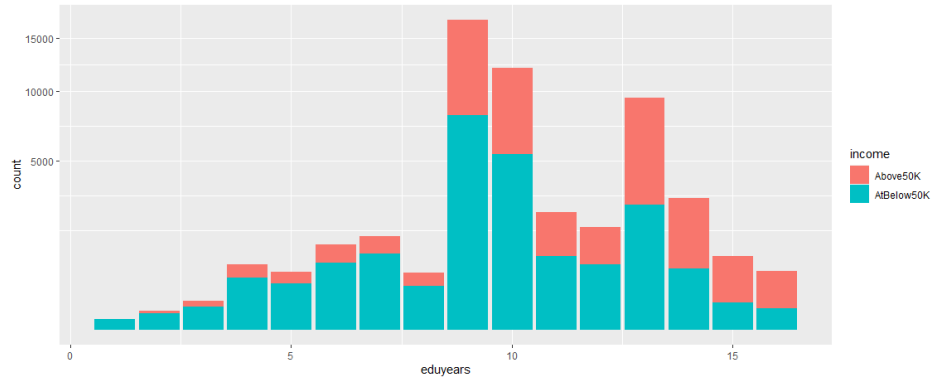


Figure 6: Education income distribution

Interestingly enough, in comparison to Bachelors and some college, group with masters have lesser above-50K. Additionally, the group that has at least 12 years of education have more above-50K than others. On an average the participants have 10 years of education with a standard deviation of 2.4. There are more at-or-below 50K earners in the high-school grad and less than 10 years of education categories.

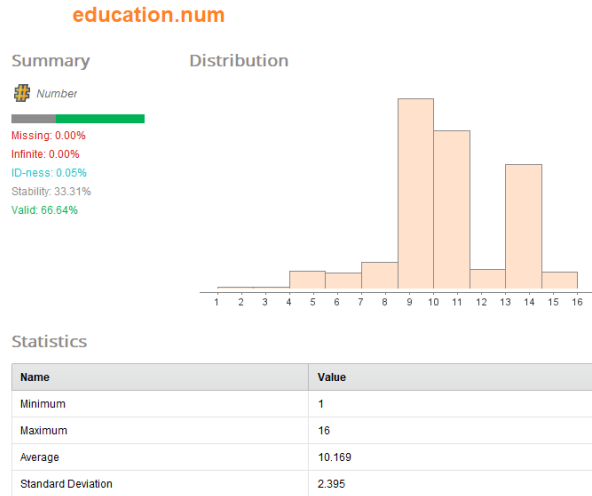


Figure 7: Years of education

The rest of the groups have sparse data. This could be because of missing or bad data that was removed during initial cleaning before it was loaded into kaggle.

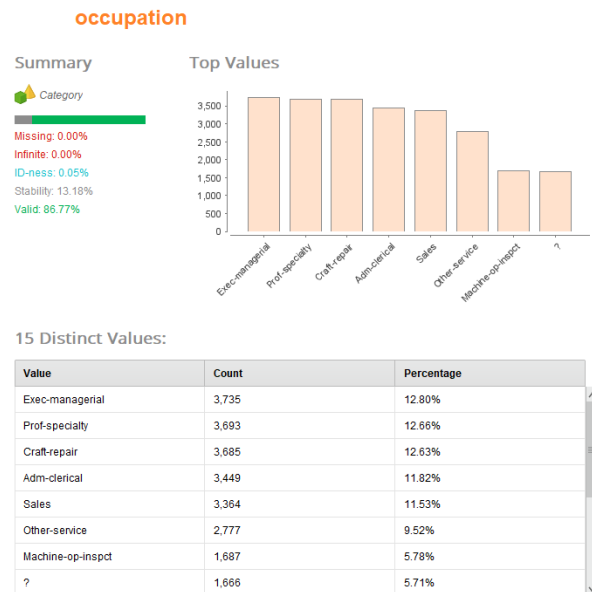


Figure 8: Occupation frequency

There are more executive and managerial occupations followed by professionals.

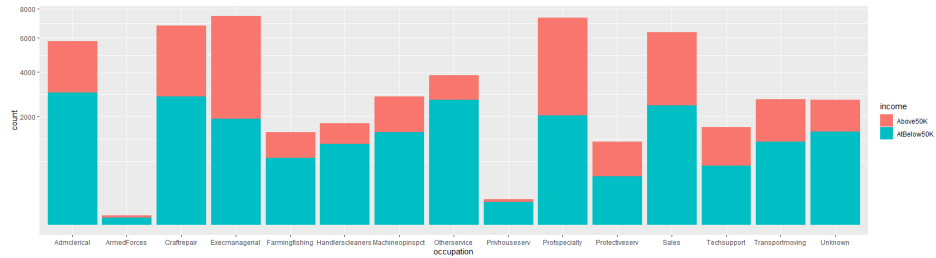


Figure 9: Occupation distribution

The same groups earn more and are in the above-50K category. There are fairly significant number of at-or-below-50K earners in the other categories. There are 1600 or so missing data (? or Unknown). This makes up 5-6% of the cleaned dataset.

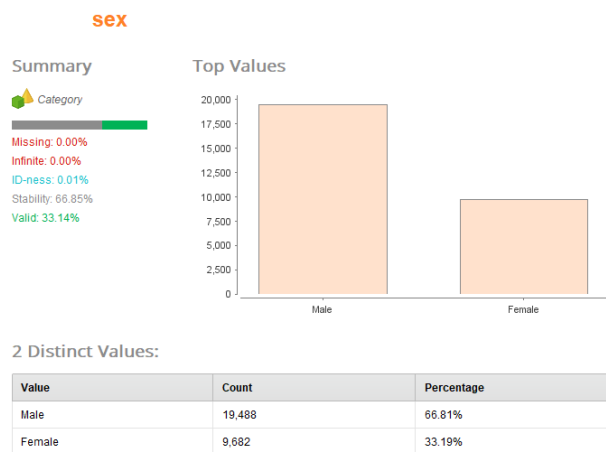


Figure 10: Sex feature characteristics

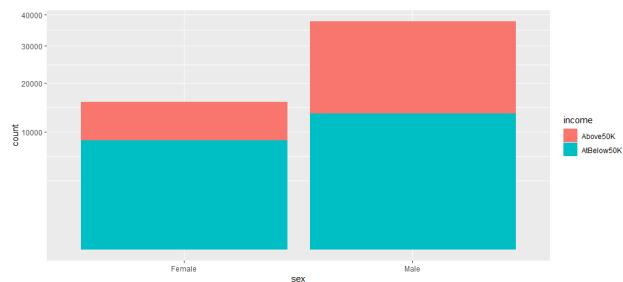


Figure 11: Sex feature characteristics

There are 67% more males in the workforce than females. The distribution also indicates that the number of males at above-50K are more than the number of females. Additionally, there are more males at-or-below-50K than females as well.

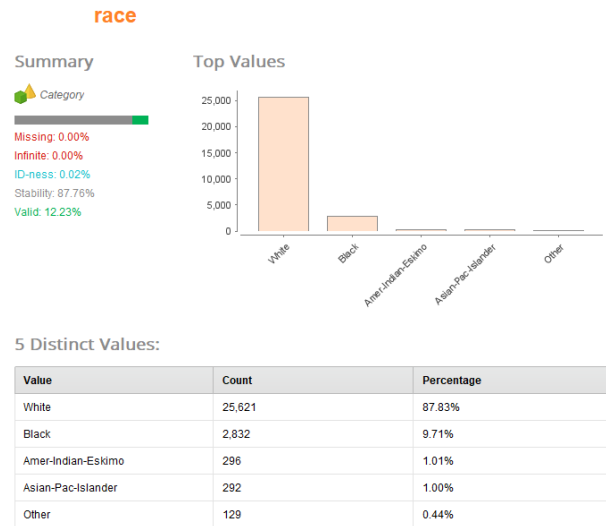


Figure 12: Race distribution

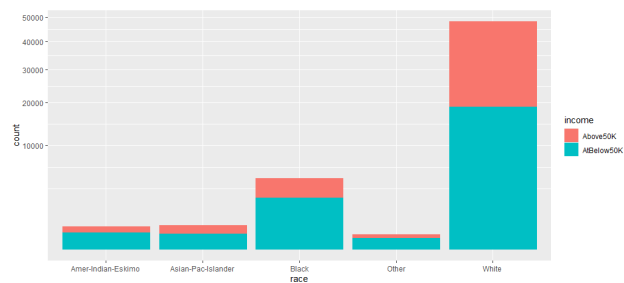


Figure 13: Race distribution

There are more white-Americans in the labor force in both the above-50K and at-or-below-50K categories. Black-Americans and other race follow next. The proportion of above-50K earners are lesser in other races when compared to white-Americans.

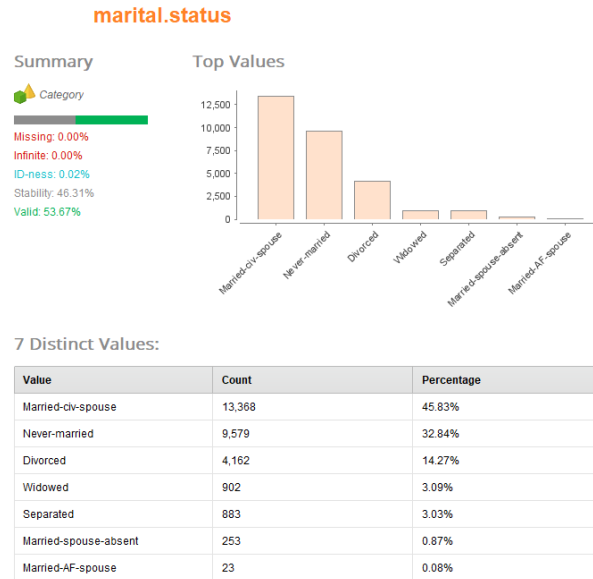


Figure 14: Marital Status frequency

The number of married with civilian spouses are more than any other groups in labor force. The number of above-50K and at-or-below-50K earners are also more in this group when compared to others. Singles follow next.

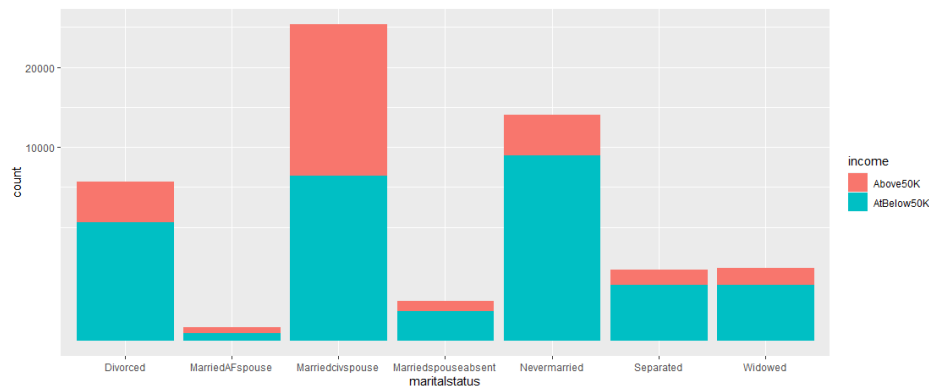


Figure 15: Marital Status distribution

The number of at-or-below-50K are more than the above-50K in the singles group and most of them are younger population. The plot also suggests most of this group is below 25 years age group. This can be correlated with the income by age group chart. The number of married with military spouses is less which may be due to lack of data.

