

# Supersymmetry and the Rationally Extended Harmonic Oscillator

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## Abstract

Our focus is on the rationally extended harmonic oscillator potential, which is isospectral to conventional simple harmonic oscillator potential and its solutions are linked with the exceptional  $X_m$ -Orthogonal polynomials of codimension  $m$ . We broaden our study by introducing a one-parameter ( $\lambda$ ) set of exactly solvable isospectral potentials, each providing a unique quantum signature. We pay particular attention to instances where  $\lambda = 0$  and  $\lambda = -1$ , which align with the fascinating Pursey and Abhram-Moses potentials, respectively. Our in-depth analysis covers the entire isospectral family, offering a fresh viewpoint on the exceptional polynomials.

**Keywords:** Supersymmetry, Rationally Extended Harmonic Oscillator, Exceptional Orthogonal Polynomials, Pursey Potential, Abhram-Moses Potential, isospectral Potential.

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