ToothGrowth Vitamin C Data Study

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Statistical Inference Project

Synopsis

This study shows the statistical inference analysis of ToothGrowth data set. Null hypothesis test is performed as part of this project.

Raw Data

ToothGrowth data set is a study of the effects of Vitamin C on tooth growth in guinea pigs. Parameters used in this data are:

Parameter Description of the parameter

len The response value of the length of odontoblasts (teeth)

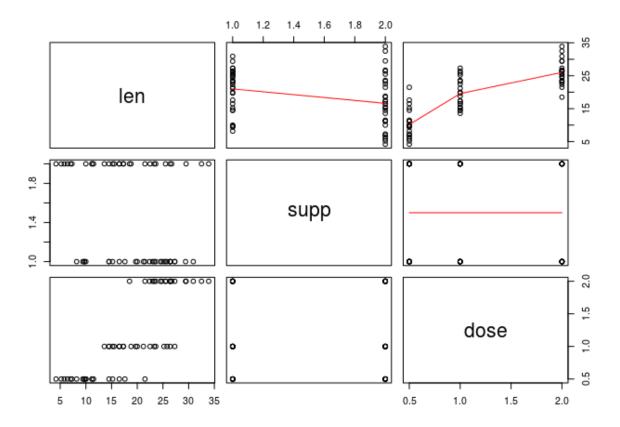
supp Delivery method of the Vitamin C by orange juice (OJ) or by ascorbic acid (VC)

dose The dosage amount of the Vitamin C with typical values of 0.5, 1.0, and 2.0 mg

Exploratory Data Analysis

Each of the parameters are shown in a 'pairs' plot, which shows that the variation of response to the two parameters of supply method and dosage.

```
library(datasets)
library(ggplot2)
data(ToothGrowth)
names(ToothGrowth)
## [1] "len" "supp" "dose"
pairs(ToothGrowth, upper.panel = panel.smooth)
```



When using a linear regression to the response variable of tooth length, the two input parameters are found to have linear trends that can be modeled with the data.

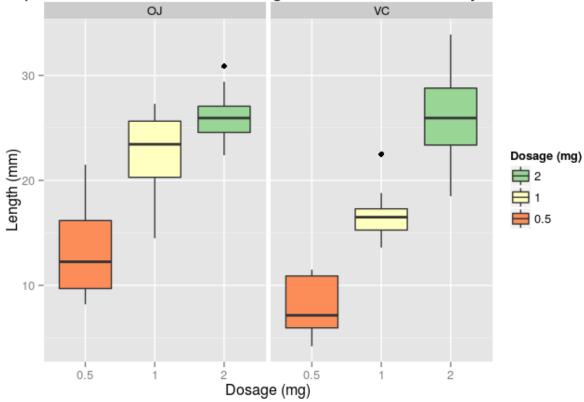
```
fit <- lm(len ~ ., data=ToothGrowth)</pre>
summary(fit)
##
## lm(formula = len ~ ., data = ToothGrowth)
##
## Residuals:
##
     Min
              1Q Median
                            3Q
                                 Max
## -6.600 -3.700 0.373 2.116 8.800
##
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
                                   7.231 1.31e-09 ***
## (Intercept)
                9.2725
                           1.2824
## suppVC
               -3.7000
                            1.0936 -3.383
                                            0.0013 **
## dose
                9.7636
                           0.8768 11.135 6.31e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 4.236 on 57 degrees of freedom
## Multiple R-squared: 0.7038, Adjusted R-squared: 0.6934
```

```
## F-statistic: 67.72 on 2 and 57 DF, p-value: 8.716e-16
```

A plot of the response variable len is shown with the input of dosage and colored for the two types of supply methods for the vitamin C.

```
ggplot(ToothGrowth, aes(x=factor(dose), y=len, fill=factor(dose))) +
  geom_boxplot() +
  scale_fill_brewer(palette="Spectral", name="Dosage (mg)") +
  guides(fill = guide_legend(reverse=TRUE)) +
  xlab("Dosage (mg)") +
  ylab("Length (mm)") +
  facet_grid(.~supp) +
  ggtitle("Response of Tooth Growth to Dosage and Vitamin C Delivery Method")
```

Response of Tooth Growth to Dosage and Vitamin C Delivery Method



Confidence Intervals/Tests

Were the results of the tests and/or intervals interpreted in the context of the problem correctly?

The null hypothesis condition is that there is no difference between the two supply methods that contributes to Guinea pig tooth growth. The alternate hypothesis is that the delivery method (orange juice or ascorbic acid) does have a difference in the tooth length response. These

hypothesis tests are performed using the t.test function with the length (len) vs supply method (supp) variables.

```
data half<-subset(ToothGrowth, dose==0.5)</pre>
data one<-subset(ToothGrowth, dose==1)</pre>
data_two<-subset(ToothGrowth, dose==2)</pre>
t.test(len ~ supp, data=ToothGrowth, paired = TRUE) # Null hypothesis test for entire
data set
##
## Paired t-test
##
## data: len by supp
## t = 3.3026, df = 29, p-value = 0.00255
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
## 1.408659 5.991341
## sample estimates:
## mean of the differences
                        3.7
t.test(len ~ supp, data=data_half, paired = TRUE) # Null hypothesis test for 0.5 mg
dosage
##
## Paired t-test
##
## data: len by supp
## t = 2.9791, df = 9, p-value = 0.01547
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
## 1.263458 9.236542
## sample estimates:
## mean of the differences
t.test(len ~ supp, data=data_one, paired = TRUE) # Null hypothesis test for 1.0 mg
dosage
##
## Paired t-test
## data: len by supp
## t = 3.3721, df = 9, p-value = 0.008229
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
## 1.951911 9.908089
## sample estimates:
## mean of the differences
                       5.93
t.test(len ~ supp, data=data_two, paired = TRUE) # Null hypothesis test for 2.0 mg
dosage
##
## Paired t-test
##
## data: len by supp
## t = -0.0426, df = 9, p-value = 0.967
## alternative hypothesis: true difference in means is not equal to 0
```

```
## 95 percent confidence interval:
## -4.328976  4.168976
## sample estimates:
## mean of the differences
## -0.08
```

Discussion

For the full data set, it was clear that there is an overall difference and that orange juice has a stronger effect to promote longer Guinea pig tooth length.

For the dosage levels of 1.0 and 2.0 mg, there was a clear test to reject the null hypothesis. This suggests that orange juice has a stronger contribution to tooth growth over ascorbic acid.

The dosage of 0.5 mg had a mean value of the differences that was below 0 and suggests that the null hypothesis is NOT to be rejected. This suggests that there are no observed difference in tooth growth between supply methods of orange juice and ascorbic acid at low dosage levels of 0.5 mg.

Assumptions

The primary assumption in this analysis is that tooth growth was measured at a specified length of time during the study. In other words, if the testing occurred at variable lengths of time that were not standardized, the growth of the teeth may have been simply due to natural growth.

Conclusions

Student's t-tests were performed on the data set to determine the effects of Vitamin C on Guinea pig tooth length. The results of this study found that orange juice (OJ) has a greater effect on Guinea Pig tooth growth when delivered at 1.0 to 2.0 mg per dosage. There was no discernible difference of Guinea pig tooth length measurements when comparing the supply methods of orange juice and ascorbic acid while delivered at a 0.5 mg dosage level.