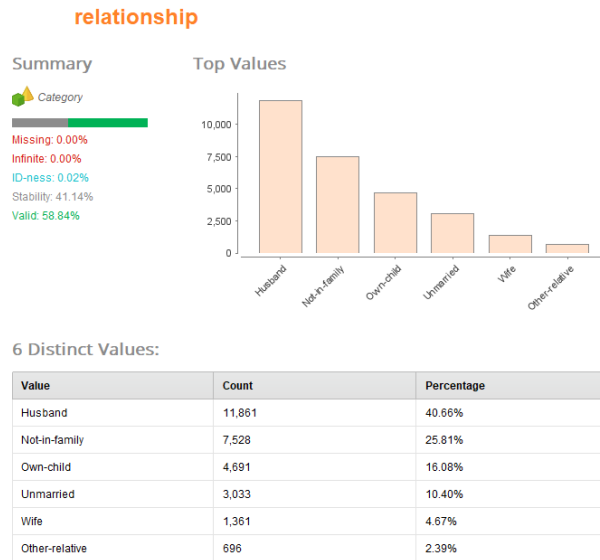


Figure 16: Relationship distribution

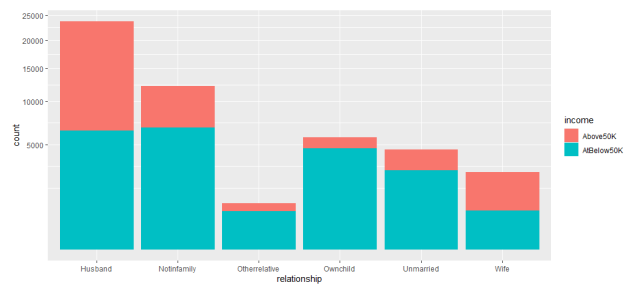


Figure 17: Relationship distribution

The number of husbands who earn more than 50K and at-or-below-50K are also more than the number of wives. Unmarried individuals also are more in the at-or-below-50K category.

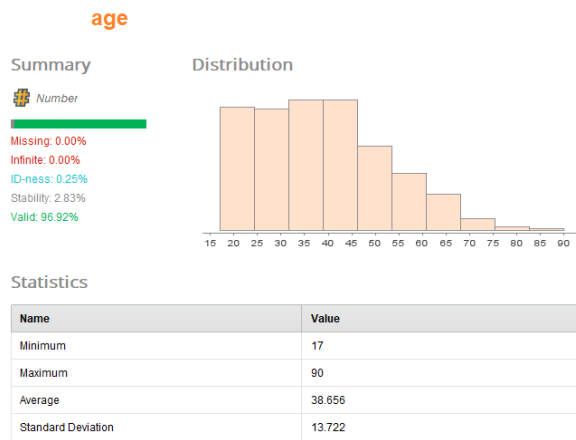


Figure 18: Age distribution

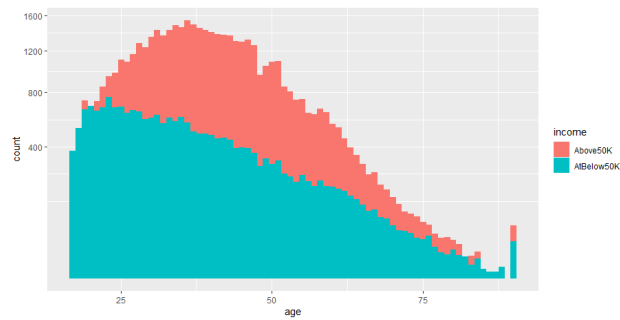


Figure 19: Age distribution

The number of people from age 30-45 are the most frequent in the distribution and the same group have more above-50K incomes. There are 12 outliers in the age group above 80 who earn Above-50K. There are similar outliers in age-sex and age-race comparisons. However, the numbers are not significant enough to skew the distributions.

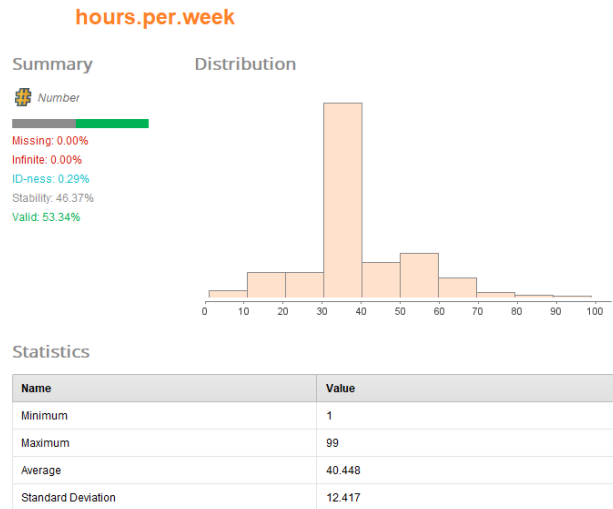


Figure 20: Hours worked

On a average most participants worked 40 hours a week followed by 50-60 hours.

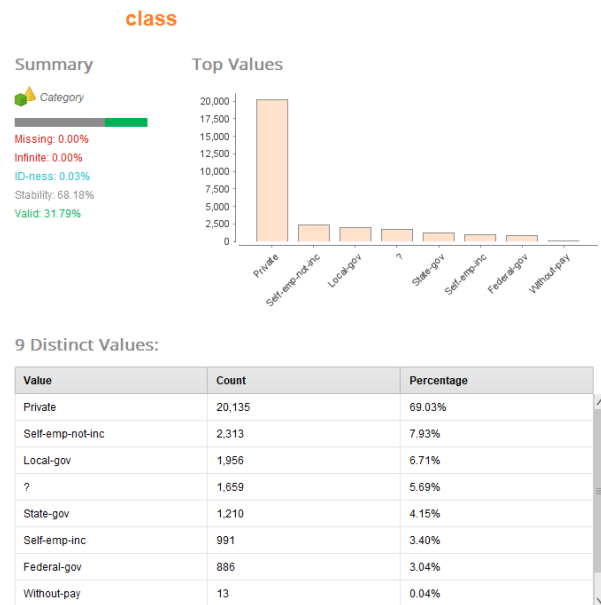


Figure 21: Class distribution



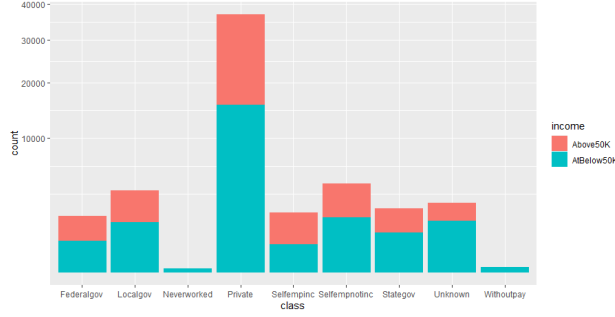


Figure 22: Class distribution

The number of private employer workers are more than other categories. They also earn more above-50K and at-or-below-50K than other categories.

As shown above the occupation and class categorical columns have more than 1600 Unknown data. As these are categorical data, we will impute them using mode. However, as this is 6% of the data, adding these to the predictor columns could skew the predictions and introduce errors. We will exclude this from our list of predictors. We will experiment with these two features in our final model. We also removed capital gains and loss columns because we do not have good realistic data for both of these columns. The final list of predictors/features used to predict the outcome income level are age, education, years of education (a.k.a. eduyears), maritalstatus, relationship, race, sex, and hoursperweek. As analyzed in the above section, there is sufficient degree of variability and correlation between these features and how they impact the income levels based on socio-economic and cultural factors.

## Process

The high-level process methodology used in this project is along the same lines as the CRISP-DM (Cross Industrial Standard Process for Data Mining) methodology. We got a business understanding of the problem we are trying to solve. We analyzed the raw data. Next we prepare the dataset from the raw data.

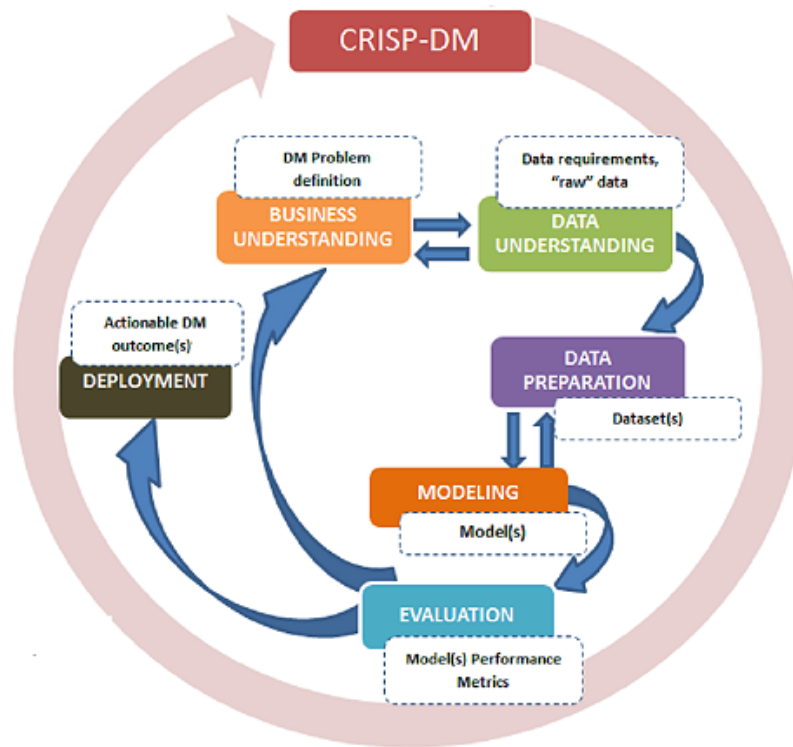


Figure 23: Process Methodology

The code `DatasetProcessingCode.R` downloads the dataset from a convenient location in github (originally downloaded from kaggle) and then unzips it and converts the dataset into a R data frame. It then does extensive cleaning, processing and munging of the data to make it tidy and meaningful for analysis. It then splits the original dataset into training and validation datasets. All analysis is done on this training dataset. Once the training is done the validation is done on the test dataset.

The caret package includes the function `createDataPartition` that helps us generate indexes for randomly splitting the data into training and test sets. The argument `times` is used to define how many random samples of indexes to return, the argument `p` is used to define what proportion of the data is represented by the index, and the argument `list` is used to decide if we want the indexes returned as a list or not. We can use the `test_index` from the `createDataPartition` function call to define the training and test sets.

```
# split dataset into training and validation sets

set.seed(1, sample.kind = "Rounding")

test_index <- createDataPartition(y = adultpayclean$income, times = 1, p = 0.1, list =
  ↪ FALSE)

adultpayclean_train <- adultpayclean[-test_index, ]

adultpayclean_validation <- adultpayclean[test_index, ]
```

```
dim(adultpayclean)
# [1] 29170 13

dim(adultpayclean_train)
# [1] 26252 13

dim(adultpayclean_validation)
# [1] 2918 13
```

We then develop an algorithm using only the training set. Once we are done developing the algorithm, we then freeze it and evaluate it using the test set.

The simplest way to evaluate the algorithm for the adultpay dataset is by simply reporting the proportion of cases that were correctly predicted in the test set. This metric is referred to as overall accuracy. Some times accuracy is skewed due to prevalence or bias of one class or the other, therefore we will weigh in on sensitivity and specificity (check true/false positives and true/false negatives) when choosing the final model.

We will also use F1 measure to validate the accuracy of the sensitivity and specificity and see if we have a good precision. F1 score is a combination of two important error metrics: Precision and Recall. Thus, it can be considered as the Harmonic mean of Precision and Recall error metrics for an imbalanced dataset with respect to binary classification of data. As income level has only 30% data for above-50K class this score is useful. The highest possible value of an F-score is 1.0, indicating perfect precision and recall, and the lowest possible value is 0. Higher the precision the better.

We will also use a widely used plot receiver operating characteristic (ROC) curve. Receiver Operating Characteristic curves are a popular way to visualize the trade-offs between sensitivity and specificity in a binary classifier. The ROC curve plots sensitivity (TPR) versus 1 - specificity or the false positive rate (FPR). This also gives us Area under the curve (a.k.a. AUC). The AUC summarizes ROC in a single value. The probabilistic interpretation is that if you randomly choose a positive case and a negative case, the probability that the positive case outranks the negative case according to the classifier is given by the AUC. Higher the AUC score the better. This indicates that the model has higher chances for getting correct predictions.

## Model Creation

### Simplest model using random sampling

We are now going to evaluate various algorithms progressively

We first start with a simple model. We sample randomly for the desired outcome. We then compare it with the actual outcomes and take a mean of the results. The result is 50% which is expected for guessing a binary outcome. Its akin to tossing a coin and getting head or tail. The chances are 50/50.

```
# Plain old guessing

seat_of_the_pants <- sample(c("Above50K", "AtBelow50K"), length(test_index), replace =
  ↪ TRUE) %>%
  factor(levels = levels(adultpayclean_validation$income))

mean(seat_of_the_pants == adultpayclean_validation$income)

# [1] 0.5010281
```

```
# build a confusion matrix for this simple model

cm <- confusionMatrix(data = seat_of_the_pants, reference =
  ↪ adu1tpayclean_validation$income)

# cm
```

#### Confusion Matrix and Statistics

	Reference	
Prediction	Above50K	AtBelow50K
Above50K	347	1087
AtBelow50K	371	1113

Accuracy : 0.5003  
 95% CI : (0.482, 0.5186)

No Information Rate : 0.7539  
 P-Value [Acc > NIR] : 1  
 Kappa : -0.0081  
 McNemar's Test P-Value : <2e-16  
 Sensitivity : 0.4833  
 Specificity : 0.5059  
 Pos Pred Value : 0.2420  
 Neg Pred Value : 0.7500  
 Prevalence : 0.2461  
 Detection Rate : 0.1189  
 Detection Prevalence : 0.4914  
 Balanced Accuracy : 0.4946  
 'Positive' Class : Above50K

```
p <- 0.1

n <- length(test_index)

y_hat <- sample(c("Above50K", "AtBelow50K"), n, replace = TRUE, prob = c(p, 1 - p)) %>%
  factor(levels = levels(adu1tpayclean_validation$income))

mean(y_hat == adu1tpayclean_validation$income)

# [1] 0.7076765

p <- 0.9

n <- length(test_index)

y_hat <- sample(c("Above50K", "AtBelow50K"), n, replace = TRUE, prob = c(p, 1 - p)) %>%
  factor(levels = levels(adu1tpayclean_validation$income))

mean(y_hat == adu1tpayclean_validation$income)

# [1] 0.2964359
```

```
f1_guess
# [1] 0.3224907

# Area under the curve

auc_guess <- auc(ifelse(adultpayclean_validation$income == "Above50K", 1, 2),
  ↪ ifelse(seat_of_the_pants ==
    "Above50K", 1, 2))

auc_guess

# Area under the curve: 0.4946
```

We then construct the confusion matrix, which basically tabulates each combination of prediction and actual value. We see that the above-50K and at-or-below-50K are almost evenly distributed with a slightly higher prevalence of the at-or-below-50K income level.

We can verify this by adjusting the probability of our sampling to skew towards above-50K vs at-or-below-50K and vice-versa.

Prevalence can result in skewed results. We will keep an eye on the other metrics like sensitivity and specificity in addition to accuracy. In this case low prevalence matches with the expected accuracy.

The F1 score for this guessing is 0.3224 and Area under the curve is 0.4946. This is in line with our expectations for mere guessing of the outcome.

Our goal is to improve the accuracy > 80% while keeping sensitivity and specificity under check. Hence we further analyze the impact of other features on the income levels.

## Logistic regression using linear models

We will start with a simple logistic model - linear model. We use the features age, education, eduyears, sex, race, maritalstatus, relationship and hoursperweek.

Both linear and logistic regressions provide an estimate for the conditional expectation:

$$E(Y | X = x)$$

which in the case of binary data is equivalent to the conditional probability:

$$Pr(Y = 1 | X = x)$$

We can use this to arrive at  $y\_hat\_logit$ . Since we have 8 features  $X = x$  is more like  $X_i = x_i$  where  $i$  is from 1 to 8.

The `lm` function applies this formula on `adultpay` dataset. Where  $y$  is the outcome and  $\epsilon$  is the error. Sum of  $\beta_1 x_1$  through  $\beta_8 x_8$  is a linear combination of  $x_1$  through  $x_8$ .

$$y = \alpha + \beta_1(\text{age}) + \beta_2(\text{eduyears}) + \beta_3(\text{sex}) + \beta_4(\text{race}) + \beta_5(\text{hoursperweek}) + \beta_6(\text{maritalstatus}) + \beta_7(\text{relationship}) + \beta_8(\text{education}) + \epsilon$$

```

# linear model

lm_fit <- adu1tpayclean_train %>%
  mutate(y = as.numeric(income == "Above50K")) %>%
  lm(y ~ age + eduyears + sex + race + hoursperweek + maritalstatus + relationship +
    education, data = .)

p_hat_logit <- predict(lm_fit, newdata = adu1tpayclean_validation)

y_hat_logit <- ifelse(p_hat_logit > 0.5, "Above50K", "AtBelow50K") %>%
  factor

accuracy_lm <- confusionMatrix(y_hat_logit,
  ↪ adu1tpayclean_validation$income)$overall[["Accuracy"]]

accuracy_lm

# [1] 0.8153

f1_lm

# [1] 0.54128

# Area under the curve: 0.81709

```

#### Confusion Matrix and Statistics

	Reference	
Prediction	Above50K	AtBelow50K
Above50K	318	139
AtBelow50K	400	2061

Accuracy : 0.8153  
 95% CI : (0.8007, 0.8292)  
 No Information Rate : 0.7539  
 P-Value [Acc > NIR] : 1.243e-15  
 Kappa : 0.4327  
 McNemar's Test P-Value : < 2.2e-16  
 Sensitivity : 0.4429  
 Specificity : 0.9368  
 Pos Pred Value : 0.6958  
 Neg Pred Value : 0.8375  
 Prevalence : 0.2461  
 Detection Rate : 0.1090  
 Detection Prevalence : 0.1566  
 Balanced Accuracy : 0.6899  
 'Positive' Class : Above50K

The accuracy for this model is 0.8153 however, sensitivity is 0.4429 and specificity is 0.9368. This indicates this model has higher ratio of negative outcomes than positive outcomes. It does have better accuracy, confidence interval, and F1 score than plain old guessing. Prevalence remains the same. AUC has improved as well. Lets see if we can do better

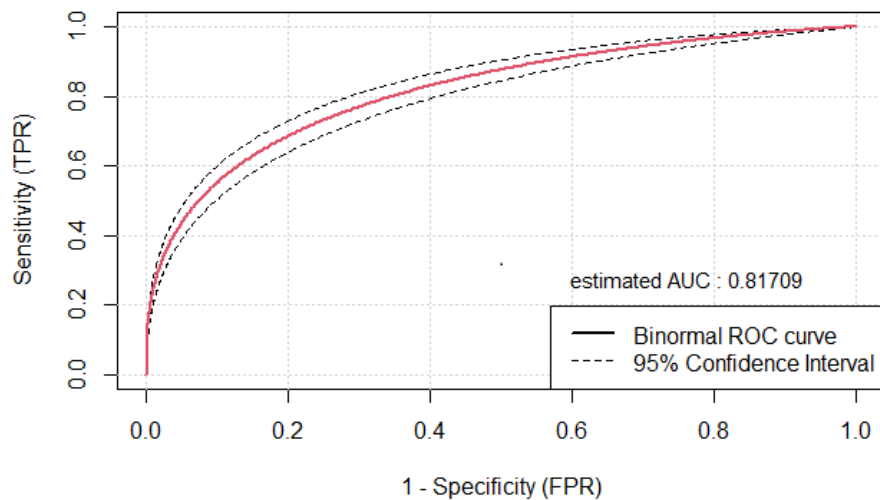


Figure 24: LM classification summary

We will now experiment with the general linear model (glm). We will be consistent with the features used across all algorithms. Glm uses the following formula

$$\log \left[ \frac{P(y=1)}{1-P(y=1)} \right] = \alpha + \beta_1(\text{age}) + \beta_2(\text{eduyears}) + \beta_3(\text{sex}) + \beta_4(\text{race}) + \beta_5(\text{hoursperweek}) + \beta_6(\text{maritalstatus}) + \beta_7(\text{relationship}) + \beta_8(\text{education})$$

Where  $y$  is the outcome and  $\epsilon$  is the error. Sum of  $\beta_1 x_1$  through  $\beta_8 x_8$  is a linear combination of  $x_1$  through  $x_8$

Logistics model assures that the estimate  $Pr(Y = 1 | X = x)$  is between 0 and 1. Glm converts probability into log odds -  $\log \left[ \frac{P(y=1)}{1-P(y=1)} \right]$ . We will then translate the probability into a decision rule to predict Above50K if probability is  $> 0.5$ . We then compare the predictions to the outcomes using confusionMatrix.

```
# general linear model

glm_fit <- adultpayclean_train %>% glm_fit <- adultpayclean_train %>%
mutate(y = as.numeric(income == "Above50K")) %>% mutate(y = as.numeric(income
mutate(y = as.numeric(income == "Above50K")) %>% == "Above50K")) %>%
glm(y ~ age + eduyears + sex + race + hoursperweek + maritalstatus + relationship +
  education, data = ., family = "binomial")

p_hat_logit <- predict(glm_fit, newdata = adultpayclean_validation)

y_hat_logit <- ifelse(p_hat_logit > 0.5, "Above50K", "AtBelow50K") %>%
  factor

accuracy_glm <- confusionMatrix(y_hat_logit,
  ↪ adultpayclean_validation$income)$overall[["Accuracy"]]

accuracy_glm
# [1] 0.8105
```

```
f1_glm
```

```
# [1] 0.50135
```

```
# Area under the curve: 0.81817
```

#### Confusion Matrix and Statistics

	Reference	
Prediction	Above50K	AtBelow50K
Above50K	278	113
AtBelow50K	440	2087

Accuracy : 0.8105  
95% CI : (0.7958, 0.8246)  
No Information Rate : 0.7539  
P-Value [Acc > NIR] : 1.758e-13  
Kappa : 0.3967  
Mcnemar's Test P-Value : < 2.2e-16  
Sensitivity : 0.38719  
Specificity : 0.94864  
Pos Pred Value : 0.71100  
Neg Pred Value : 0.82588  
Prevalence : 0.24606  
Detection Rate : 0.09527  
Detection Prevalence : 0.13400  
Balanced Accuracy : 0.66791  
'Positive' Class : Above50K

glm produces accuracy of 0.8105, however, specificity 0.94864 is still higher than sensitivity 0.38719 and prevalence about the same. CI and F1 scores can be better. AUC can also do better. We can do better!



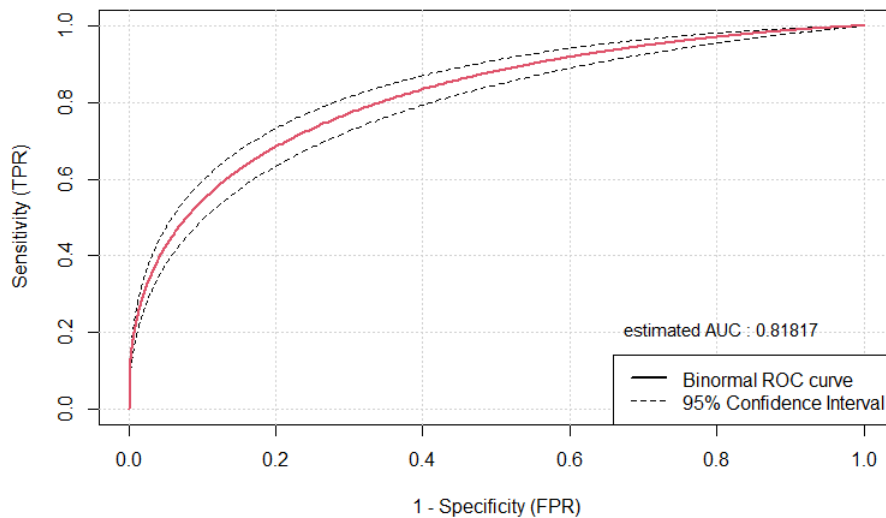


Figure 25: GLM classification summary

## Naive Bayes

We will now experiment with generative models like naive bayes classification. It assumes the features that go into the model are independent of each other. That is changing the value of one feature, does not directly influence or change the value of any of the other features used in the algorithm. When we analyzed the dataset it didn't appear to have independent features. An example of dependent feature would be age and education years, age and marital status etc. However, let's see how naive bayes performs with this assumption.

```
# Naive Bayes

train_nb <- adu1tpayclean_train %>%
  mutate(y = as.factor(income == "Above50K")) %>%
  naiveBayes(y ~ age + eduyears + sex + race + hoursperweek + maritalstatus +
    ↪ relationship +
    education, data = .)

y_hat_nb <- predict(train_nb, newdata = adu1tpayclean_validation)

cm_tab <- table(adu1tpayclean_validation$income == "Above50K", y_hat_nb)

cm_nb <- confusionMatrix(cm_tab)

## Accuracy : 0.8009

f1_nb

# [1] 0.86064

# Area under the curve: 0.80143
```

## Confusion Matrix and Statistics

```

y_hat_nb
  FALSE TRUE
FALSE 1794 406
TRUE   175 543

```

```

Accuracy : 0.8009
 95% CI : (0.7859, 0.8152)
No Information Rate : 0.6748
P-Value [Acc > NIR] : < 2.2e-16
      Kappa : 0.5158
McNemar's Test P-Value : < 2.2e-16
Sensitivity : 0.9111
Specificity : 0.5722
Pos Pred Value : 0.8155
Neg Pred Value : 0.7563
Prevalence : 0.6748
Detection Rate : 0.6148
Detection Prevalence : 0.7539
Balanced Accuracy : 0.7417
'Positive' Class : FALSE

```

Naive bayes gives us an accuracy of 0.8009 with a lower prevalence than other algorithms but higher than plain guessing. However the confidence interval is lower and accuracy of the prediction is lower too. There are more false negatives as well. F1 score has increased. This indicates there are more true positives as well. However, given that this is an imbalanced dataset, we can try other advanced algorithms and compare this later.

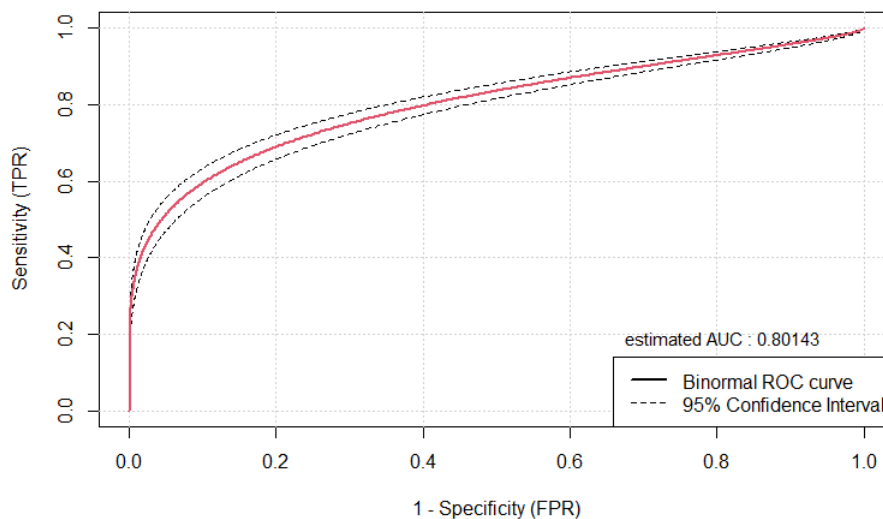


Figure 26: naive bayes classification summary

Lets explore k-nearest model now with same feature set. We will use cross-validation to tune the k parameter. By default, the cross validation is performed by taking 25 bootstrap samples comprised of 25% of the

observations. For the kNN method, the default is to try  $k=5,7,9$ . We change this using the `tuneGrid` parameter. We will try the  $k$  values in the following sequence  $k = \text{seq}(3, 71, 2)$ . Running this code will take several seconds. This is because when we run the algorithm, we will have to compute a distance between each observation in the test set and each observation in the training set. There are a lot of computations. Therefore, we use the `trainControl` function to make the code above go a bit faster by using, 10-fold cross validation. This means we have 10 samples using 10% of the observations each. We set the seed because cross validation is a random procedure and we want to make sure the result here is reproducible

## K-Nearest Neighbors

```
# KNN

temp <- adultpayclean_train %>%
  mutate(y = as.factor(income == "Above50K"))

set.seed(2008)

control <- trainControl(method = "cv", number = 10, p = 0.9)

train_knn <- train(y ~ age + eduyears + sex + race + hoursperweek + maritalstatus +
  relationship + education, method = "knn", data = temp, tuneGrid = data.frame(k =
  ↪ seq(3,
    71, 2)), trControl = control)

train_knn$bestTune

y_hat_knn <- predict(train_knn, adultpayclean_validation, type = "raw")

accuracy_knn <- confusionMatrix(y_hat_knn, as.factor(adultpayclean_validation$income ==
  "Above50K"))$overall[["Accuracy"]]

ggplot(train_knn, highlight = TRUE)

accuracy_knn

# [1] 0.80535

f1_knn

# [1] 0.87522

# Area under the curve: 0.78721
```

The  $k$  parameter that lead to maximum accuracy can be obtained by `bestTune`. The plot for that is shown in the figure “KNN tuning”.

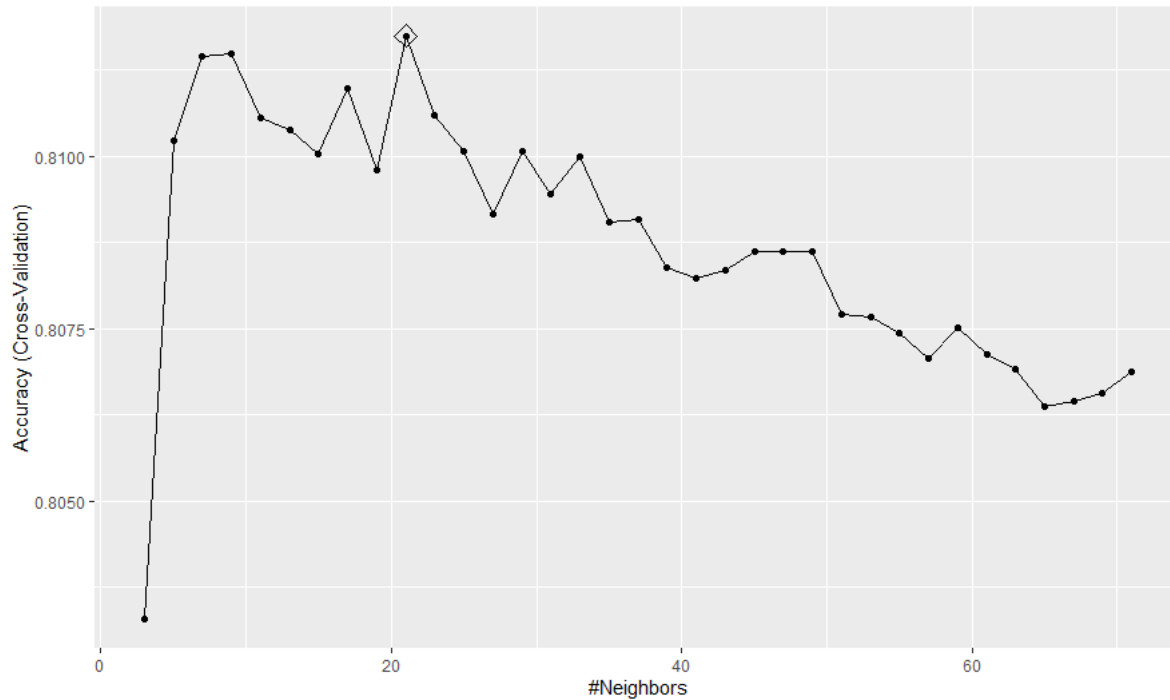


Figure 27: knn tuning

Here is the confusion matrix for the knn tuned raw model

#### Confusion Matrix and Statistics

```

Reference
Prediction FALSE TRUE
  FALSE   1992   360
   TRUE    208   358

Accuracy : 0.8053
 95% CI : (0.7905, 0.8196)
No Information Rate : 0.7539
P-Value [Acc > NIR] : 2.195e-11
    Kappa : 0.4351
McNemar's Test P-Value : 2.361e-10
    Sensitivity : 0.9055
    Specificity : 0.4986
  Pos Pred Value : 0.8469
  Neg Pred Value : 0.6325
    Prevalence : 0.7539
    Detection Rate : 0.6827
Detection Prevalence : 0.8060
Balanced Accuracy : 0.7020
'Positive' Class : FALSE

```

knn raw model produces accuracy of 0.8053, however, specificity is lower than sensitivity and prevalence is now 0.753. We now see the positive prediction is better. F1 score has improved. However, the AUC score

is less than naive bayes. This indicates that the number of true positives are lesser than before. Balanced accuracy is better. Can we do better with accuracy and precision?

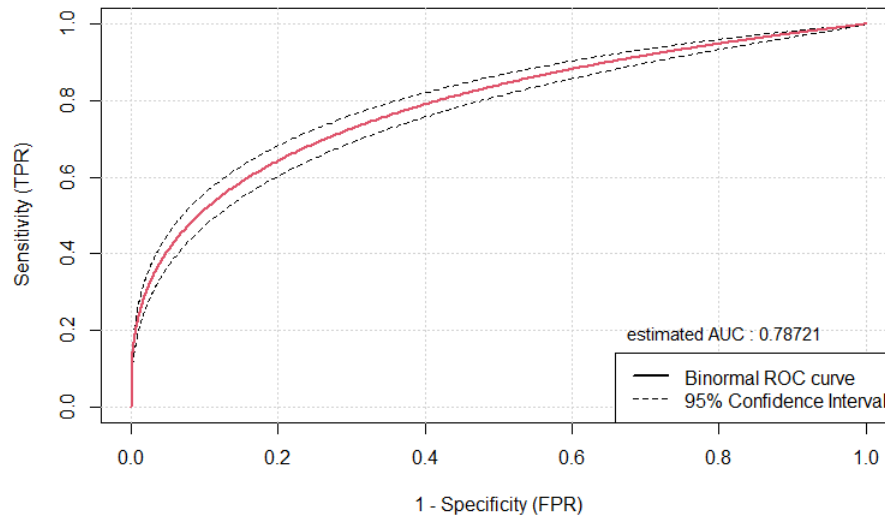


Figure 28: knn classification summary

We will now try to use classification with knn3. We will again use different values of k but using map\_df function to repeat the above for each one. Running this classification model is going to be slow as it has to iterate through all the k values and find the one that is the highest.

```
ks <- seq(3, 251, 2)

knntune <- map_df(ks, function(k) {

  temp <- adultpayclean_train %>%
    mutate(y = as.factor(income == "Above50K"))

  temp_test <- adultpayclean_validation %>%
    mutate(y = as.factor(income == "Above50K"))

  knn_fit <- knn3(y ~ age + eduyears + sex + race + hoursperweek + maritalstatus +
    relationship + education, data = temp, k = k)

  y_hat <- predict(knn_fit, temp, type = "class")

  cm_train <- confusionMatrix(y_hat, temp$y)

  train_error <- cm_train$overall["Accuracy"]

  y_hat <- predict(knn_fit, temp_test, type = "class")

  cm_test <- confusionMatrix(y_hat, temp_test$y)

  test_error <- cm_test$overall["Accuracy"]

})
```

```

    tibble(train = train_error, test = test_error)
  })

accuracy_knntune <- max(knntune$test)

# get the confusion matrix for that k

knn_fit <- knn3(y ~ age + eduyears + sex + race + hoursperweek + maritalstatus +
  relationship, data = temp, k = ks[which.max(knntune$test)])

y_hat <- predict(knn_fit, adu1tpayclean_validation, type = "class")

cm_knntune <- confusionMatrix(y_hat, as.factor(adu1tpayclean_validation$income ==
  "Above50K"))

f1_knntune

# [1] 0.87745

# Area under the curve: 0.7941

```

#### Confusion Matrix and Statistics

	Reference	
Prediction	FALSE	TRUE
FALSE	1994	351
TRUE	206	367

Accuracy : 0.8091  
 95% CI : (0.7944, 0.8232)  
 No Information Rate : 0.7539  
 P-Value [Acc > NIR] : 6.680e-13  
 Kappa : 0.448  
 McNemar's Test P-Value : 1.051e-09  
 Sensitivity : 0.9064  
 Specificity : 0.5111  
 Pos Pred Value : 0.8503  
 Neg Pred Value : 0.6405  
 Prevalence : 0.7539  
 Detection Rate : 0.6833  
 Detection Prevalence : 0.8036  
 Balanced Accuracy : 0.7088  
 'Positive' Class : FALSE

The accuracy of the knn tuned classification is 0.8091 with a sensitivity of 0.9064 and specificity of 0.5111. This is better than the previous models. Prevalence is just about the same as raw knn. Balanced accuracy has improved. F1 score is also at ~ 88% and AUC has improved a bit.

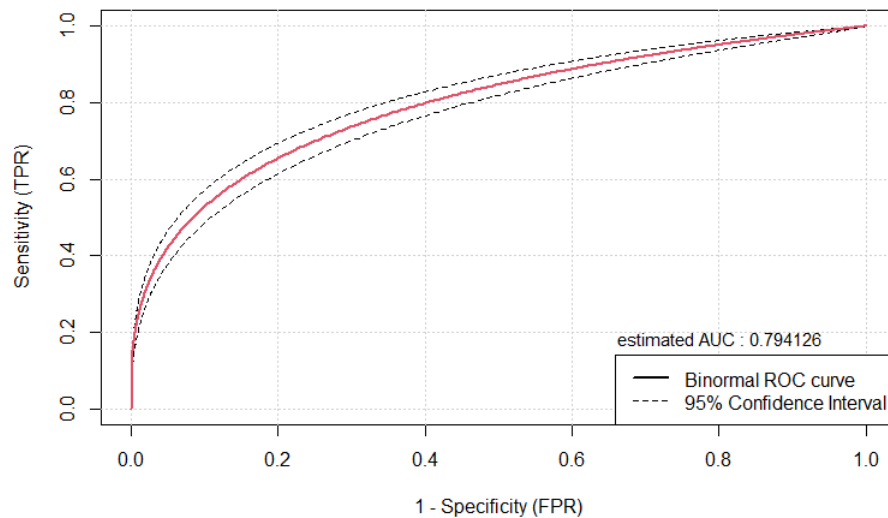


Figure 29: knn tune classification summary

## Recursive partitioning with rpart

Next we use classification trees, or decision trees. We use the recursive partitioning library `rpart` for this. The general idea is to define an algorithm that uses data to create trees with predictions at the ends, referred to as nodes. Decision trees operate by predicting a categorical outcome variable  $Y$  by partitioning the predictors.

```
train_rpart <- train(y ~ age + eduyears + sex + race + hoursperweek + maritalstatus +
  relationship + education, method = "rpart", tuneGrid = data.frame(cp = seq(0,
    0.1, len = 25)), data = temp)

y_hat <- predict(train_rpart, adu1tpayclean_validation)

accuracy_rpart <- confusionMatrix(y_hat, as.factor(adu1tpayclean_validation$income ==
  "Above50K"))$overall["Accuracy"]

accuracy_rpart
# Accuracy
# 0.8211

f1_rpart
# [1] 0.8846664
# Area under the curve: 0.81573
```

## Confusion Matrix and Statistics

		Reference	
Prediction		FALSE	TRUE
FALSE	2002	324	
TRUE	198	394	

Accuracy : 0.8211  
 95% CI : (0.8067, 0.8349)  
 No Information Rate : 0.7539  
 P-Value [Acc > NIR] : < 2.2e-16  
 Kappa : 0.4876  
 McNemar's Test P-Value : 4.472e-08  
 Sensitivity : 0.9100  
 Specificity : 0.5487  
 Pos Pred Value : 0.8607  
 Neg Pred Value : 0.6655  
 Prevalence : 0.7539  
 Detection Rate : 0.6861  
 Detection Prevalence : 0.7971  
 Balanced Accuracy : 0.7294  
 'Positive' Class : FALSE

The results of the tuning of the decision trees can be seen in this figure

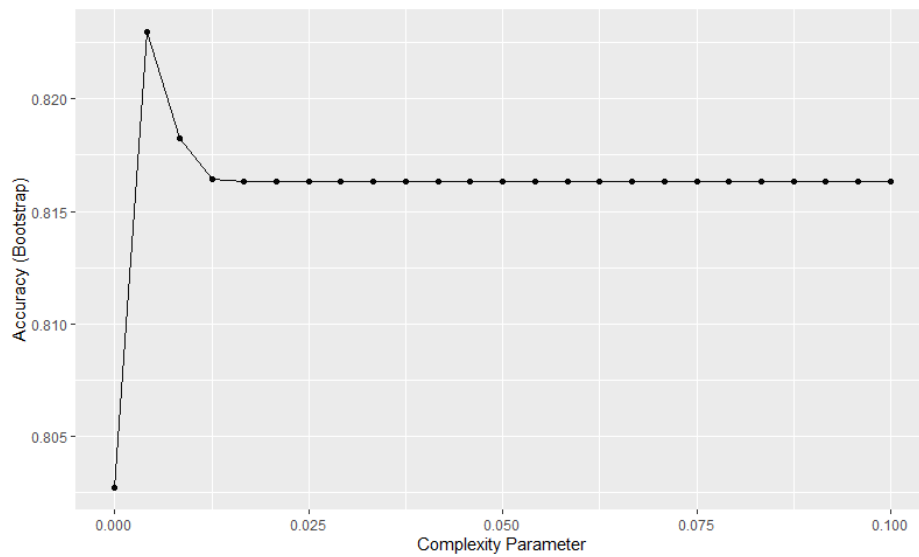


Figure 30: rpart accuracy

The rpart algorithm followed the rule below to classify the dataset



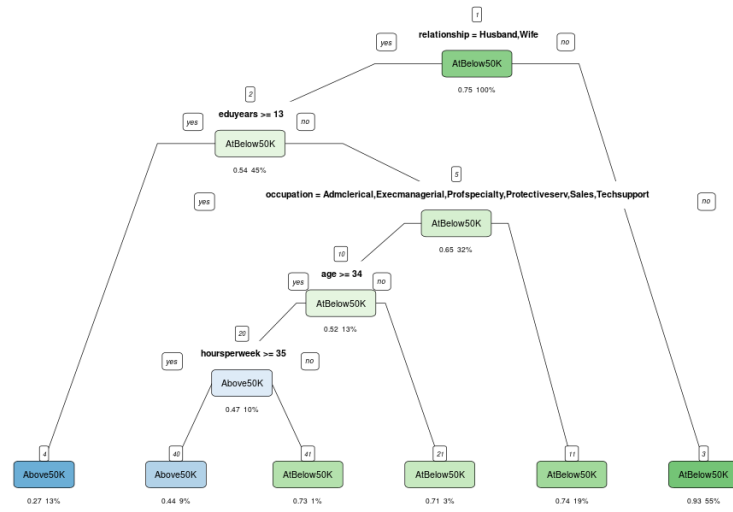


Figure 31: rpart decision tree

The accuracy of recursive partitioning is 0.8211, sensitivity is higher at 0.91 and specificity is at 0.5487 with prevalence about the same. Balanced accuracy has improved. Confidence intervals for positive and negative has improved as well. The F1 score for rpart is 0.88467 and AUC is 0.81573 which is a positive sign.

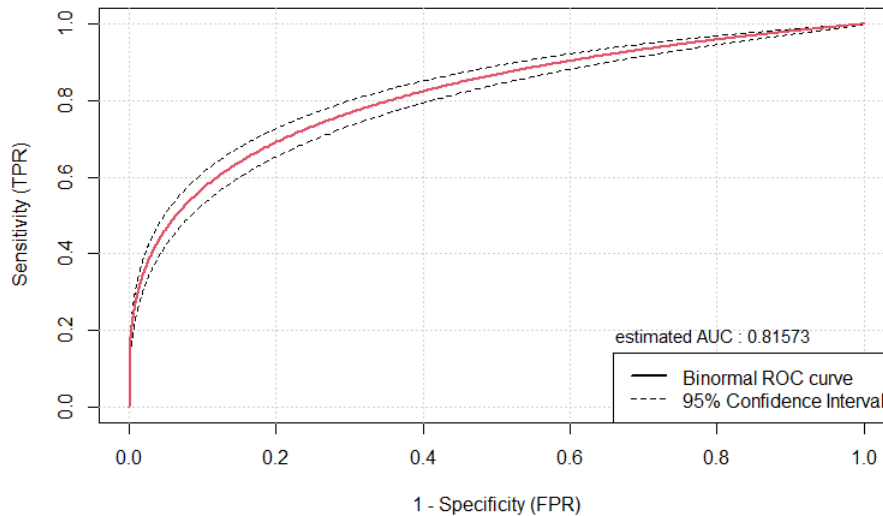


Figure 32: rpart classification summary

Classification trees have certain advantages that make them very useful. They are highly interpretable, even more so than linear models. They are easy to visualize (if small enough). Finally, they can model human decision processes and don't require use of dummy predictors for categorical variables. On the other hand, the approach via recursive partitioning can easily over-train and is therefore a bit harder to train than, for example, linear regression or kNN. Furthermore, in terms of accuracy, it is rarely the best performing method since it is not very flexible and is highly unstable to changes in training data. Random forests, explained next, improve on several of these shortcomings. We will next look at random forest algorithm.

## Random forests

The goal of random forest is to improve prediction performance and reduce instability by averaging multiple decision trees. The first step is bootstrap aggregation or bagging. The general idea is to generate many predictors, each using regression or classification trees, and then forming a final prediction based on the average prediction of all these trees. To assure that the individual trees are not the same, we use the bootstrap to induce randomness. Bagging or bootstrapping is very useful in our scenario as we have an imbalanced dataset.

```
train_rf <- randomForest(y ~ age + eduyears + sex + race + hoursperweek + maritalstatus +
  relationship + education, data = temp)

accuracy_rf <- confusionMatrix(predict(train_rf, adu1tpayclean_validation),
  ↪ as.factor(adu1tpayclean_validation$income ==
    "Above50K"))$overall["Accuracy"]

accuracy_rf

# Accuracy
```

```
# 0.8218

f1_rf

# [1] 0.88556

# Area under the curve: 0.81804

varImp(train_rf)
```

## Variable Importance

### Overall

age	696.37032
eduyears	606.59083
sex	114.11631
race	77.66081
hoursperweek	484.89859
maritalstatus	923.10055
relationship	991.96874
education	652.20573

## Confusion Matrix and Statistics

	Reference	
Prediction	FALSE	TRUE
FALSE	2012	332
TRUE	188	38

```

Accuracy : 0.8218
95% CI : (0.8074, 0.8355)
No Information Rate : 0.7539
P-Value [Acc > NIR] : < 2.2e-16
Kappa : 0.4849
Mcnemar's Test P-Value : 3.588e-10
Sensitivity : 0.9145
Specificity : 0.5376
Pos Pred Value : 0.8584
Neg Pred Value : 0.6725
Prevalence : 0.7539
Detection Rate : 0.6895
Detection Prevalence : 0.8033
Balanced Accuracy : 0.7261
'Positive' Class : FALSE
```

With "Occupation" as one of the feature

## Confusion Matrix and Statistics

Reference

Prediction	FALSE	TRUE
FALSE	1990	293
TRUE	210	425

```

Accuracy : 0.8276
95% CI : (0.8134, 0.8412)
No Information Rate : 0.7539
P-Value [Acc > NIR] : < 2.2e-16
Kappa : 0.5166
McNemar's Test P-Value : 0.000256
Sensitivity : 0.9045
Specificity : 0.5919
Pos Pred Value : 0.8717
Neg Pred Value : 0.6693
Prevalence : 0.7539
Detection Rate : 0.6820
Detection Prevalence : 0.7824
Balanced Accuracy : 0.7482
'Positive' Class : FALSE

```

The accuracy of random forest is at 0.8218, sensitivity is at 0.9145 and specificity is at 0.5376. Prevalence is about the same when compared to knn and rpart classification models. The confidence intervals is about the same as rpart. The F1 score is 0.88556 is the best so far. AUC also on the positive side. Due to the randomization of features during the random forest bootstrapping, its hard to know if all the features will be used. Fortunately, we can investigate into how often a specific feature is used in the predictions using variable importance

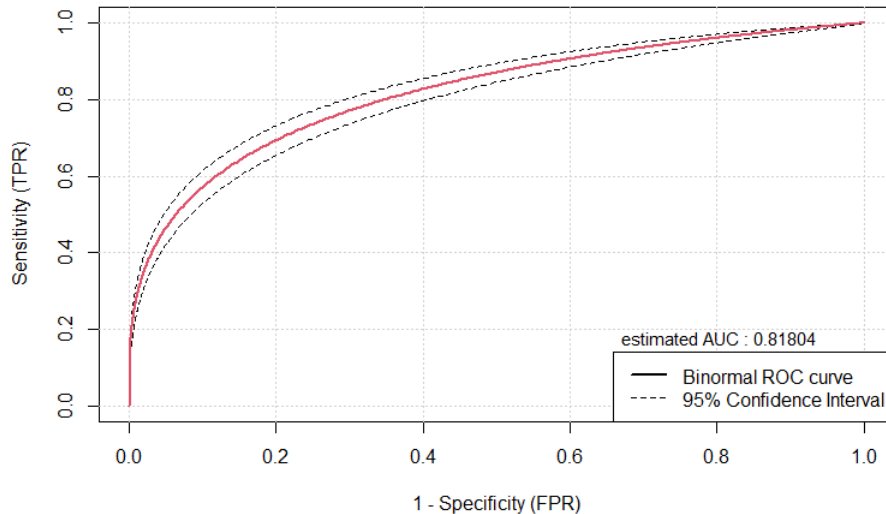


Figure 33: random forest classification summary

The out-of-bag errors and errors for Above-50K and AtBelow50K classes are shown in the classification errors figure. You can see the errors reduce as the number of trees are added and then plateau after a while. The errors are around 16% and are within acceptable limits.

When we add “Occupation” as one the feature (with some missing occupation data (5%)) we see that the

accuracy is 0.8276 and sensitivity and specificity are 0.9045 and 0.5919 respectively with a F1 score of 0.88779.

When we add “class” as one the feature (with some missing occupation data (5%)) we see that the accuracy is 0.8283 and sensitivity and specificity are 0.9077 and 0.5850 respectively with a F1 score of 0.88854.

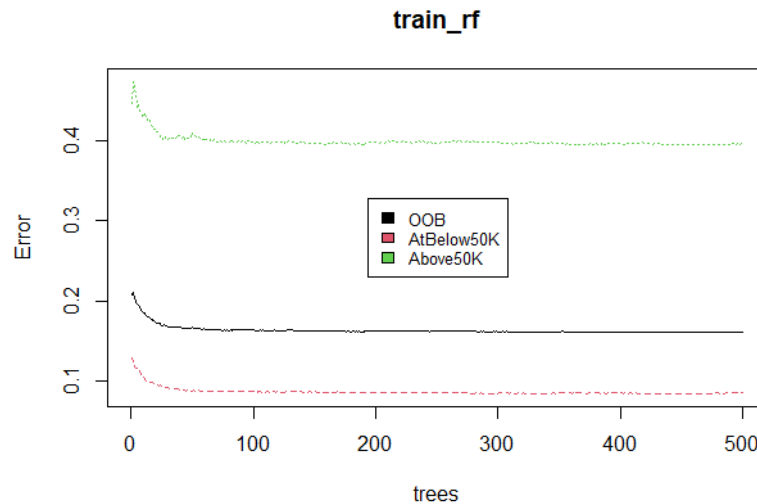


Figure 34: random forest classification errors

We can see the variable importance with occupation and class.

```
varImp(train_rf)
```

Overall

age	1296.5653
eduyears	655.8616
sex	123.8927
race	143.0220
hoursperweek	770.9115
maritalstatus	863.0918
relationship	1192.2686
education	633.8376
occupation	905.2539
class	409.0696

We can see that age, years of education, relationship, occupation and maritalstatus are the most used and sex and race are the least used features. We can also see that occupation did have a greater impact on decisioning even though we had 5% unknown data.

Lets tune this model just like the KNN3 classification and see if we can do better.

```
nodesize <- seq(1, 51, 10)

acc <- sapply(nodesize, function(ns) {
  train(y ~ age + eduyears + sex + race + hoursperweek + maritalstatus + relationship,
    method = "rf", data = temp, tuneGrid = data.frame(mtry = 2), nodesize =
    ns)$results$Accuracy
```

```

})

qplot(nodesize, acc)

train_rf_2 <- randomForest(y ~ age + eduyears + sex + race + hoursperweek + maritalstatus
↪ +
  relationship, data = temp, nodesize = nodesize[which.max(acc)])

y_hat_rf2 <- predict(train_rf_2, adultpayclean_validation)

accuracy_rftune <- confusionMatrix(predict(train_rf_2, adultpayclean_validation),
  as.factor(adultpayclean_validation$income == "Above50K"))$overall["Accuracy"]

accuracy_rftune

# Accuracy
# 0.8221

f1_rf2

# [1] \t0.88596

# Area under the curve: 0.81917

```

#### Confusion Matrix and Statistics

	Reference	
Prediction	FALSE	TRUE
FALSE	2016	335
TRUE	184	383

Accuracy : 0.8221  
 95% CI : (0.8078, 0.8359)  
 No Information Rate : 0.7539  
 P-Value [Acc > NIR] : < 2.2e-16  
 Kappa : 0.4841  
 McNemar's Test P-Value : 4.571e-11  
 Sensitivity : 0.9164  
 Specificity : 0.5334  
 Pos Pred Value : 0.8575  
 Neg Pred Value : 0.6755  
 Prevalence : 0.7539  
 Detection Rate : 0.6909  
 Detection Prevalence : 0.8057  
 Balanced Accuracy : 0.7249  
 'Positive' Class : FALSE

With "Occupation" and "class" features

#### Confusion Matrix and Statistics

Reference		
Prediction	FALSE	TRUE
FALSE	2025	293
TRUE	175	425

Accuracy : 0.83996  
 95% CI : (0.8261, 0.8531)  
 No Information Rate : 0.7539  
 P-Value [Acc > NIR] : < 2.2e-16  
 Kappa : 0.5441  
 McNemar's Test P-Value : 1.325e-07  
 Sensitivity : 0.9200  
 Specificity : 0.5947  
 Pos Pred Value : 0.8743  
 Neg Pred Value : 0.7081  
 Prevalence : 0.7539  
 Detection Rate : 0.6936  
 Detection Prevalence : 0.7934  
 Balanced Accuracy : 0.7574  
 'Positive' Class : FALSE

#### Variable Importance

varImp(train\_rf\_2)

	Overall
age	491.55809
eduyears	595.07607
sex	101.73626
race	49.67436
hoursperweek	340.57118
maritalstatus	839.06711
relationship	981.20678
education	598.69678

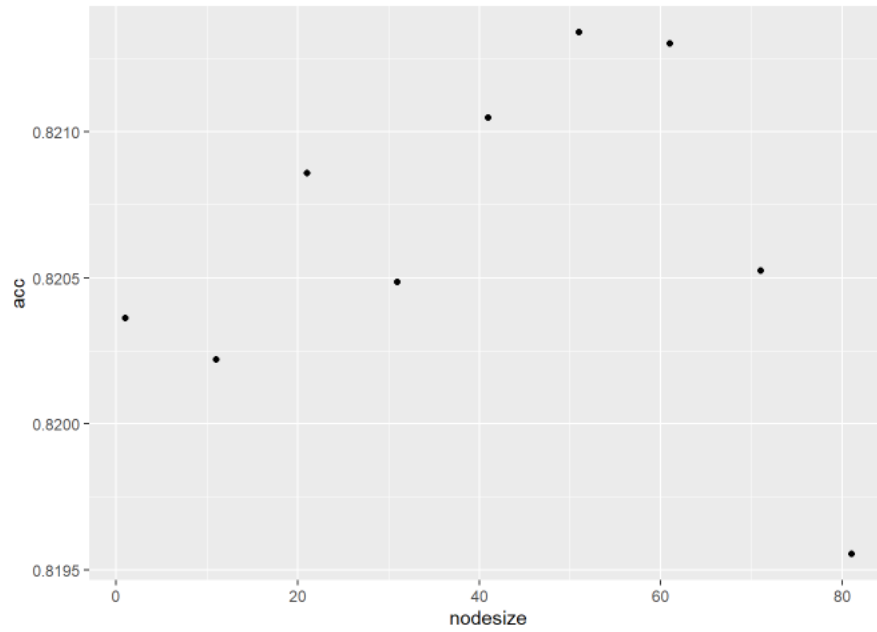


Figure 35: rf tuning

The accuracy of random forest with tuning is at 0.8221, sensitivity is at 0.916 and specificity is at 0.533. Prevalence is about the same when compared to knn and rpart classification models. The confidence intervals is just about the same as rpart and random forest without tuning. AUC improved slightly. In addition to the accuracy, precision increased to 0.8859.



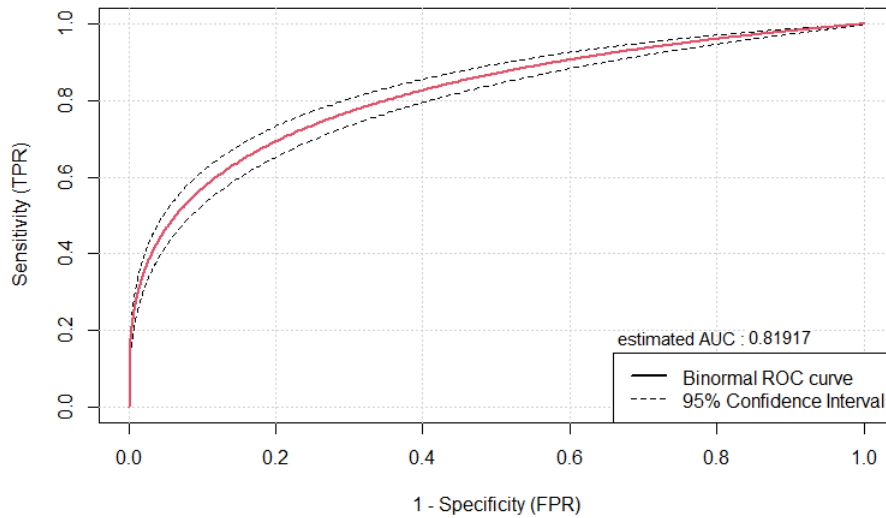


Figure 36: random forest tuned classification summary

When we added the experimental occupation and class data into the dataset for rf tuned test we see that the accuracy improves to 0.83996 and sensitivity is 0.9205 and specificity is 0.5947 with prevalence being the same as before and balanced accuracy improved to 0.7574. The F1 score for this is 0.896

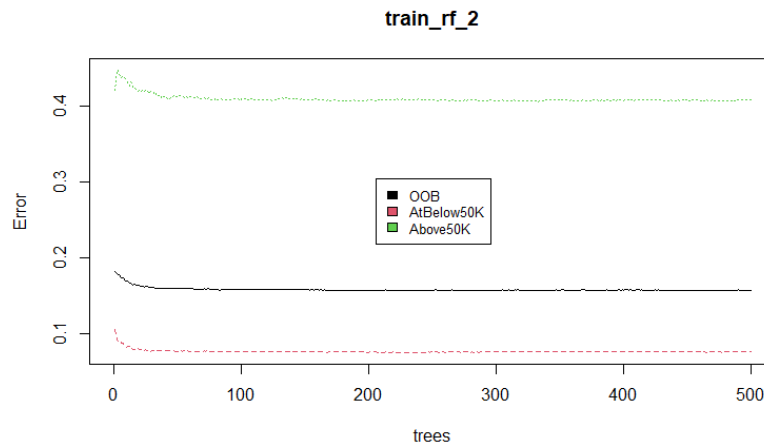


Figure 37: tuned random forest classification errors

The out-of-bag errors and errors for Above-50K and AtBelow50K classes are shown in the classification errors figure. You can see the errors reduce as the number of trees are added and then plateau after a while. The errors are around 16% and are within acceptable limits.

We can see the variable importance with occupation and class.

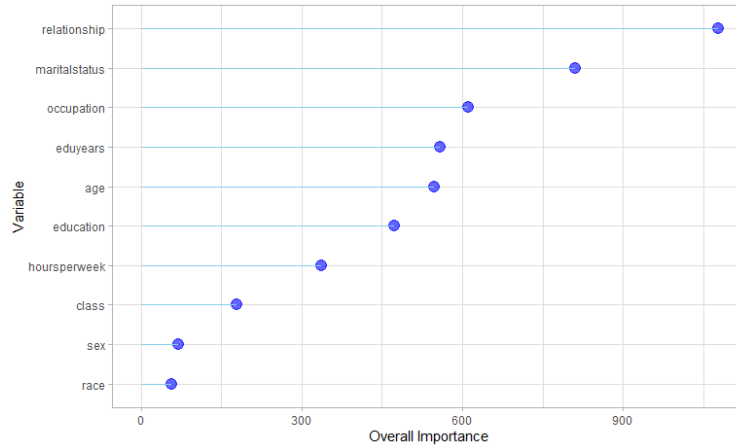


Figure 38: tuned random forest variable importance

When we compare our final model with glm, naive bayes, knn and rpart the random forest model took quite a bit of time to generate. Hence the cost of generation is high. However, on the flip side the accuracy, CI, precision is higher than other models. Prevalence plateaus once the accuracy and precision are high. The logistic and generative models like GLM, and Naive Bayes could return a faster response but sacrifices accuracy and precision and has a decent prevalence. Naive Bayes achieves a better accuracy than glm and has compatible sensitivity and specificity and lower prevalence when compared to random forest and knn. KNN is a mid-range model with speed faster than random forest but with lower accuracy and precision. It is slower than Naive Bayes and Glm.

If my objective were to get the outcomes faster with slightly lesser accuracy then I would have gone with Naive Bayes. However, if you look closer at the classification models, there is a high degree of imbalance in the dataset and naive bayes doesn't do very well when the dataset is imbalanced. F1 score of random forest is higher than naive bayes. For this reason I chose random forest over naive bayes. Further more as this is a Census pay prediction application, the frequency of runs would be lesser compared to applications like detecting if a person will get a heart attack in the next 24 hours. In such a scenario getting a faster prediction at a lower accuracy can be used to err on the safe side.

## Results

This project created a machine learning model that predicts income level of adults based on 8 shortlisted attributes and 2 experimental attributes. This model was run on a test dataset that included an income level indicator, allowing us to compare the predicted and actual value.

We chose random forest as the final model after comparison. The model returned an accuracy of 82 to 83% while predicting annual income more than \$50,000 annually. If occupation and class (with 5% unknown data) are included as features then accuracy changes to 83 to 84%. A summary table of results is given below:

	Method	Accuracy	Sensitivity	Specificity	Prevalence	F1
1.	Plain old guess	0.50822	0.50279	0.51	0.24606	0.33472
2.	linear model	0.81528	0.4429	0.93682	0.24606	0.54128
3.	General linear model	0.81049	0.38719	0.94864	0.24606	0.50135
4.	naive bayes	0.80089	0.91112	0.57218	0.67478	0.86064
5.	knn	0.80535	0.90545	0.49861	0.75394	0.87522
6.	knn tune	0.8098	0.90636	0.51114	0.75394	0.87745
7.	rpart	0.82111	0.91	0.54875	0.75394	0.88467
8.	rf	0.8218	0.91455	0.5376	0.75394	0.88556
9.	rf tune	0.83996	0.92	0.59471	0.75394	0.89657

Figure 39: Final Results

The accuracy of the predictions is backed by sensitivity of 0.9163 and specificity of 0.540. The F1 score 0.8869 vouches for the sensitivity and specificity. AUC is around 0.818 and is considered as acceptable considering some degree of imbalance in the dataset.

This model can be used to determine income levels for adults in any year with similar attribute sets and achieve comparable accuracies. The following attributes were determined to influence annual adult incomes in the US:

- age
- eduyears
- education
- sex
- race
- hoursperweek
- maritalstatus
- relationship
- occupation and class (experimental with 5% unknown data each)

## Conclusion

This machine learning model was able to predict annual incomes of persons in US based (1994) on 8 parameters with an accuracy of 82 to 83%. This model can be applied to data from other census years as well. The model will perform better if the training set is updated with new data that is confirmed for correctness, that is, the label value is the real life value, and not the predicted value. Additional data for certain features like marital status, occupation, and class will make the model better. The model can continuously learn from changing data in the training set to adapt to new parameters, thus improving its accuracy and other metrics

Further improvements could be made by using random oversampling and/or under-sampling techniques to fill the void created by imbalanced datasets.

Another approach for improving accuracy would be to create an ensemble based on multiple algorithms like rpart, random forest and glm.

Additionally, we could also use advanced algorithms like Ada Boost Gradient Boost Trees, support Vector Machines, Neural Networks, and Deep Learning to improve the predicted outcomes.

## Appendix A - Complete code

```
## @knitr CensusPayR

# Note: This script will take a while to run. In particular the knn and random
# forest algorithms with tuning grids will take more time. please be patient if
# you happen to execute it. The execution report is available in the github
# location as well

# Execute the given source code for the project
source("DatasetProcessingCode.R")

if (!require(randomForest)) install.packages("randomForest", repos =
  ↪ "http://cran.us.r-project.org")

if (!require(purrr)) install.packages("purrr", repos = "http://cran.us.r-project.org")

if (!require(e1071)) install.packages("e1071")

if (!require(pROC)) install.packages("pRoc")

if (!require(ROCit)) install.packages("ROCit")

library(caret)
library(gridExtra)
library(kableExtra)
library(randomForest)
library(purrr)
library(e1071)
library(caTools)
library(pROC)
library(ROCit)

# set the seed for reproducible results
set.seed(2008, sample.kind = "Rounding")

# the simplest possible machine algorithm: guessing the outcome
seat_of_the_pants <- sample(c("Above50K", "AtBelow50K"), length(test_index), replace =
  ↪ TRUE) %>%
  factor(levels = levels(adultpayclean_validation$income))
# calculate the accuracy of this sampling
accuracy_guess <- mean(seat_of_the_pants == adultpayclean_validation$income)

# build a confusion matrix for this simple model
table(predicted = seat_of_the_pants, actual = adultpayclean_validation$income)

# tabulate accuracy by income levels
adultpayclean_validation %>%
  mutate(y_hat = seat_of_the_pants) %>%
```

```

group_by(income) %>%
  summarize(accuracy = mean(y_hat == income))

# confusion matrix using R function
cm <- confusionMatrix(data = seat_of_the_pants, reference =
  ↪ adu1tpayclean_validation$income)
# display the confusion matrix
cm

# record the sensitivity, specificity, and prevalence
sensitivity_guess <- cm$byClass[["Sensitivity"]]
specificity_guess <- cm$byClass[["Specificity"]]
prevalence_guess <- cm$byClass[["Prevalence"]]
f1_guess <- cm$byClass[["F1"]]

# find the area under the curve/ROC
auc(ifelse(adu1tpayclean_validation$income == "Above50K", 1, 0), ifelse(seat_of_the_pants
  ↪ ==
    "Above50K", 1, 0))

set.seed(2008)
# logistic linear model create the model
lm_fit <- adu1tpayclean_train %>%
  mutate(y = as.numeric(income == "Above50K")) %>%
  lm(y ~ age + eduyears + sex + race + hoursperweek + maritalstatus + relationship +
    education, data = .)

# predict using test set
p_hat_logit <- predict(lm_fit, newdata = adu1tpayclean_validation)

# translate predicted data into factor
y_hat_logit <- ifelse(p_hat_logit > 0.5, "Above50K", "AtBelow50K") %>%
  factor

# compare the predicted vs observed values and use confusionMatrix to get the
# accuracy and other metrics
cm_lm <- confusionMatrix(y_hat_logit, adu1tpayclean_validation$income)
accuracy_lm <- confusionMatrix(y_hat_logit,
  ↪ adu1tpayclean_validation$income)$overall[["Accuracy"]]

cm_lm

# record the sensitivity, specificity, and prevalence
sensitivity_lm <- cm_lm$byClass[["Sensitivity"]]
specificity_lm <- cm_lm$byClass[["Specificity"]]
prevalence_lm <- cm_lm$byClass[["Prevalence"]]
f1_lm <- cm_lm$byClass[["F1"]]

# Find the ROC and plot it. Show the AUC as well
pROC_bin <- ROCit::rocit(ifelse(adu1tpayclean_validation$income == "Above50K", 1,
  0), ifelse(unname(y_hat_logit) == "Above50K", 1, 0), method = "bin")
ciROC_bin95 <- ROCit::ciROC(pROC_bin, level = 0.95)
plot(ciROC_bin95, col = 1, values = TRUE)

```

```

lines(ciROC_bin95$TPR ~ ciROC_bin95$FPR, col = 2, lwd = 2)
ROCit::ciAUC(pROC_bin)

set.seed(2008)
# general linear model create the glm model
glm_fit <- adultpayclean_train %>%
  mutate(y = as.numeric(income == "Above50K")) %>%
  glm(y ~ age + eduyears + sex + race + hoursperweek + maritalstatus + relationship +
    education, data = ., family = "binomial")

# predict using validation set
p_hat_logit <- predict(glm_fit, newdata = adultpayclean_validation)

# translate the predicted data into factor
y_hat_logit <- ifelse(p_hat_logit > 0.5, "Above50K", "AtBelow50K") %>%
  factor

# compare the predicted vs observed values and use confusionMatrix to get the
# accuracy and other metrics for the glm model
cm_glm <- confusionMatrix(y_hat_logit, adultpayclean_validation$income)
accuracy_glm <- confusionMatrix(y_hat_logit,
  ↪ adultpayclean_validation$income)$overall[["Accuracy"]]

cm_glm

# record the sensitivity, specificity, and prevalence
sensitivity_glm <- cm_glm$byClass[["Sensitivity"]]
specificity_glm <- cm_glm$byClass[["Specificity"]]
prevalence_glm <- cm_glm$byClass[["Prevalence"]]
f1_glm <- cm_glm$byClass[["F1"]]

# Find the ROC and plot it. Show the AUC as well
pROC_bin <- ROCit::rocit(ifelse(adultpayclean_validation$income == "Above50K", 1,
  0), ifelse(unname(y_hat_logit) == "Above50K", 1, 0), method = "bin")
ciROC_bin95 <- ROCit::ciROC(pROC_bin, level = 0.95)
plot(ciROC_bin95, col = 1, values = TRUE)
lines(ciROC_bin95$TPR ~ ciROC_bin95$FPR, col = 2, lwd = 2)
ROCit::ciAUC(pROC_bin)

# Naive bayes
set.seed(2008)
# create the naive bayes model
train_nb <- adultpayclean_train %>%
  mutate(y = as.factor(income == "Above50K")) %>%
  naiveBayes(y ~ age + eduyears + sex + race + hoursperweek + maritalstatus +
    ↪ relationship +
    education, data = .)

# predict using the validation dataset
y_hat_nb <- predict(train_nb, newdata = adultpayclean_validation)
# create the confusion matrix
cm_tab <- table(adultpayclean_validation$income == "Above50K", y_hat_nb)
cm_nb <- confusionMatrix(cm_tab)

```

```

cm_nb

# get the accuracy, sensitivity, specificity, prevalence and, F1 score
accuracy_nb <- cm_nb$overall[["Accuracy"]]
sensitivity_nb <- cm_nb$byClass[["Sensitivity"]]
specificity_nb <- cm_nb$byClass[["Specificity"]]
prevalence_nb <- cm_nb$byClass[["Prevalence"]]
f1_nb <- cm_nb$byClass[["F1"]]

# Find the ROC and plot it. Show the AUC as well
pROC_bin <- ROCit::rocit(ifelse(adultpayclean_validation$income == "Above50K", 1,
0), ifelse(unname(y_hat_nb) == "TRUE", 1, 0), method = "bin")
ciROC_bin95 <- ROCit::ciROC(pROC_bin, level = 0.95)
plot(ciROC_bin95, col = 1, values = TRUE)
lines(ciROC_bin95$TPR ~ ciROC_bin95$FPR, col = 2, lwd = 2)
ROCit::ciAUC(pROC_bin)

# translate income factor into binary outcome
temp <- adultpayclean_train %>%
  mutate(y = as.factor(income == "Above50K"))

# k-nearest neighbors with a train control and tuning
set.seed(2008)
# train control to use 10% of the observations each to speed up computations
control <- trainControl(method = "cv", number = 10, p = 0.9)
# train the model using knn. choose the best k value using tuning algorithm
train_knn <- train(y ~ age + eduyears + sex + race + hoursperweek + maritalstatus +
  relationship + education, method = "knn", data = temp, tuneGrid = data.frame(k =
  seq(3,
    71, 2)), trControl = control)

# plot the resulting model
ggplot(train_knn, highlight = TRUE)
# verify which k value was used
train_knn$bestTune
train_knn$finalModel

# use this trained model to predict raw knn predictions
y_hat_knn <- predict(train_knn, adultpayclean_validation, type = "raw")

# compare the predicted and observed values using confusionMatrix to get the
# accuracy and other metrics
cm_knn <- confusionMatrix(y_hat_knn, as.factor(adultpayclean_validation$income ==
"Above50K"))
accuracy_knn <- confusionMatrix(y_hat_knn, as.factor(adultpayclean_validation$income ==
"Above50K"))$overall[["Accuracy"]]

cm_knn

# record the sensitivity, specificity, and prevalence
sensitivity_knn <- cm_knn$byClass[["Sensitivity"]]
specificity_knn <- cm_knn$byClass[["Specificity"]]
prevalence_knn <- cm_knn$byClass[["Prevalence"]]

```

```

f1_knn <- cm_knn$byClass[["F1"]]

# Find the ROC and plot it. Show the AUC as well
pROC_bin <- ROCit::rocit(ifelse(adultpayclean_validation$income == "Above50K", 1,
0), ifelse(unname(y_hat_knn) == "TRUE", 1, 0), method = "bin")
ciROC_bin95 <- ROCit::ciROC(pROC_bin, level = 0.95)
plot(ciROC_bin95, col = 1, values = TRUE)
lines(ciROC_bin95$TPR ~ ciROC_bin95$FPR, col = 2, lwd = 2)
ROCit::ciAUC(pROC_bin)

# k-nearest classification using tuning function
set.seed(2008)

# train the model using knn3 classification
ks <- seq(3, 251, 2)
knntune <- map_df(ks, function(k) {
  temp <- adultpayclean_train %>%
    mutate(y = as.factor(income == "Above50K"))
  temp_test <- adultpayclean_validation %>%
    mutate(y = as.factor(income == "Above50K"))
  # create the knn3 model
  knn_fit <- knn3(y ~ age + eduyears + sex + race + hoursperweek + maritalstatus +
    relationship + education, data = temp, k = k)
  # predict the model for the current k
  y_hat <- predict(knn_fit, temp, type = "class")
  # get the confusionmatrix for the current k
  cm_train <- confusionMatrix(y_hat, temp$y)
  train_error <- cm_train$overall["Accuracy"]
  # do the same for test model
  y_hat <- predict(knn_fit, temp_test, type = "class")
  cm_test <- confusionMatrix(y_hat, temp_test$y)
  test_error <- cm_test$overall["Accuracy"]

  tibble(train = train_error, test = test_error)
})
# get the accuracy for the k with maximum accuracy
accuracy_knntune <- max(knntune$test)
# get the confusion matrix for that k
knn_fit <- knn3(y ~ age + eduyears + sex + race + hoursperweek + maritalstatus +
  relationship + education, data = temp, k = ks[which.max(knntune$test)])
# predict the knn tune using the model for the k neighbor
y_hat_knntune <- predict(knn_fit, adultpayclean_validation, type = "class")
cm_knntune <- confusionMatrix(y_hat_knntune, as.factor(adultpayclean_validation$income ==
"Above50K"))

cm_knntune

# record the sensitivity, specificity, and prevalence
sensitivity_knntune <- cm_knntune$byClass[["Sensitivity"]]
specificity_knntune <- cm_knntune$byClass[["Specificity"]]
prevalence_knntune <- cm_knntune$byClass[["Prevalence"]]

```



```

f1_knntune <- cm_knntune$byClass[["F1"]]

# Find the ROC and plot it. Show the AUC as well
pROC_bin <- ROCit::rocit(ifelse(adultpayclean_validation$income == "Above50K", 1,
0), ifelse(unname(y_hat_knntune) == "TRUE", 1, 0), method = "bin")
ciROC_bin95 <- ROCit::ciROC(pROC_bin, level = 0.95)
plot(ciROC_bin95, col = 1, values = TRUE)
lines(ciROC_bin95$TPR ~ ciROC_bin95$FPR, col = 2, lwd = 2)
ROCit::ciAUC(pROC_bin)

# recursive partitioning using rpart
set.seed(2008)
# train the model with the recursive partitioning
train_rpart <- train(y ~ age + eduyears + sex + race + hoursperweek + maritalstatus +
relationship + education, method = "rpart", tuneGrid = data.frame(cp = seq(0,
0.1, len = 25)), data = temp)
# predict the outcomes with this model
y_hat_rpart <- predict(train_rpart, adultpayclean_validation)
# confusion matrix for the rpart model
cm_rpart <- confusionMatrix(y_hat_rpart, as.factor(adultpayclean_validation$income ==
"Above50K"))
# get the accuracy
accuracy_rpart <- confusionMatrix(y_hat_rpart, as.factor(adultpayclean_validation$income
↪ ==
"Above50K"))$overall["Accuracy"]

cm_rpart
# record the sensitivity, specificity, and prevalence
sensitivity_rpart <- cm_rpart$byClass[["Sensitivity"]]
specificity_rpart <- cm_rpart$byClass[["Specificity"]]
prevalence_rpart <- cm_rpart$byClass[["Prevalence"]]
f1_rpart <- cm_rpart$byClass[["F1"]]

# Find the ROC and plot it. Show the AUC as well
pROC_bin <- ROCit::rocit(ifelse(adultpayclean_validation$income == "Above50K", 1,
0), ifelse(unname(y_hat_rpart) == "TRUE", 1, 0), method = "bin")
ciROC_bin95 <- ROCit::ciROC(pROC_bin, level = 0.95)
plot(ciROC_bin95, col = 1, values = TRUE)
lines(ciROC_bin95$TPR ~ ciROC_bin95$FPR, col = 2, lwd = 2)
ROCit::ciAUC(pROC_bin)

# random forest
set.seed(2008)
# train the vanilla random forest model
train_rf <- randomForest(y ~ age + eduyears + sex + race + hoursperweek + maritalstatus +
relationship + education, data = temp)

y_hat_rf <- predict(train_rf, adultpayclean_validation)

# create the confusionMatrix
cm_rf <- confusionMatrix(y_hat_rf, as.factor(adultpayclean_validation$income ==
↪ "Above50K"))
# get the accuracy

```

```

accuracy_rf <- confusionMatrix(y_hat_rf, as.factor(adultpayclean_validation$income ==
  "Above50K"))$overall["Accuracy"]

cm_rf

# record the sensitivity, specificity, and prevalence
sensitivity_rf <- cm_rf$byClass[["Sensitivity"]]
specificity_rf <- cm_rf$byClass[["Specificity"]]
prevalence_rf <- cm_rf$byClass[["Prevalence"]]
f1_rf <- cm_rf$byClass[["F1"]]

# Find the ROC and plot it. Show the AUC as well
pROC_bin <- ROCit::rocit(ifelse(adultpayclean_validation$income == "Above50K", 1,
  0), ifelse(unname(y_hat_rf) == "TRUE", 1, 0), method = "bin")
ciROC_bin95 <- ROCit::ciROC(pROC_bin, level = 0.95)
plot(ciROC_bin95, col = 1, values = TRUE)
lines(ciROC_bin95$TPR ~ ciROC_bin95$FPR, col = 2, lwd = 2)
ROCit::ciAUC(pROC_bin)

# Plot the error rate chart for the random forest
plot(train_rf)
legend("center", ifelse(colnames(train_rf$err.rate) == "FALSE", "AtBelow50K",
  ↪ ifelse(colnames(train_rf$err.rate) ==
    "TRUE", "Above50K", "OOB")), col = 1:4, cex = 0.8, fill = 1:4)

set.seed(2008)
# random forest with tuning
nodesize <- seq(1, 90, 10)
acc <- sapply(nodesize, function(ns) {
  # train the model with tuning
  train(y ~ age + edueyears + sex + race + hoursperweek + maritalstatus + relationship +
    education, method = "rf", data = temp, tuneGrid = data.frame(mtry = 2), nodesize
  ↪ = ns)$results$Accuracy
})
qplot(nodesize, acc)

set.seed(2008)
# get the trained model for the max node size
train_rf_2 <- randomForest(y ~ age + edueyears + sex + race + hoursperweek + maritalstatus
  ↪ +
    relationship + education, data = temp, nodesize = nodesize[which.max(acc)])
# predict the outcomes
y_hat_rf2 <- predict(train_rf_2, adultpayclean_validation)
# get the confusion matrix for random forest model
cm_rf2 <- confusionMatrix(y_hat_rf2, as.factor(adultpayclean_validation$income ==
  "Above50K"))
# get the accuracy
accuracy_rftune <- confusionMatrix(y_hat_rf2, as.factor(adultpayclean_validation$income
  ↪ ==
    "Above50K"))$overall["Accuracy"]

cm_rf2

```

```

# record the sensitivity, specificity, and prevalence
sensitivity_rf2 <- cm_rf2$byClass[["Sensitivity"]]
specificity_rf2 <- cm_rf2$byClass[["Specificity"]]
prevalence_rf2 <- cm_rf2$byClass[["Prevalence"]]
f1_rf2 <- cm_rf2$byClass[["F1"]]

# Find the ROC and plot it. Show the AUC as well
pROC_bin <- ROCit::rocit(ifelse(adultpayclean_validation$income == "Above50K", 1,
0), ifelse(unname(y_hat_rf2) == "TRUE", 1, 0), method = "bin")
ciROC_bin95 <- ROCit::ciROC(pROC_bin, level = 0.95)
plot(ciROC_bin95, col = 1, values = TRUE)
lines(ciROC_bin95$TPR ~ ciROC_bin95$FPR, col = 2, lwd = 2)
ROCit::ciAUC(pROC_bin)

# Plot the error rate chart for the random forest
plot(train_rf_2)
legend("center", ifelse(colnames(train_rf_2$err.rate) == "FALSE", "AtBelow50K",
↪ ifelse(colnames(train_rf_2$err.rate) ==
"TRUE", "Above50K", "OOB")), col = 1:4, cex = 0.8, fill = 1:4)

# tabulate all the accuracy results with sensitivity and specificity
accuracy_results <- matrix(c("Plain old guess", round(accuracy_guess, 5),
↪ round(sensitivity_guess,
5), round(specificity_guess, 5), round(prevalence_guess, 5), round(f1_guess,
5), "linear model", round(accuracy_lm, 5), round(sensitivity_lm, 5),
↪ round(specificity_lm,
5), round(prevalence_lm, 5), round(f1_lm, 5), "General linear model",
↪ round(accuracy_glm,
5), round(sensitivity_glm, 5), round(specificity_glm, 5), round(prevalence_glm,
5), round(f1_glm, 5), "naive bayes", round(accuracy_nb, 5), round(sensitivity_nb,
5), round(specificity_nb, 5), round(prevalence_nb, 5), round(f1_nb, 5), "knn",
round(accuracy_knn, 5), round(sensitivity_knn, 5), round(specificity_knn, 5),
round(prevalence_knn, 5), round(f1_knn, 5), "knn tune", round(accuracy_knntune,
5), round(sensitivity_knntune, 5), round(specificity_knntune, 5),
↪ round(prevalence_knntune,
5), round(f1_knntune, 5), "rpart", round(accuracy_rpart, 5),
↪ round(sensitivity_rpart,
5), round(specificity_rpart, 5), round(prevalence_rpart, 5), round(f1_rpart,
5), "rf", round(accuracy_rf, 5), round(sensitivity_rf, 5), round(specificity_rf,
5), round(prevalence_rf, 5), round(f1_rf, 5), "rf tune", round(accuracy_rftune,
5), round(sensitivity_rf2, 5), round(specificity_rf2, 5), round(prevalence_rf2,
5), round(f1_rf2, 5)), nrow = 9, ncol = 6, byrow = TRUE, dimnames = list(c("1.",
"2.", "3.", "4.", "5.", "6.", "7.", "8.", "9."), c("Method", "Accuracy",
↪ "Sensitivity",
"Specificity", "Prevalence", "F1")))
# style the table with knitr
accuracy_results %>%
knitr::kable() %>%
kable_styling(bootstrap_options = c("striped", "hover", "condensed"))

```

## Appendix B - Code Execution

The code in this project takes long time to execute. Please find the execution summary at the link below.

<https://github.com/rajeshharidas/havardxwork2/blob/main/CensusPayExecutionSummary.pdf>

<https://github.com/rajeshharidas/havardxwork2/blob/main/DatasetProcessingCode.pdf>

<https://github.com/rajeshharidas/havardxwork2/blob/main/CensusPayExecutionSummary.html>

<https://github.com/rajeshharidas/havardxwork2/blob/main/DatasetProcessingCode.html>

## Appendix C - Links

<https://www.edx.org/professional-certificate/harvardx-data-science>

<https://www.crcpress.com/Introduction-to-Data-Science-Data-Analysis-and-Prediction-Algorithms-with-Irizarry/p/book/9780367357986>

<https://leanpub.com/datasciencebook>

## Citations

Irizarry, Rafael A., “Introduction to Data Science: Data Analysis and Prediction Algorithms in R” <https://rafalab.github.io/dsbook/>

ML-Friendly kaggle dataset for adult census income - <https://www.kaggle.com/uciml/adult-census-income>